

# Comprehensive Assignment

## Digital fundamental concept & Number Sys

S1) An

→ Example of Analog:

old radio, land line.

→ Example of Both digital & Analog System:

- Digital Camera.

Digital camera like image sensor of a digital camera is analog. On board analog to digital converted convert image analog to digital.

→ Name of ~~entire~~ digital Systems

- Accumulator.

S2) S1)

~~Pulse~~

$$\text{Pulse width} = 35 \mu\text{s} \Rightarrow 35 \times 10^{-6} \text{ s}$$

$$\text{Time period} = 210 \mu\text{s} \Rightarrow 210 \times 10^{-6} \text{ s}$$

$$F = \frac{1}{T} \Rightarrow \frac{1}{210 \times 10^{-6}} \Rightarrow 4761 \text{ MHz}$$

$$D.C = \frac{35 \times 10^{-6}}{210 \times 10^{-6}} \times 100\% \Rightarrow 16.67\% \quad \text{Ans}$$

Q3)

- =
- Rise Time.
  - Fall Time.
  - Pulse width
  - Amplitude.

Rise Time:

$$\text{Rise time} = 3 - 1 = 2 \text{ ms}$$

Fall Time:

$$\Rightarrow 15.5 \text{ ms} \rightarrow 13.2 \text{ ms}$$

$$\Rightarrow 2.3 \text{ ms}$$

PULSE WIDTH:

$$\Rightarrow 14.4 - 2.2$$

$$\Rightarrow 12.2 \text{ ms}$$

Amplitude:

$$\Rightarrow 5 \text{ V}$$

Q4) List the octal and hexadecimal numbers from 8 to 64:

Octal	Hexadecimal	Octal	Hexadecimal
10	8	35	1D
11	9	36	1E
12	A	37	1F
13	B	40	20
14	C	41	21
15	D	42	22
16	E	43	23
17	F	44	24
20	10	45	25
21	11	46	26
22	12	47	27
23	13	50	28
24	14	51	29
25	15	52	2A
26	16	53	2B
27	17	54	2C
30	18	55	2D
31	19	56	2E
32	1A	57	2F
33	1B	60	30
34	1C	61	31

Octal	Hexadecimal
62	32
63	33
64	34
65	35
66	36
67	37
70	38
71	39
72	3A
73	3B
74	3C

Using A and B for the last two digits  
list numbers 4 to 32 in base 12.

$$\begin{aligned} \text{Base } 12: & 4, 5, 6, 7, 8, 9, A, B, 10, 11, 12, 13 \\ \Rightarrow & 14, 15, 16, 17, 18, 19, 1A, 1B, 20, 21 \\ \Rightarrow & 22, 23, \cancel{24} \end{aligned}$$

- Qs) A) 32 K bytes  $\Rightarrow 32 \times 2^{10} = 32768$  bytes
- =
- B) 64 M bytes  $\Rightarrow 64 \times 2^{20} = 67108864$  bytes
- C) 6.4 G bytes  $\Rightarrow 6.4 \times 2^{30} = 6871947674$  bytes

Q6) Convert the following

a)  $(4230)_5 \Rightarrow 4 \times 5^3 + 2 \times 5^2 + 3 \times 5^1 + 0 \times 5^0$   
 $\Rightarrow 500 + 50 + 15 + 0$   
 $\Rightarrow \boxed{565}_{10}$

b)  $(1A8)_{12} \Rightarrow 1 \times 12^2 + A \times 12^1 + 8 \times 12^0$   
 $\Rightarrow 144 + 120 + 8$   
 $\Rightarrow \boxed{272}_{10}$

c)  $(735)_8 \Rightarrow 7 \times 8^2 + 3 \times 8^1 + 5 \times 8^0$   
 $\Rightarrow 448 + 24 + 5$   
 $\Rightarrow \boxed{477}_{10}$

d)  $(452)_6 \Rightarrow 4 \times 6^2 + 5 \times 6^1 + 2 \times 6^0$   
 $\Rightarrow 144 + 30 + 2$   
 $\Rightarrow \boxed{176}_{10}$

Q7) Ans)

largest number of 16 bits

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{array} = \boxed{(65535)_{10}}$$
$$\Rightarrow (FFFF)_{16}$$

Q8) A13)

- a) base 6
- b) base 8
- c) base 11

Q9) Solutions of Quadratic equations

Sol

$$x^2 - 11x + 22 = 0, \quad n=3, \quad x=6$$

$$(x-3)(x-6)=0$$

$$x^2 - 9x + 18 = 0$$

Working in base 8

Q10) Convert:

Hexa to binary:

7    3    D    C<sub>16</sub>

0111 0011 1101 1100<sub>2</sub>, ↗

Binary to Octal:

0111 0011 1101 1100<sub>2</sub>     $\Rightarrow [71734]_8$

7 1 7 8 3 4<sub>8</sub>

## S21) Conversions

decimal to binary:

523<sub>10</sub>

$$\frac{523}{2} \Rightarrow 261.5 \rightarrow 0.5 \times 2 = 1$$

$$\frac{261}{2} \Rightarrow 130.5 \rightarrow 0.5 \times 2 = 1$$

$$\frac{130}{2} \Rightarrow 65 \rightarrow 0 \times 2 = 0$$

$$\frac{65}{2} \Rightarrow 32.5 \rightarrow 0.5 \times 2 = 1$$

$$\frac{32}{2} \Rightarrow 16 \rightarrow 0 \times 2 = 0$$

$$\frac{16}{2} \Rightarrow 8 \rightarrow 0 \times 2 = 0$$

$$\frac{8}{2} \Rightarrow 4 \rightarrow 0 \times 2 = 0$$

$$\frac{4}{2} \Rightarrow 2 \rightarrow 0 \times 2 = 0$$

$$\frac{2}{2} \Rightarrow 1 \rightarrow 0 \times 2 = 0$$

$$\frac{1}{2} \Rightarrow 0.5 \rightarrow 0.5 \times 2 = 1 \Rightarrow 1000001011$$

