

# SSN COLLEGE OF ENGINEERING RECORD SHEET

Sheet No. .... 1

Name : Aafreen . M

Dept : III year CSE - A

Reg. NO : 205001301

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## Logic Programming Assignment - II

1. Given the following statements.

Laxman is wherever Ram is .

Ram is at Ayodhya .

Where is Laxman?

generate answer using logic programming .

Laxman is wherever Ram is.

$$\forall x \text{ At}(\text{Ram}, x) \rightarrow \text{At}(\text{Laxman}, x)$$

$$\neg \text{At}(\text{Ram}, x) \vee \text{At}(\text{Laxman}, x)$$

$$\textcircled{1} \text{ clause : } \{ \neg \text{At}(\text{Ram}, x), \text{At}(\text{Laxman}, x) \}$$

Ram is at Ayodhya .

$$\text{At}(\text{Ram}, \text{Ayodhya})$$

$$\textcircled{2} \text{ clause : } \{ \text{At}(\text{Ram}, \text{Ayodhya}) \}$$

Goal clause : where is Laxman ?  $\Rightarrow \text{At}(\text{Laxman}, y)$   
(negation)

$$\textcircled{3} \text{ clause : } \{ \neg \text{At}(\text{Laxman}, y), \text{Answer}(y) \}$$

$$\textcircled{1} \{ \neg \text{At}(\text{Ram}, x), \text{At}(\text{Laxman}, x) \} \quad \textcircled{2} \{ \neg \text{At}(\text{Laxman}, y), \text{Answer}(y) \}$$

$$\{ \neg \text{At}(\text{Ram}, y), \text{Answer}(y) \}$$

$$\textcircled{2} \{ \text{At}(\text{Ram}, \text{Ayodhya}), \text{Answer}(y) \}$$

$$y | \text{Ayodhya}$$

$$\{ \text{Answer}(\text{Ayodhya}) \}$$

By Answer generation,  
we find that Laxman is at Ayodhya



2. i. female ancestor of george.

$\text{ancestor}(\text{George}, w) \wedge \text{female}(w)$

Negation:  $\neg \text{ancestor}(\text{George}, w) \vee \neg \text{female}(w)$ .

$\neg \text{ancestor}(\text{George}, w) \vee \neg \text{female}(w) \cdot \text{ancestor}(x, z) \vee$

$\neg \text{parent}(x, y) \vee \neg \text{ancestor}(y, z).$

$x / \text{George}$   
 $z / w$

$\neg \text{female}(w) \vee \neg \text{parent}(\text{George}, y)$

$\vee \neg \text{ancestor}(y, w).$

$\text{parent}(\text{George}, \text{andy}).$

$y / \text{andy}.$

$\neg \text{female}(w) \vee \neg \text{ancestor}(\text{andy}, w), \text{ancestor}(x, z) \vee \neg \text{parent}(x, y)$

$\vee \text{ancestor}(y, z)$

$x / \text{Andy}.$   
 $z / w$

$\neg \text{female}(w) \vee \neg \text{parent}(\text{Andy}, y)$

$\vee \neg \text{ancestor}(y, w).$

$\text{parent}(\text{andy}, \text{mary})$

$y / \text{mary}$

$\neg \text{female}(w) \vee \neg \text{ancestor}(y, w)$

$\text{female}(\text{mary}).$

$w / \text{mary}.$

$\neg \text{ancestor}(\text{mary}, \text{mary}).$

$\text{ancestor}(x, x).$

$x / \text{mary}.$

$\perp$

Answer:  $w = \text{Mary}.$

ii. male ancestor of george.

$\neg \text{ancestor}(\text{George}, @) \vee \text{male}(@) \quad \text{ancestor}(x, x)$

