

Arrays:

Index: 1st 2nd 3rd 4th 5th 6th

Index: 0 1 2 3 4 5 6

Int ar[6] = -3 2 5 6 7 8

ar[N] = first element : ar[0] $\underline{[0, N-1]} = N \text{ elements}$

last element : ar[N-1]

// To access index i^{th} element : ar[i] $\Rightarrow O(1)$

// Print an arr[N]

$i=0; i < N; i++\}$ } $\underline{\text{TC: } O(N)}$
|
| print(arr[i]) |

Q) Given N array elements, count no. of elements having

at least 1 Element greater than itself. [No External Libraries]

arr[7]: { -3, -2, 6, 8, 4, 8, 5 } output: 5
Observations:
1) For max element there won't be an element

arr[8]: { 2, 3, 10, 7, 3, 10, 2, 10, 3 } output: 5
greater than that.
2) Calculate No if Max Val = X
3) Final: $N - X$

Steps

1) Find Max ↗

2) Calculate No. of Max = Count

3) Avg: N - Count

// Find max of array

int man = 0 / ar[0] / INT_MIN

i = 0; i < N; i++) {

if (ar[i] > man) {

man = ar[i]

int Cnt = 0

i = 0; i < N; i++) {

if (man == ar[i]) {

Cnt++

return N - Cnt

If array contains negative.

TC: O(N)
SC: O(1)

TO DO HW

Trying i using a
single loop.

// 2Q)

Given N array elements, to return true/false checks if there exists a pair (i, j) such that $ar[i] + ar[j] = k$ eg $i=1, j=2$ } $i \neq j$ index

[No ExtraSpace / No External Library]

$ar[] : 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6$
 $ar[] : 3 \quad -2 \quad 1 \quad 4 \quad 3 \quad 6 \quad 8$

$k=10 :$ i
 3 j
 5 } $ar[3] + ar[5] = 10 = ar[5] + ar[3]$

$k=8 :$ No pair

Idea: Generate all pairs sum $\neq k$

$ar[4] : 0 \quad 1 \quad 2 \quad 3$

$i=0; i < N; i++ \{$

$j=0; j < N; j++ \{$

$i == j$

if ($i == j$) { continue }

if ($ar[i] + ar[j] == k$) {

return true

}

}

}

}

return false

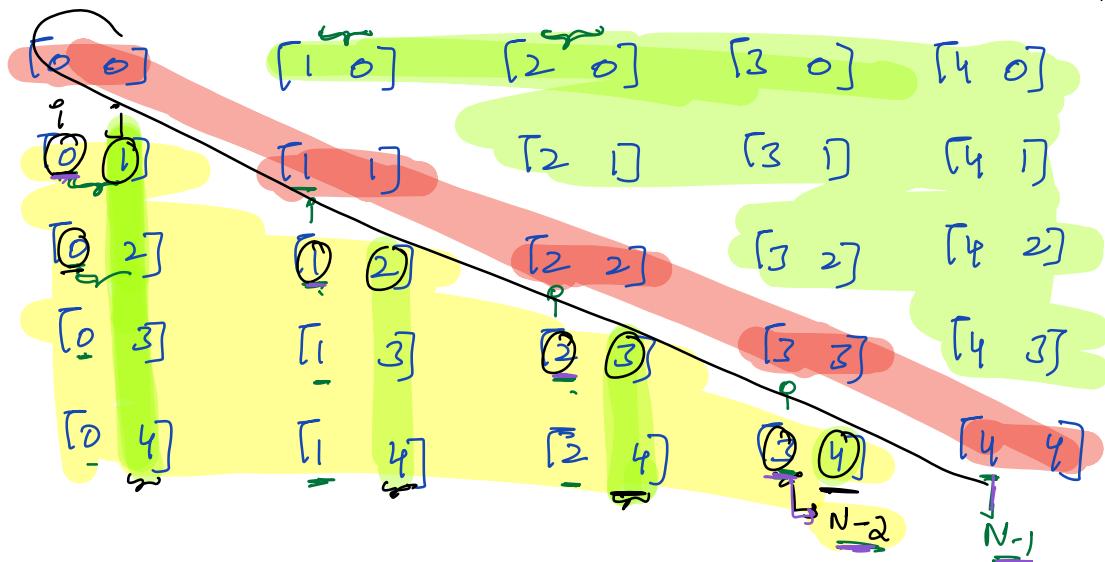
Iterations: $\underline{\underline{N^2}}$