~~523~~<sup>10</sup>  
Convert decimal to Hexa and then Binary

$$\frac{523}{16} \Rightarrow 32.6875 \rightarrow 0.6875 \times 16 = B$$

$$\frac{32}{16} \Rightarrow 2.0 \rightarrow 0 \times 16 = 0$$

$$\frac{2}{16} = 0.125 \rightarrow 0.125 \times 16 = 2$$

~~208~~  
~~258~~  
A  
B

20B<sub>16</sub>  
/ /  
0010 00001011<sub>2</sub>

Method B is faster

$$8_{(2)} \stackrel{S_0}{=} 1) (10110.0101)_2$$

$$\begin{aligned}
 &= 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} \\
 &= 16 + 0 + 4 + 2 + 0 + 0 + 0.25 + 0 + 0.0625 \\
 &\Rightarrow (22.3125)_{10}
 \end{aligned}$$

$$2) (16.5)_{16} \stackrel{S_0}{=}$$

$$\begin{aligned}
 &= 1 \times 16^2 + 6 \times 16^0 + 0.5 \times 16^{-1} \\
 &= 16 + 6 + 0.03125 \\
 &\Rightarrow (22.03125)_{10}
 \end{aligned}$$

$$\begin{aligned}
 3) (26.24)_8 \stackrel{S_0}{=} & 2 \times 8^1 + 6 \times 8^0 + 2 \times 8^{-1} + 4 \times 8^{-2} \\
 &= 16 + 6 + 0.25 + 0.0625 \\
 &\Rightarrow (22.3125)_{10}
 \end{aligned}$$

$$\begin{aligned}
 4) (DADAB.B)_{16} \stackrel{S_0}{=} & D \times 16^3 + A \times 16^2 + D \times 16^1 + A \times 16^0 + B \times 16^{-1} \\
 &= 57344 + 2560 + 224 + 10 + 0.6875 \\
 &\Rightarrow (60138.6875)_{10}
 \end{aligned}$$

$$\begin{aligned}
 5) (1010.1102)_2 \stackrel{S_0}{=} & 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} \\
 &= 8 + 0 + 2 + 0 + 0.5 + 0.25 + 0 + 0.0625 \\
 &\Rightarrow (10.8125)_{10}
 \end{aligned}$$

# Boolean Algebra & Logic Gate

Q13 Simplify:

$$(a) ABC + \bar{A}B + AB\bar{C}$$

$$\stackrel{\text{SOL}}{=} ABC + AB\bar{C} + \bar{A}B$$

$$= AB(C + \bar{C}) + \bar{A}B \quad \therefore (A + \bar{A} = 1)$$

$$= AB + \bar{A}B$$

$$= B(A + \bar{A}) \quad \therefore A + \bar{A} = 1$$

$$\Rightarrow B$$

$$b) \bar{X}YZ + XZ$$

$$\stackrel{\text{SOL}}{=}$$

$$= Z(\bar{X}Y + X)$$

$$\therefore A + \bar{A}B = A + B$$

$$= Z(Y + X)$$

$$\therefore DL$$

$$= 2x + 2y$$

$$c) (\bar{X} + Y)(\bar{X} + \bar{Y})$$

$$\stackrel{\text{SOL}}{=}$$

$$\therefore \overline{A + B} = \bar{A}\bar{B}$$

$$= (\bar{X}\bar{Y})(\bar{X} + \bar{Y})$$

$$\therefore \bar{A} + \bar{A} = \bar{A}$$

$$= \bar{X}\bar{Y}\bar{X} + \bar{X}\bar{Y}\bar{Y}$$

$$\therefore \bar{A} + \bar{A} = \bar{A}$$

$$= \bar{X}\bar{Y} + \bar{X}\bar{Y}$$

$$= \bar{X}\bar{Y}$$

$$d) xy + x(wz + w\bar{z})$$

Sol

$$\Rightarrow xy + x[w(z + \bar{z})]$$

$$\therefore A + \bar{A} = 1$$

$$\Rightarrow xy + xw(w)$$

$$\Rightarrow wy + xw$$

$$\Rightarrow w(y + w)$$

$$e) (B\bar{C} + \cancel{\bar{A}D})(A\bar{B} + C\bar{D})$$

Sol

$$\therefore DL$$

$$B\bar{C}A\bar{B} + B\bar{C}C\bar{D} + \bar{A}D A\bar{B} + \bar{A}D C\bar{D}$$

$$AC(B\cdot \bar{B}) + BD(\bar{C}\cdot C) + BD(A\cdot A) + \bar{A}C(D\cdot \bar{D})$$

$$\therefore A \cdot \bar{A} = 0$$

$$A(\bar{A} + \bar{C})(A + \bar{B} + \bar{C})$$

Sol

$$\bar{A} \cdot A + \bar{A}\bar{B} + \bar{A}\bar{C} + A\bar{C} + \bar{B}\bar{C} + \bar{C} \cdot \bar{C}$$