$x / \text{George}$   
 $@ / w$

$\neg \text{male}(\text{George})$

$\text{male}(\text{George}).$

$\square$

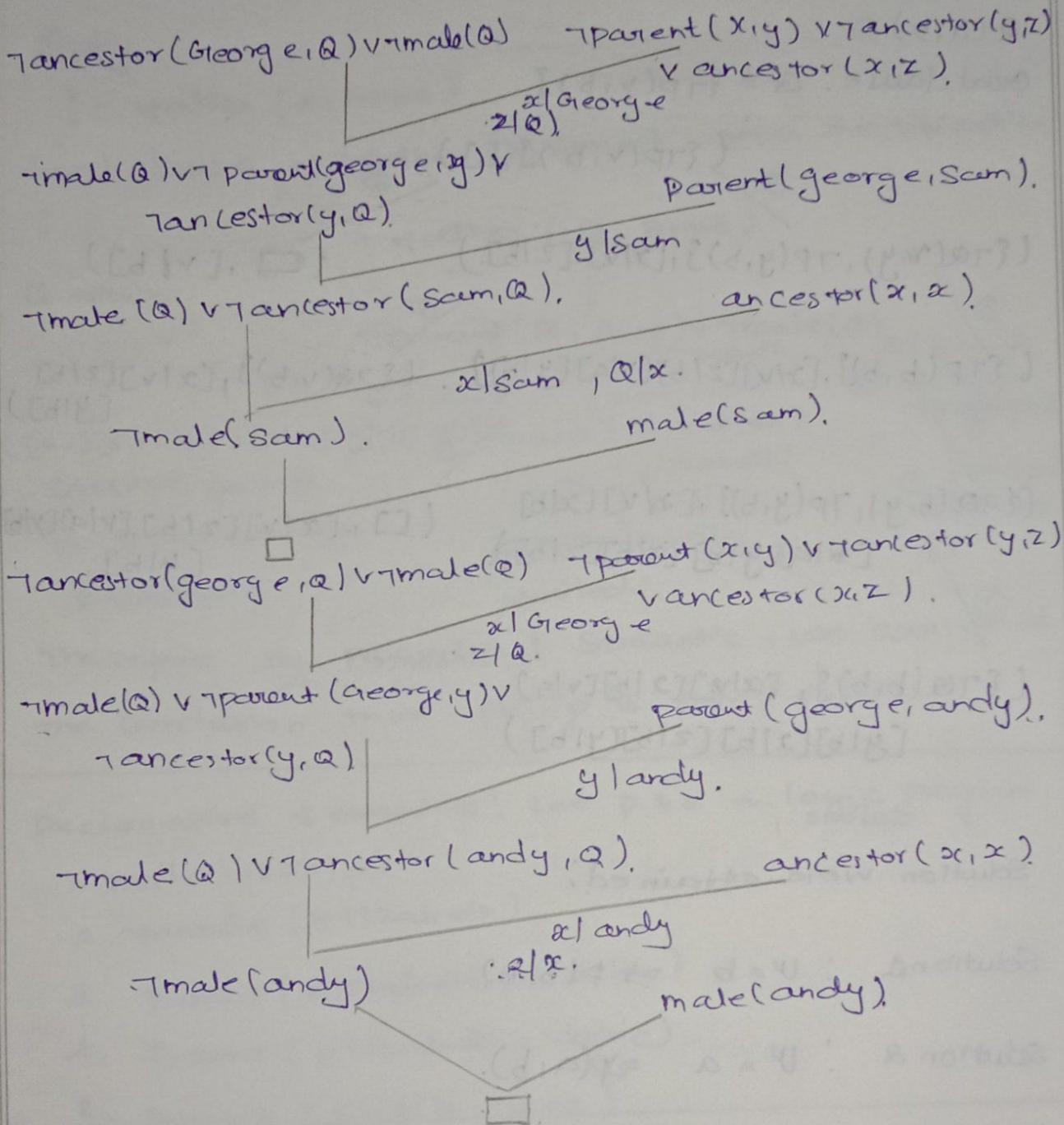


# SSN COLLEGE OF ENGINEERING RECORD SHEET

Sheet No. 3

$\text{ancestor}(\text{george}, a) \wedge \text{male}(a).$

Goal clause:  $\neg \text{ancestor}(\text{george}, a) \vee \neg \text{male}(a).$



Male ancestors of george are george, sam and andy.