T.C: $O(N^2)$

S.C: $O(1)$

$$ar[5] : 0 \ 1 \ 2 \ 3 \ 4 \quad \leftarrow ar[i] + ar[j] = ar[j] + ar[i]$$

$N=5$



// Iteration in lower triangular pattern.

$$i = 0; i < N-1; i++ \{$$

$$j = i+1; j < N; j++ \{$$

if ($ar[i] + ar[j] == k$) {

return True

}

// Sum of N Natural

$$\Rightarrow \frac{(N)(N+1)}{2}$$

Iterations :

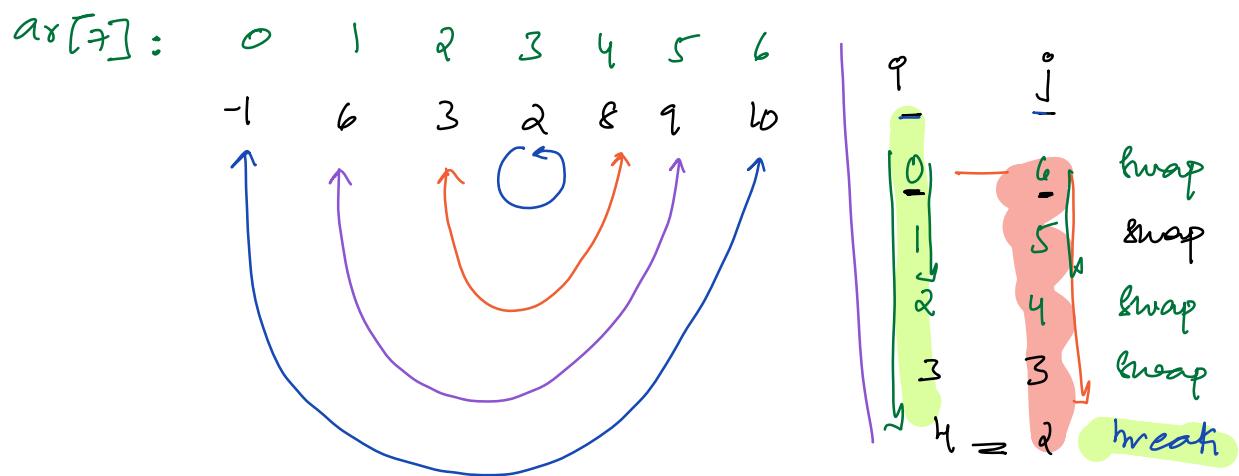
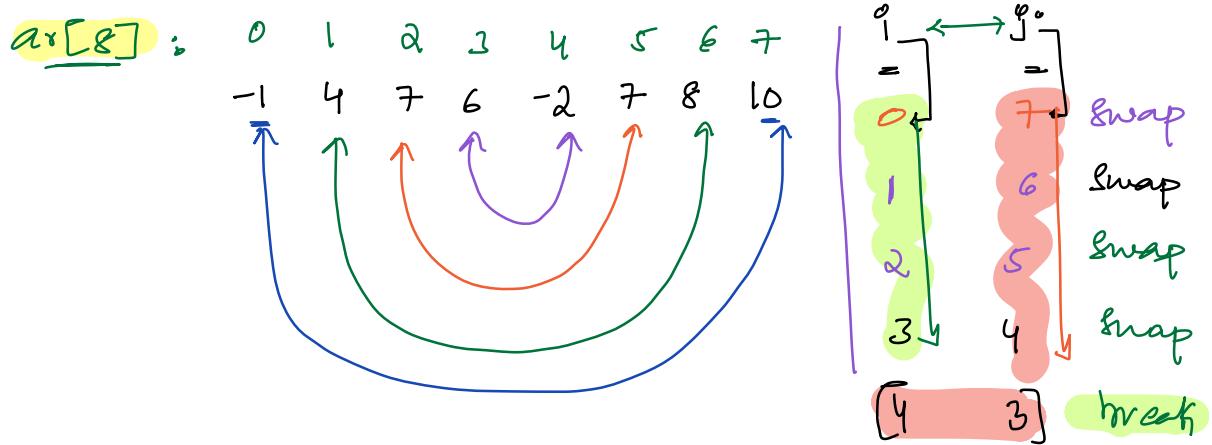
<u>i</u>	<u>$j [P_i, N-1]$</u>
0	$[1, N-1]$
1	$[2, N-1]$
2	$[3, N-1]$
\vdots	
$N-2$	$[N-1, N-1]$