$$\therefore A \cdot \bar{A} = 0$$

$$\bar{A} \cdot \bar{A} = \bar{A}$$

$$\bar{A}\bar{B} + \bar{A}\bar{C} + A\bar{C} + \bar{B}\bar{C} + \bar{C}$$

$$\bar{A}\bar{B} + \bar{C}(\bar{A} + A) + \bar{B}\bar{C} + \bar{C}$$

$$\therefore A + \bar{A} = 1$$

$$\bar{A}\bar{B} + \bar{C} + \bar{C} + \bar{B}\bar{C}$$

$$\bar{A} + \bar{A} = \bar{A}$$

$$\bar{A}\bar{B} + \bar{C} + \bar{B}\bar{C}$$

$$\therefore \cancel{\bar{A} + \bar{B} + \bar{C}} = \bar{A} + \bar{B}$$

$$\underline{S_{14})} \quad A\bar{C} + ABC + A\bar{C}$$

$$\cancel{\bar{C}(A+A)} + ABC$$

$$\therefore \bar{A} + A = 0$$

$$\bar{C} + ABC$$

$$\therefore A + I = I$$

$$\bar{C} + AB$$

$$b) (\bar{n}\bar{y} + z) + z + xy + wz$$

Sol

$$\therefore A + B = \bar{A}\bar{B}$$

$$(\bar{n}\bar{y} \cdot \bar{z}) + z + xy + wz \quad \therefore \bar{AB} = \bar{A} + \bar{B}$$

$$(\bar{n} + \bar{y} \cdot \bar{z}) + z + ny + wz \quad \therefore \bar{A} = A$$

$$(n+y) \cdot \bar{z} + z + ny + wz$$

$$\bar{z}ny\bar{z} + z + ny + wz \quad \therefore A + \bar{A}B = A + B$$

$$ny\bar{z} + z + y + ny + wz$$

$$z + ny + y + ny + wz$$

$$\therefore A + AB = A$$

$$ny + z + wz$$

$$ny + z$$

$$c) \overline{AB}(\overline{D} + \overline{CD}) + B(A + \overline{AC}D)$$

Sol

$$= A + \overline{AB} \Leftrightarrow A + R$$

$$\overline{AB}(\overline{D} + \overline{C}) + B(A + \overline{CD})$$

$$\overline{AB}\overline{D} + \overline{AB}\overline{C} + BA + BC\overline{D}$$

$$B(\overline{AD} + A) + \overline{ABC} + BCD \quad \therefore A + \overline{AB} = A + R$$

$$B(A + \overline{D}) + \overline{ABC} + BCD$$

$$AB + \cancel{BD} \overline{BD} + \overline{ABC} + BCD$$

$$\cancel{AB} + B(\overline{D} + \overline{CD}) + \overline{ABC}$$

$$\cancel{AB} + B(A + \overline{AC}) + B(\overline{D} + \overline{B})$$

$$B(A + \overline{C}) + B(\overline{D} + C)$$

$$AB + B\overline{C} + B\overline{D} + BC$$

$$AB + \cancel{BD} + B(\overline{C} + C)$$

$$\therefore A + \overline{A} = 1$$

$$AB + BD + B$$

$$\therefore A + AB = A$$

$$\begin{array}{c} B + BD \\ \hline (B) \end{array}$$

$$d) (\overline{A} + C)(\overline{A} + \overline{C})(A + B + \overline{CD})$$

Sol

$\because DL$

$$\therefore \overline{A} \cdot \overline{A} = \overline{A}$$

$$(\overline{A}\overline{A} + \overline{A}\overline{C} + \overline{A}C + C \cdot \overline{C})(A + B + \overline{CD}) \quad \therefore A \cdot \overline{A} = 0$$

$$(\overline{A} + \overline{A}\overline{C} + \overline{A}C + C)(A + B + \overline{CD})$$

$$[\overline{A} + \overline{A}(\overline{C}, C)](A + B + \overline{CD})$$

$$\overline{A}(A + B + \overline{CD})$$

$$\overline{A} \cdot A + \overline{AB} + \overline{ACD}$$

$$\overline{AB} + \overline{ACD}$$

$$\overline{A}(B + \overline{CD})$$

$$e) AB\bar{C}D + \bar{A}B\bar{D} + A\bar{B}CD$$

(6)

$$\Rightarrow ABD(\bar{C}+C) + \bar{A}BD$$

$\because A+\bar{A}=1$

$$\Rightarrow ABD + \bar{A}BD$$

$\therefore A+\bar{A}=1$

$$\Rightarrow BD(A+\bar{A})$$

$$\Rightarrow BD$$

Q15)  $F = AB + CD$  : find complement

$$\bar{F} = \overline{AB + CD}$$

$$\bar{F} = (\bar{A}\bar{B})(\bar{C}\bar{D})$$

$$\bar{A} + \bar{B} = \bar{A}\bar{B}$$

$$\bar{A}\bar{B} = \bar{A} + \bar{B}$$

$$\bar{F} = (\bar{A} + \bar{B})(\bar{C} + \bar{D})$$

$$\cancel{\bar{A}\bar{C}} + \cancel{\bar{A}\bar{D}} + \cancel{\bar{B}\bar{C}} + \cancel{\bar{B}\bar{D}}$$

$$F \cdot \bar{F} = (AB + CD)(\bar{A} + \bar{B})(\bar{C} + \bar{D})$$

$$= (AB + CD)(\bar{A}\bar{C} + \bar{A}\bar{D} + \bar{B}\bar{C} + \bar{B}\bar{D})$$

$$= AB\bar{A}\bar{C} + AB\bar{A}\bar{D} + AB\bar{B}\bar{C} + AB\bar{B}\bar{D}$$

$$+ CD\bar{A}\bar{C} + CD\bar{A}\bar{D} + CD\bar{B}\bar{C} + CD\bar{B}\bar{D}$$

$$= BC(A \cdot \bar{A}) + BD(A \cdot \bar{A}) + AC(B \cdot \bar{B}) + AD(B \cdot \bar{B})$$

