

August/September 2022
MCA II SEMESTER
Analysis Design of Algorithms (MCA-20-102)

Time: 3 Hours

Max. Marks:75

- Instructions:**
1. It is compulsory to answer all the questions (1.5 marks each) of Part -A in short.
 2. Answer any four questions from Part -B in detail.
 3. Different sub-parts of a question are to be attempted adjacent to each other.

PART -A

- Q1 (a) What do you mean by pseudocode? (1.5)
- (b) What are the types of algorithm efficiencies? (1.5)
- (c) What is the complexity of Quick sort? (1.5)
- (d) What is complexity of Binary Search? (1.5)
- (e) What do you mean by NP-Hard and NP-complete problems? (1.5)
- (f) Explain important properties of B-Tree. (1.5)
- (g) Specify the difference between divide and conquer strategy and dynamic programming. (1.5)
- (h) Distinguish Greedy method and Dynamic Programming. (1.5)
- (i) What is tree edge and cross edge? (1.5)
- (j) What is the complexity of Selection sort? (1.5)

PART -B

- Q2 (a) Write and explain merge sort algorithm using divide and conquer strategy. (10)
 Also analyze the complexity.
- (b) Consider a complete undirected graph with vertex set {0, 1, 2, 3, 4}. Entry W_{ij} in the matrix W below is the weight of the edge $\{i, j\}$. What is the minimum possible weight of a spanning tree T in this graph such that vertex 0 is a leaf node in the tree T ? (5)

$$W = \begin{pmatrix} 0 & 1 & 8 & 1 & 4 \\ 1 & 0 & 12 & 4 & 9 \\ 8 & 12 & 0 & 7 & 3 \\ 1 & 4 & 7 & 0 & 2 \\ 4 & 9 & 3 & 2 & 0 \end{pmatrix}$$

- Q3 (a) Write down Prim's algorithm and analyze the complexity. (5)
- (b) Write the algorithm for general iterative backtracking method and explain various factors that define the efficiency of backtracking. (10)

- Q4 Explain how 4 Queen problem can be solved using backtracking. Draw the state space tree corresponding to 4 Queen problem. (15)
- Q5 (a) Explain subset-sum problem and discuss the possible solution strategies using backtracking. (5)
- (b) Define Travelling Salesman Problem (TSP). Explain the basic steps that are to be followed to solve TSP using branch and bound. Illustrate with an example. (10)
- Q6 (a) State knapsack problem. Give an algorithm for knapsack problem using greedy strategy. (10)
- (b) Find an optimal solution to the knapsack problem for an instance with number of items 7, Capacity of the sack $W=15$, profit associated with the items $(p_1, p_2, \dots, p_7) = (10, 5, 15, 7, 6, 18, 3)$ and weight associated with each item $(w_1, w_2, \dots, w_7) = (2, 3, 5, 7, 1, 4, 1)$. (5)
- Q7 Describe the algorithm for Hamiltonian cycles and determine the order of magnitude of the worst-case computing time for the backtracking procedure that finds all Hamiltonian cycles. (15)