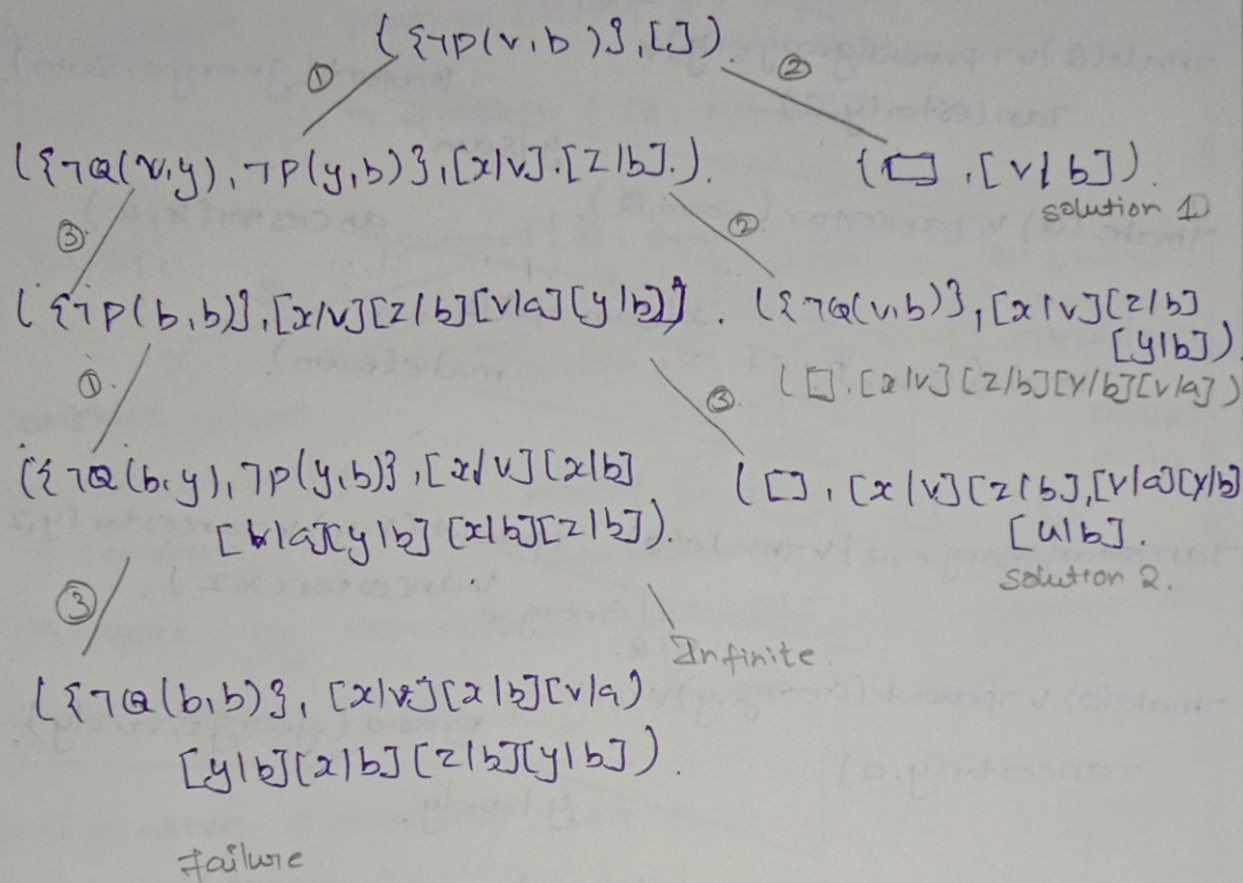


3.  $P(x, z) :- Q(x, y), P(y, z)$  ①

$P(u, w)$  ②

$Q(a, b)$  ③

Goal clause:  $G = \{ \neg P(v, b) \}$ .



Solution were obtained;

Solution 1 :  $v = b \Rightarrow P(b, b)$

Solution 2 :  $v = a \Rightarrow P(a, b)$

4. Procedural semantics :-

1. male (philip)
2. female (elizabeth)
3. parent (elizabeth, charles)
4. parent (elizabeth, anne)



5. parent ( philip , anne ).

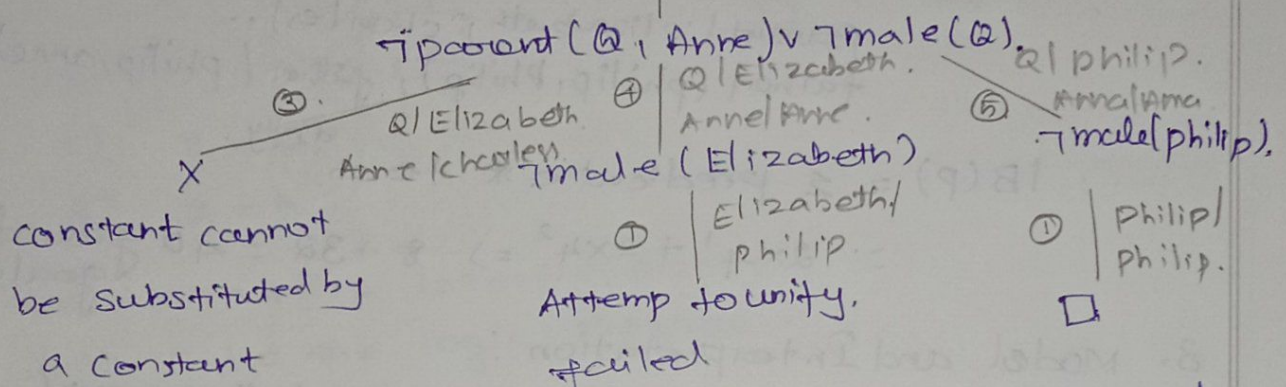
6. father (X,Y) :- parent (X,Y) , male (X).