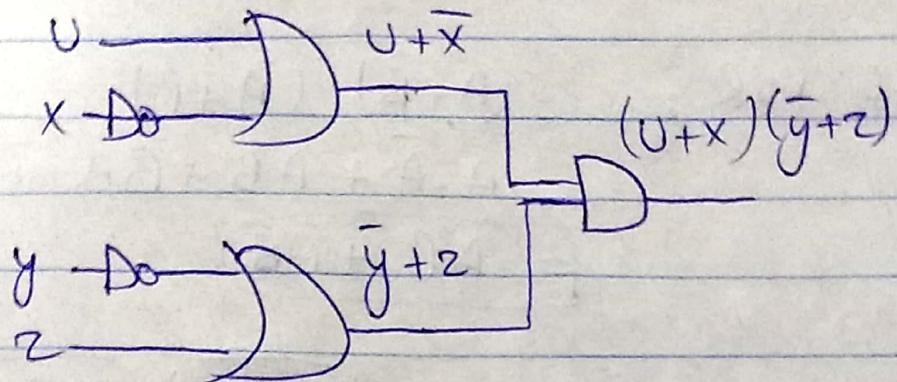
$$+ \bar{A}D(C \cdot \bar{C}) + \bar{A}D(D \cdot \bar{D}) + \bar{B}D(C \cdot \bar{C}) + \bar{B}C(D \cdot \bar{D})$$

$$\therefore A\bar{A} = 0$$

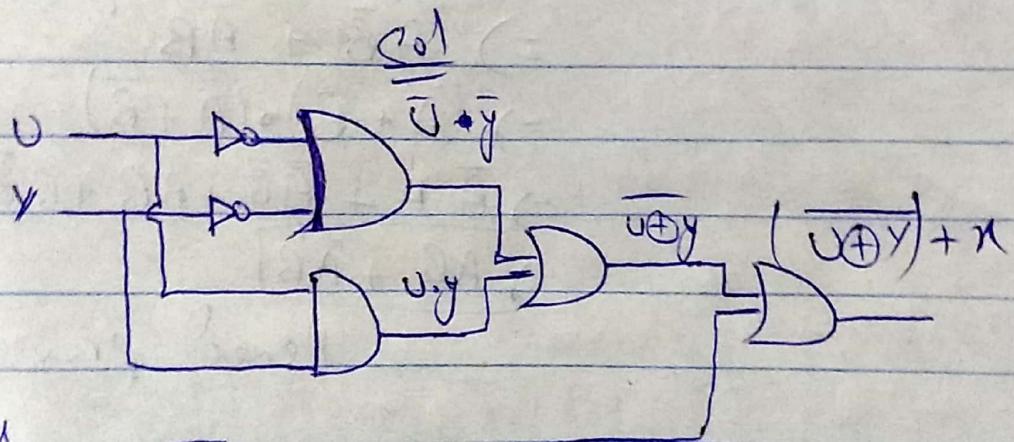
$$\Rightarrow 0$$

Q16) Diagram

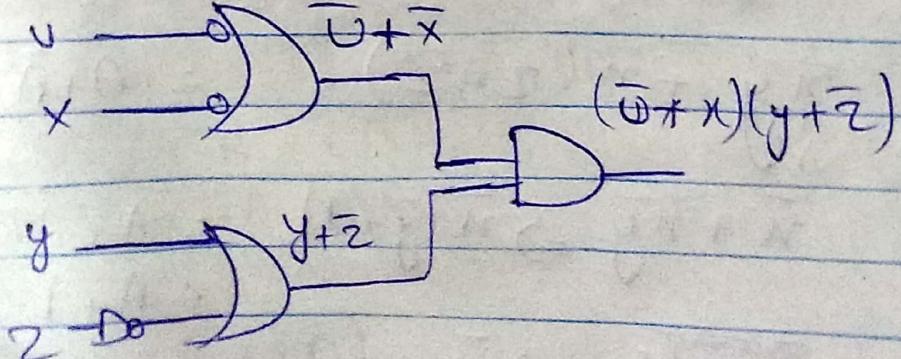
a)  $A = \overline{[(U + \bar{X})(\bar{Y} + Z)]}$



b)  $B = \overline{(U \oplus X)} + X$



c)  $C = (\overline{U + X})(Y + \bar{Z})$



Q17 Sol

$$\text{XOR: } \cancel{x \oplus y} = \cancel{xy^*} + \cancel{\bar{x}y}$$

$$\text{XOR: } A \oplus B = A\bar{B} + \bar{A}B$$

$$\begin{aligned}\text{Dual of XOR: } &= (A + \bar{B})(\bar{A} + B) \\ &= A \cdot \bar{A} + AB + \bar{B}\bar{A} + \bar{B}B \\ &\boxed{= AB + \bar{A}\bar{B}}\end{aligned}$$

$$\begin{aligned}\text{Complement of XOR: } &\Rightarrow (\cancel{A \oplus y}) \quad \cancel{A \oplus B} \\ &\Rightarrow \cancel{AB + \bar{A}\bar{B}} \\ &\Rightarrow \bar{A}\bar{B} + \bar{A}B \\ &\Rightarrow (\bar{A} + B)(A + \bar{B}) \\ &\Rightarrow \cancel{\bar{A} \cdot A + \bar{A}\bar{B} + AB + B \cdot \bar{B}} \\ &\Rightarrow \boxed{AB + \bar{A}\bar{B}}\end{aligned}$$