// Sum of $N-1$ Natural Number

Replace N with $N-1$

$$\frac{(N-1)(N)}{2} \Rightarrow \frac{N^2-N}{2} : O(N^2)$$

Q8) Given an array, Reverse entire array $[] \rightarrow$ No Extra Space



```
void reverse(Pnt ar[], int N) {
```

$i=0, j=N-1 \rightarrow i < N/2$ Iterations: $N/2$
while ($i < j$) {
 Swap $ar[i]$ & $ar[j]$
 $i++$, $j--$

TC: $\Theta(N)$

on your own un
tag variable a Not

SC: $\Theta(1)$

Swap a & b

$temp = a$

$a = b$

$b = temp$

a	b	$temp$
20	10	a

// Subarray : Continuous sequence of an array is called Subarray

$[s^i \dots e^j]$: All elements from s^i to e^j is Subarray

- Doubts :
- 1) YES, Full array is Subarray
 - 2) YES, Single Element is Subarray
 - 3) No, Subarray cannot be empty

$ar[8]$:

0	1	<u>2</u>	3	4	5	6	7	8
-3	4	5	-6	8	9	10	-10	8

$[1 \dots 5]$: YES

$[5 \dots 5]$: Is Subarray YES

$[3 \dots 6 \dots 7 \dots 8]$: NO

$[0 \dots 8]$: YES

5 is missing

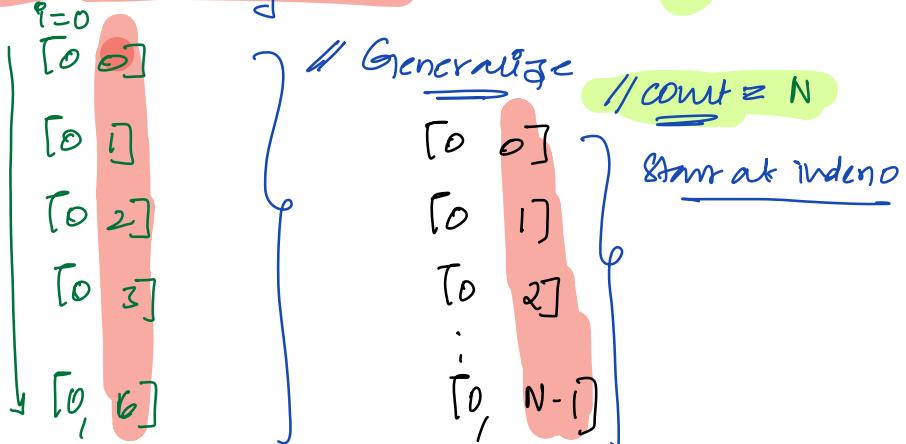
$[2 \dots 6]$: $\{5, -6, 8, 9, 10\}$

$[0 \dots 3]$: YES