Query

? - father (X, Anne).

Goal clause  $\Rightarrow \neg \text{father} (X, \text{Anne})$  After rectification

$\neg \text{father} (Q, \text{Anne})$ .



Therefore by procedural Semantics, we arrive at the conclusion that philip is Anne's father

5. Declarative Semantics: Let p be a logic program.

1. male (philip)

2. female (Elizabeth)

3. parent (elizabeth, charles)

4. parent (elizabeth, anne).

5. parent (philip, anne).

6.  $\neg \text{parent} (X, Y) \vee \neg \text{male} (X) \vee \text{father} (X, Y)$

Model theoretic Semantics based on following Principles.



1. Herbrand universe..

$$U(p) = \{ \text{philip, elizabeth, charles, anna} \}$$

$$|U(p)| = 4.$$

2. Herbrand Base:

$$B(p) = \{ \text{male}(\text{philip}), \text{male}(\text{elizabeth}), \dots, \\ \text{female}(\text{philip}), \text{female}(\text{elizabeth}), \dots, \\ \text{parent}(\text{philip, philip}), \text{parent}(\text{philip, elizabeth}), \dots, \\ \text{parent}(\text{elizabeth, charles}), \dots, \\ \text{father}(\text{philip, philip}), \text{father}(\text{philip, anna}) \}.$$

arity.

$$|B(p)| = \sum \text{predicate} * \text{term}$$

$$= 2 \times 4^1 + 2 \times 4^2 = 8 + 32 = 40 \text{ ground goals.}$$

3. Model and Interpretation :-

$$M(p) = \{ \text{male}(\text{philip}), \text{female}(\text{elizabeth}), \text{parent}(\text{elizabeth, charles}), \text{parent}(\text{elizabeth, anna}), \text{parent}(\text{philip, anna}), \text{father}(\text{philip, anna}) \}.$$

$$M(p) \in B(p).$$

$$\text{father}(\text{philip, anna}) \in M(p) \text{ since each}$$

$B_1, B_2, B_3, \dots$  in  $A \leftarrow B_1, B_2, B_3, \dots$  is in the interpretation.

$$\text{i.e. } \text{parent}(\text{philip, anna}), \text{male}(\text{philip}) \in M(p)$$

6.

$$p(a, a) \quad 0$$

$$p(a, b) \quad 2$$

$$p(x, y) :- p(y, x) \quad 2$$

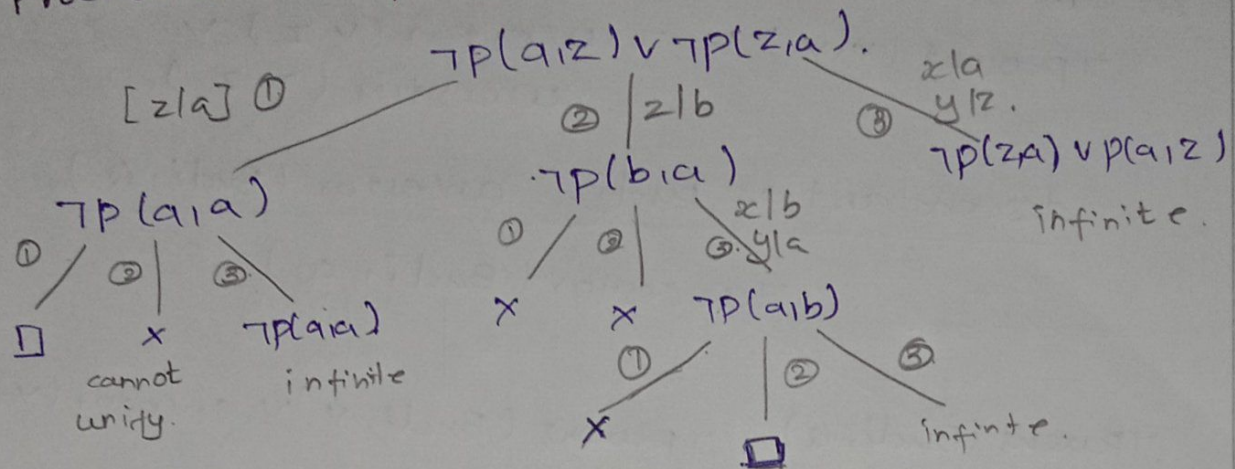
$$\neg p(y, x) \vee p(x, y) \quad \leftarrow$$

$$? - p(a, z) \vee p(z, a).$$

$$\text{Goal clause: } \neg p(a, z) \vee \neg p(z, a)$$



Procedural interpretation:-



Solution obtained :

- 1)  $z = a$
- 2)  $z = b$

Model theoretic interpretation:-

Let  $P$  be the logic program.