Hence proved

Q18 Sol L.H.S

$$\bar{n}\bar{y} + \bar{n}z + \bar{n}\bar{z}$$

$$\bar{n}\bar{y} + \bar{n}(z + \bar{z}) \quad : A + \bar{A} = 1$$

$$\bar{n} + \bar{n}\bar{y} \Rightarrow \bar{n}(\bar{y} + 1) \quad : \bar{A} + \bar{A}\bar{B} = \bar{A} + \bar{B}$$

$$\therefore A + 1 = 1$$

$$\cancel{x \oplus y} \Rightarrow \bar{n}$$

R.H.S

$$\bar{x}\bar{z} + \bar{y}\bar{z} + \bar{x}z$$

$$\bar{x}(\bar{z}+z) + \bar{y}\bar{z}$$

$$\bar{x} + \bar{y}\bar{z}$$

Truth Table:

x	y	z	$\bar{x}$	<del><math>\bar{y}</math></del>	$\bar{z}$	$\bar{x} + \bar{y}\bar{z}$
0	0	0	1	1	1	1
0	0	1	1	1	0	1
0	1	0	1	0	1	1
0	1	1	1	0	0	1
1	0	0	0	1	1	1
1	0	1	0	1	0	0
1	1	0	0	0	1	0
1	1	1	0	0	0	0

Not Equal

$$\underline{\underline{Q_{20}}}) (B+D)(\bar{A}+\bar{B}+C)$$

Sol

$$\bar{A}B + \bar{B}\bar{B} + BC + \bar{A}D + \bar{B}D + CD \quad \because A\bar{A}=0$$

$$\bar{A}B + BC + \bar{A}D + \bar{B}D + CD \quad AD$$

$$\underline{\underline{Q_{21}}}) \bar{A}B + \bar{A}\bar{C} + ABC$$

Sol

$$\bar{A}B(C+\bar{C}) + \bar{A}(B+\bar{B})\bar{C} + ABC$$

$$\bar{A}BC + \bar{A}B\bar{C} + \bar{A}BC + \bar{A}\bar{B}C + ABC$$

$$\therefore A+A=A$$

$$ABC + \bar{A}B\bar{C} + \bar{A}\bar{B}C + ABC$$

0 1 1    0 1 0    0 0 1    1 1 1

A	B	C	X	Sum Term
0	0	0	0	$A+B+C$
0	0	1	1	
0	1	0	1	
0	1	1	1	
1	0	0	0	$\bar{A}+B+C$
1	0	1	0	$\bar{A}+B+\bar{C}$
1	1	0	0	$\bar{A}+\bar{B}+C$
1	1	1	1	

$$(A+B+C)(\bar{A}+B+C)(\bar{A}+B+\bar{C})(\bar{A}+\bar{B}+C)$$

$$Q_{22} \text{ a) } f(x,y,z) = \Sigma(0,2,4,5,6)$$

Sof

$xz$	$\bar{z}$	$z$
$\bar{x}\bar{y}$	1	
$\bar{x}y$	1	
$xy$	1	
$x\bar{y}$	1	1

$$\Rightarrow \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + xy\bar{z} + x\bar{y}\bar{z} + x\bar{y}z$$

$xz$	$\bar{z}$	$\bar{z}$
$\bar{x}\bar{y}$	1	
$\bar{x}y$	1	
$xy$	1	
$x\bar{y}$	1	1

$$\Rightarrow \bar{z} + x\bar{y}$$

$$b) f(x,y,z) = \Sigma(3,4,6,7)$$

Sof

$xz$	$\bar{z}$	$z$
$\bar{x}\bar{y}$		
$\bar{x}y$		1
$xy$	1	1
$x\bar{y}$	1	

$xz$	$\bar{z}$	$z$
$\bar{x}\bar{y}$		
$\bar{x}y$		
$xy$	1	1
$x\bar{y}$	1	1

$$\Rightarrow \bar{x}yz + x\bar{y}\bar{z} + xy\bar{z} + x\bar{y}z \Rightarrow x\bar{z} + yz$$

$$c) f(A, B, C) = \Sigma(1, 2, 3, 5, 7)$$

$\sum$

$ABC$	$\bar{C}$	$C$
$\bar{A}\bar{B}$	1	
$\bar{A}B$	1	1
$A\bar{B}$		1
$AB$		

$ABC$	$\bar{C}$	$C$
$\bar{A}\bar{B}$	1	
$\bar{A}B$	1	1
$A\bar{B}$	?	1
$AB$		

$$\Rightarrow ABC + A\bar{B}C + \bar{A}BC + \bar{A}B\bar{C} + \bar{A}\bar{B}C \Rightarrow \bar{A}B + C$$

$$d) f(w, x, y, z) = \Sigma(0, 1, 2, 4, 5, 6, 8, 9, 12, 13, 14)$$

$\sum$

$wx$	$y^2$	$\bar{y}z$	$\bar{y}z$	$yz$	$\bar{y}\bar{z}$
$\bar{w}x$	1	1		1	
$\bar{w}x$	1	1		1	
$wx$	1	1		1	
$w\bar{x}$	1	1			