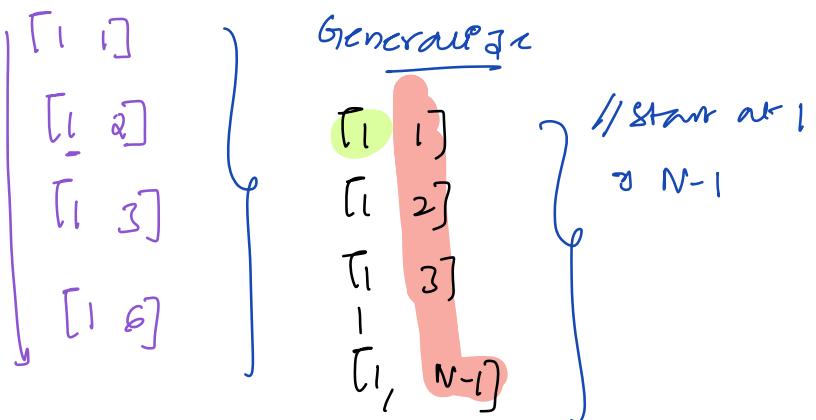
$s^i \dots e^j$

1 2 3 4 5 6 7 8 9 10

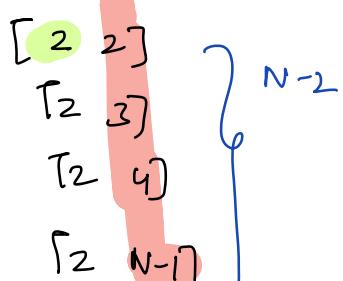
// Can subarray start at index = 0



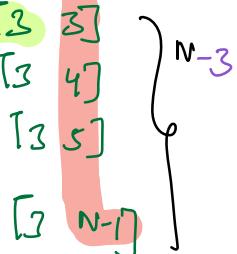
// Can subarrays start at index 1



// Generalized Start = 2



start = 3



$$\text{Start} = N-1$$

$$[N-1, N-1] : ①$$

Total Subarrays

$$N + N-1 + N-2 + \dots + 1$$

$$= \frac{N(N+1)}{2}$$

// Generate all Subarrays

// Generating all Subarrays

```
i = 0; i < N; i++) { // start of subarray  
    j = i; j < N; j++) { // end of subarray  
        // subarray [i - j]  
        k = i; k <= j; k++) { print(ar[k])  
    }  
    print("\n")
```

TC: $O(N^3)$

SC: $O(1)$

//
ar[4]: 0 1 2 3
 -3 4 5 -6

[0 0] : {-3}

[0 1] : {-3, 4}

[0 2] : {-3, 4, 5}

[0 3] : {-3, 4, 5, -6}

[1 1] : {4, 3}

[1 2] : {4, 5, 3}

[1 3] : {4, 5, -6}

[2 2] : {5, -6}

[2 3] : {5, -6}

[3 3] : {5, -6}

//
 $\alpha[\ell] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 3 & 4 & -1 & 8 & 6 & 8 & -2 & 10 \end{matrix} \Rightarrow$