\*  $U(P) = \{a, b\}$   $|U(P)| = 2 \Rightarrow$  Herbrand universe.

\*  $B(P) = \{P(a, a), P(a, b), P(b, a), P(b, b)\} \Rightarrow$  Herbrand Base.

$$|B(P)| = 1 \times 2^2 = 4.$$

\* Model  $M(P) = \{P(a, a), P(a, b), P(b, a)\}$ .

$\downarrow$   
 $P(a, b)$  is in the model.

7. Logic program  $P$ .

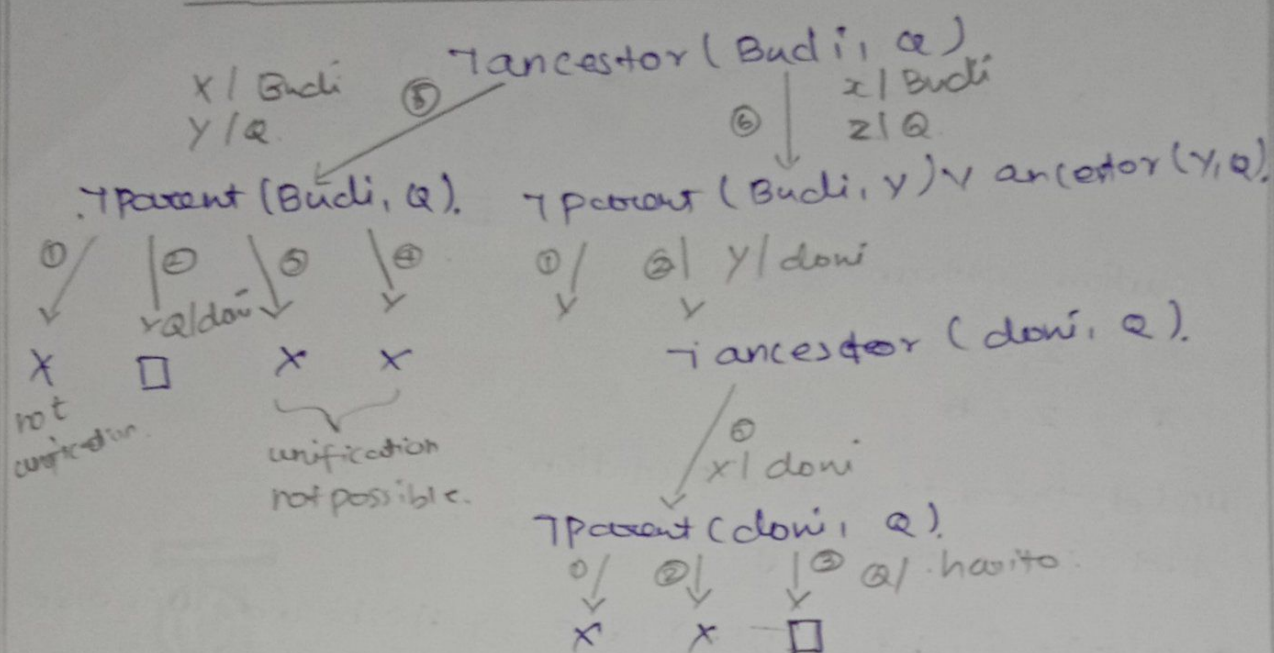
1.  $\text{parent}(\text{tukul}, \text{budi})$ .
2.  $\text{parent}(\text{budi}, \text{doni})$ .
3.  $\text{parent}(\text{doni}, \text{harto})$ .
4.  $\text{parent}(\text{harto}, \text{tomi})$ .

5.  $\text{ancestor}(x, y) :- \text{parent}(x, y)$   
 $\text{parent}(x, y) \vee \text{ancestor}(x, y)$



6.  $\text{ancestor}(x, z) :- \text{parent}(x, y), \text{ancestor}(y, z)$   
 $\neg \text{parent}(x, y) \vee \neg \text{ancestor}(y, z) \vee$   
 $\text{ancestor}(x, z)$

descendant of budhi - ancestor(Budhi, Q)



Answer : first 2 descendants of Budhi during DFS Traversal are.

1) doni.

2) harito.