$wx$	$y^2$	$\bar{y}z$	$\bar{y}z$	$yz$	$\bar{y}\bar{z}$
$\bar{w}x$	1	1	1		1
$\bar{w}x$	1	1	1	1	1
$wx$	1	1	1	1	1
$w\bar{x}$	1	1		1	

$$\Rightarrow w\bar{z} + \bar{w}\bar{z} + \bar{y}$$

$$\Rightarrow \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}\bar{x}yz + wx\bar{y}\bar{z} + wx\bar{y}z + w\bar{x}\bar{y}\bar{z}.$$

$$e) F(A, B, C, D) = \{0, 2, 3, 5, 7, 8, 9, 10, 11, 13, 15\}$$

$\overline{AB}$	$CD$	$\overline{C}\overline{D}$	$\overline{C}D$	$C\overline{D}$	$CD$
$\overline{AB}$	1		1		1
$\overline{AB}$		1	1		
$\overline{AB}$		1	1		
$\overline{AB}$	1	1	1	1	



$$\Rightarrow \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}CD + \overline{A}\overline{B}C\overline{D} + \overline{A}\overline{B}\overline{C}D + \overline{A}\overline{B}C\overline{D}$$

$$+ AB\overline{C}D + AB CD + A\overline{B}\overline{C}\overline{D} + A\overline{B}\overline{C}D + A\overline{B}C\overline{D}$$

$$+ A\overline{B}C\overline{D}$$

$\overline{AB}$	$CD$	$\overline{C}\overline{D}$	$\overline{C}D$	$C\overline{D}$	$CD$
$\overline{AB}$	1			1	1
$\overline{AB}$		1		1	
$\overline{AB}$		1		1	
$\overline{AB}$	1	1	1	1	1

$$\Rightarrow \overline{AB} + \overline{B}\overline{D} + CD + BD$$

(Q23) a)  $f(A, B, C, D) = \{0, 1, 2, 5, 8, 9, 10\}$

$\overline{AB}$	$CD$	$\overline{C}\overline{D}$	$\overline{C}D$	$C\overline{D}$
$\overline{AB}$	0	0	0	0
$\overline{AB}$		0		
$\overline{AB}$				
$\overline{AB}$	0	0	0	0

$$\Rightarrow (A+B+C+D)(A+B+C+\overline{D})$$

$$(A+B+\overline{C}+D)(A+\overline{B}+C+\overline{D})$$

$$(\overline{A}+B+C+D)(\overline{A}+B+C+\overline{D})$$

$$(\overline{A}+B+\overline{C}+D)$$

b)  $f(n, y, z) = \Sigma (1, 3, 4, 6)$

$ny$	$z$	$\bar{z}$
$n$	0	0
$\bar{n}$	0	0
$y$	0	0
$\bar{y}$	0	0

$ny$	$z$	$\bar{z}$
$n+y$	0	0
$n+\bar{y}$	0	0
$\bar{n}+y$	0	0
$\bar{n}+\bar{y}$	0	0

$$\Rightarrow (n+z)(\bar{n}+z)$$

$$\Rightarrow (n+y+z)(n+\bar{y}+z)(\bar{n}+\bar{y}+z)(\bar{n}+y+z)$$

c)  $f(n, y, z) = \Sigma (1, 2, 3, 4, 5, 7)$

$ny$	$z$	$\bar{z}$
$n+y$	0	0
$n+\bar{y}$	0	0
$\bar{n}+y$	0	0
$\bar{n}+\bar{y}$	0	0

$ny$	$z$	$\bar{z}$
$n+y$	0	0
$n+\bar{y}$	0	0
$\bar{n}+y$	0	0
$\bar{n}+\bar{y}$	0	0

$$\Rightarrow (\bar{n}+y)(n+\bar{y})(\bar{z})$$

$$\Rightarrow (n+y+\bar{z})(n+\bar{y}+z)(n+\bar{y}+\bar{z})(\bar{n}+\bar{y}+z)(\bar{n}+y+\bar{z})$$

d)  $f(A, B, C, D) = \Sigma (3, 7, 11, 13, 14, 15)$

Sel

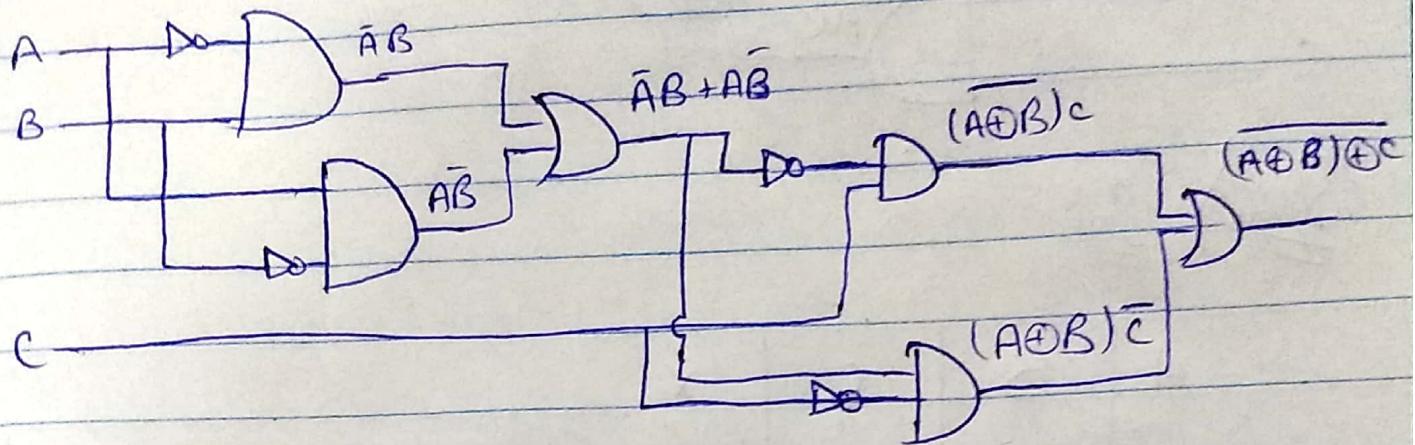
$A\bar{B}$	$C+D$	$C+\bar{D}$	$\bar{C}+\bar{D}$	$\bar{C}+D$
$A+B$			0	
$A+\bar{B}$			0	
$\bar{A}+\bar{B}$	0	0	0	
$\bar{A}+B$		0		