// $\text{len}=1$ $\text{len}=2$ $\text{len}=3$ // Generalize: N

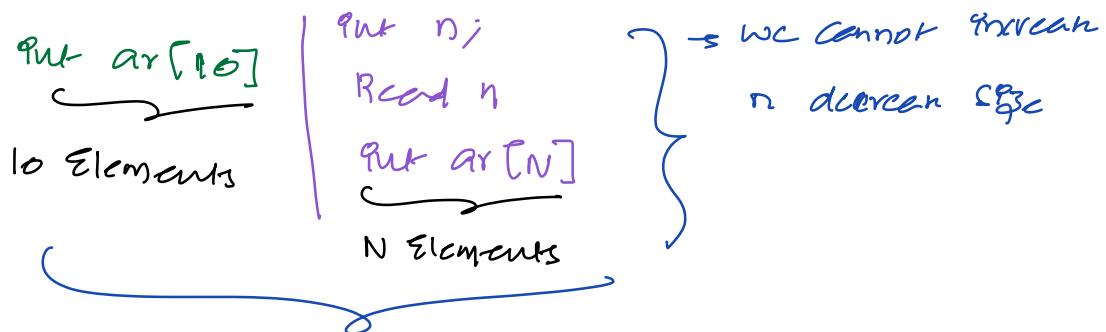
$[0, 0]$	$[0, 1]$	$[0, 2]$	<u>count $\text{len}=1$</u> : N
$[1, 1]$	$[1, 2]$	$[1, 3]$	<u>count $\text{len}=2$</u> : $N-1$
$[2, 2]$	$[2, 3]$	$[2, 4]$	
\vdots	\vdots	\vdots	
$[7, 7]$	$[6, 7]$	$[5, 7]$	

// Generalize $\text{len}=3$ // General $\text{len}=4$ # Generalize $\text{len}=k$

$[0, 2]$ $[1, 3]$ $[2, 4]$ $[3, 5]$ \downarrow $[N-3, N-1]$:	$[0, 3]$ $[k-1]$ $[1, 4]$ $[2, 5]$ \downarrow $[N-4, N-1]$	$\times [0, k]$ $\rightarrow k+1$ Elements $[0, k-1]$ $[k-1, N-1]$ $[1, k]$ \downarrow $[2, k+1]$ $[N-1 - (k-1)] + 1$ \downarrow $(N-k)$ $N-1$ # count = $[N-k+1]$
--	--	--

[# count $\geq N-2$] # count $\geq N-3$ # count = $[N-k+1]$

// Disadvantages of arrays



Dynamic Arrays :-

↳ size not fixed

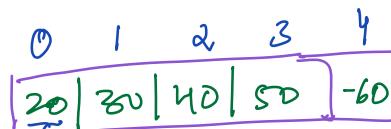
C++	Java	Python	C#	JavaScript	C
<code>vector</code>	<code>ArrayList</code>	<code>list</code>	<code>ArrayList</code>	<code>Array</code>	-

list → Dynamic Array

$\text{list} < \text{list} > a : \rightarrow a.size() == 0$

Dynamic list array

{
 $a.insert(20)$
 $a.insert(20)$
 $a.insert(40)$
 $a.insert(50)$



→ insert(): This will add an element at back.
→ a single insert = $O(1)$

$a.size() == 4$

→ size() → $O(1)$

$a.insert(-60)$ → delete(): Delete element from back.
→ $O(1)$

```

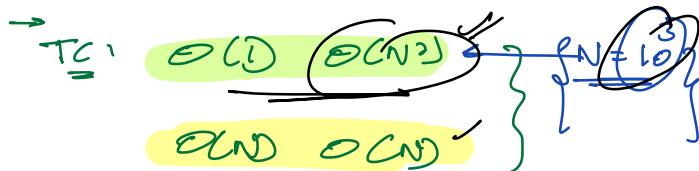
—— func (arr[], N) {
    lptr <int> clc;
    p=0; q< N, p++ {
        ↓      clc.insert(arr[q])
    }
}

// Given an lptr point
—— point(lptr<int> clc) {
    put N = clc.size();
    p=0; q< N, p++ {
        ↓      point(clc[i])
    }
}

```

// Doubts:

$ar[] \Rightarrow \{ -3, 8, 4, 7, 4, 8, 9, 10 \} \xrightarrow{\quad} N=10$



//

// Doubts:

$$\begin{aligned} & [a \ b] \Rightarrow b - a_{\text{el}} \\ & \xrightarrow{\quad} (N) \frac{(N+1)}{2} \\ & \xrightarrow{\quad} \log N \end{aligned}$$

: flatten