$$\Rightarrow (A+B+\bar{C}+\bar{D})(A+\bar{B}+\bar{C}+\bar{D})(\bar{A}+\bar{B}+C+\bar{D}) \\ (\bar{A}+\bar{B}+\bar{C}+\bar{D})(\bar{A}+\bar{B}+\bar{C}+D)(\bar{A}+B+\bar{C}+D)$$

$A\bar{B}$	$C+D$	$C+\bar{D}$	$\bar{C}+\bar{D}$	$\bar{C}+D$
$A+B$			0	
$A+\bar{B}$			0	
$\bar{A}+\bar{B}$	0	0	0	0
$\bar{A}+B$		0	0	

$$\Rightarrow (\bar{C}+\bar{D})(\bar{A}+\bar{B}+\bar{D})(\bar{A}+\bar{B}+\bar{C})$$

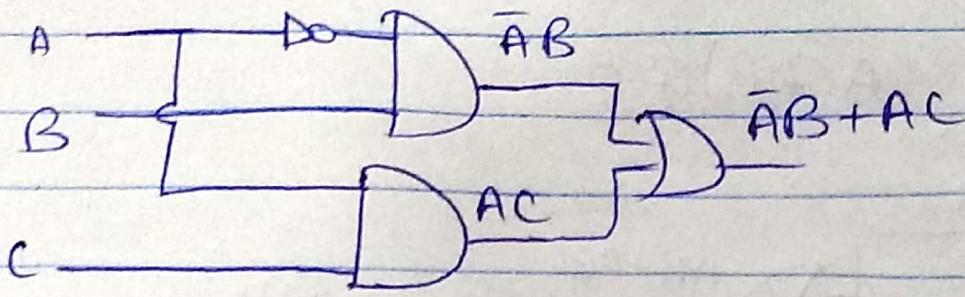
Q<sub>24</sub> Construct:  $(A \oplus B) \oplus C$



Q<sub>25</sub>) Truth Table:

A	B	C	X	Product Term	Sum Term
0	0	0	0		$A + B + C$
0	0	1	0		$A + B + \bar{C}$
0	1	0	1	$\bar{A} B \bar{C}$	
0	1	1	1	$\bar{A} B C$	
1	0	0	0		$\bar{A} + B + C$
1	0	1	1	<del><math>\bar{A} \bar{B} A \bar{B} C</math></del>	
1	1	0	0		$\bar{A} + \bar{B} + C$
1	1	1	1	$A B C$	

$$\begin{aligned}
 f &= \bar{A} B \bar{C} + \bar{A} B C + A \bar{B} \bar{C} + A B C \\
 &\Rightarrow \bar{A} B (\bar{C} + C) + A \bar{B} \bar{C} + A B C \quad \because \bar{A} + A = 1 \\
 &\Rightarrow \bar{A} B + A C (\bar{B} + B) \\
 &\Rightarrow \bar{A} B + A C
 \end{aligned}$$



Q26) Sol

A	B	C	X
---	---	---	---

0	0	0	0
---	---	---	---

0	0	1	0
---	---	---	---

0	1	0	0
---	---	---	---

0	1	1	1
---	---	---	---

1	0	0	0
---	---	---	---

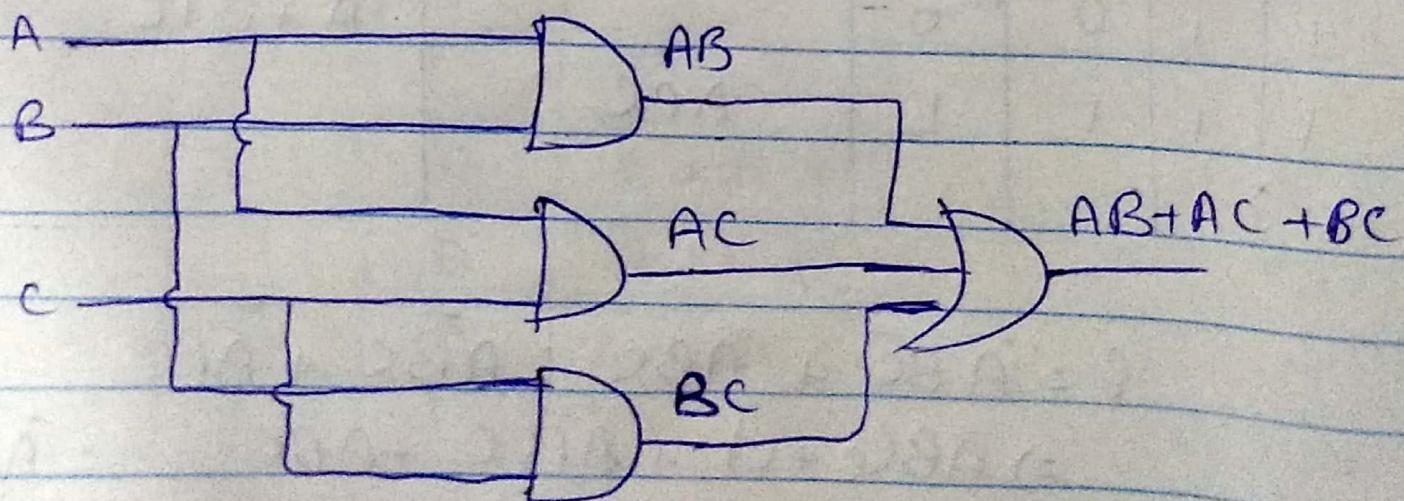
1	0	1	1
---	---	---	---

1	1	0	1
---	---	---	---

1	1	1	1
---	---	---	---

$\bar{A}B$	$C$	$\bar{c}$	$c$
$\bar{A}B$	0	0	
$\bar{A}B$	0	1	
$AB$	1	1	
$AB$	0	1	

$$F = AB + AC + BC$$



Q<sub>27</sub> Sol

A) 01  
Sol

$$\sum = 1, \cancel{C_{OUT}} = 0$$

B) 00

Sol

$$\sum = 0, C_{OUT} = 0$$

C) 10

Po

$$\sum = 1, C_{OUT} = 0$$

D) 11

Sol

$$\sum = 0, C_{OUT} = 1$$

Q<sub>28</sub> A(B)

$$\sum = 0, C_{OUT} = 1$$

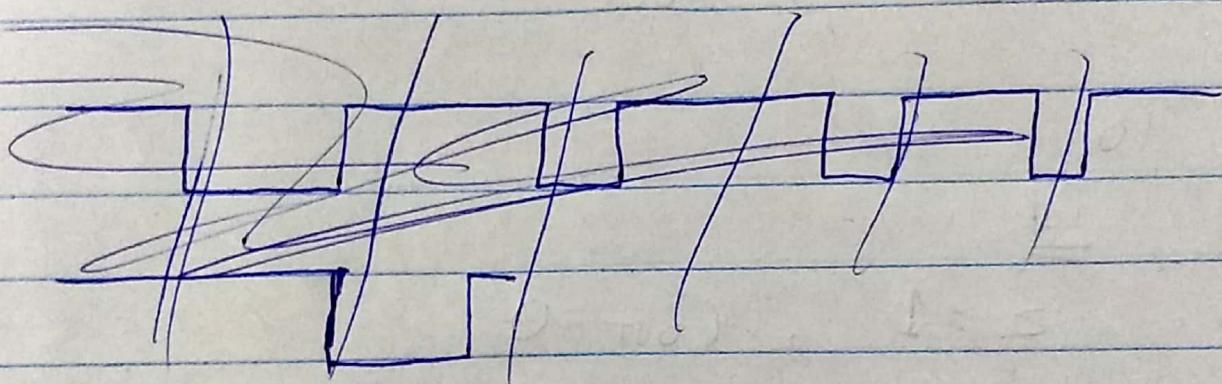
Q29 AB

$$\begin{array}{r} 1011 \\ 1111 \\ \hline \text{Count} < \underline{11011} \end{array}$$

$$E = 1011, \text{ Count} = 1$$

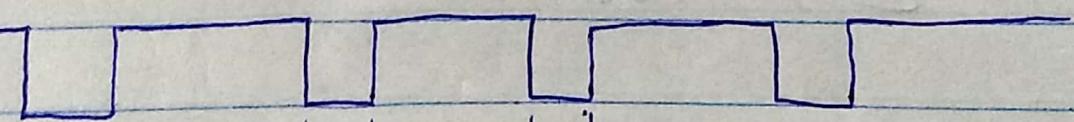
~~Q30 Sol~~

a)

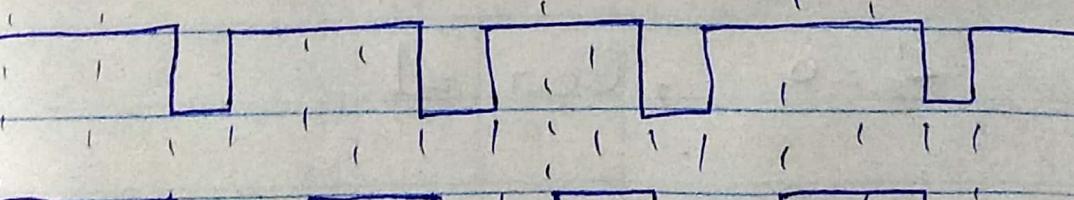


Q30 AB

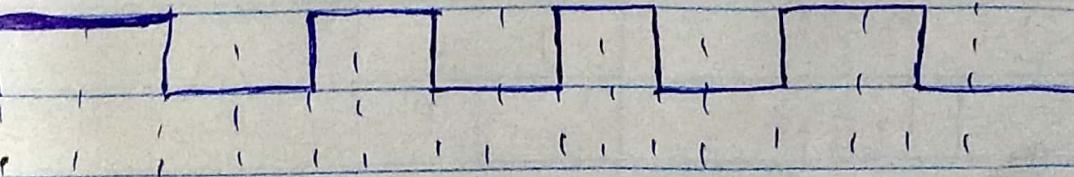
S



R̄



Q̄



$\delta_{30}$      $s_0$

