

# Digital Signatures & Authentication Protocols

# Digital Signatures

- have looked at message authentication
  - but does not address issues of lack of trust
- digital signatures provide the ability to:
  - verify author, date & time of signature
  - authenticate message contents
  - be verified by third parties to resolve disputes
- hence include authentication function with additional capabilities

# Digital Signature Properties

- must depend on the message signed
  - must use information unique to sender
    - to prevent both forgery and denial
  - must be relatively easy to produce
  - must be relatively easy to recognize & verify
  - be computationally infeasible to forge
    - with new message for existing digital signature
    - with fraudulent digital signature for given message
- be practical save digital signature in storage

# Direct Digital Signatures

- involve only sender & receiver
- assumed receiver has sender's public-key
- digital signature made by sender signing entire message or hash with private-key
- can encrypt using receivers public-key
- important that sign first then encrypt message & signature
- security depends on sender's private-key

# Arbitrated Digital Signatures

- involves use of arbiter A
  - validates any signed message
  - then dated and sent to recipient
- requires suitable level of trust in arbiter
- can be implemented with either private or public-key algorithms
- arbiter may or may not see message

## Conventional Encryption, Arbiter Sees Message

(1)  $X \rightarrow A: M \parallel E(K_{xa}, [ID_X \parallel H(M)])$

(2)  $A \rightarrow Y: E(K_{ay}, [ID_X \parallel M \parallel E(K_{xa}, [ID_X \parallel H(M)]) \parallel T])$

## Conventional Encryption, Arbiter Does Not See Message

(1)  $X \rightarrow A: ID_X \parallel E(K_{xy}, M) \parallel E(K_{xa}, [ID_X \parallel H(E(K_{xy}, M))])$

(2)  $A \rightarrow Y: E(K_{ay}, [ID_X \parallel E(K_{xy}, M)]) \parallel E(K_{xa}, [ID_X \parallel H(E(K_{xy}, M)) \parallel T])$

## Public-Key Encryption, Arbiter Does Not See Message

(1)  $X \rightarrow A: ID\text{\underline{X}} \parallel E(PR\text{\underline{x}}, [ID\text{\underline{X}} \parallel E(PU\text{\underline{y}}, E(PR\text{\underline{x}}, M))])$

(2)  $A \rightarrow Y: E(PR\text{\underline{a}}, [ID\text{\underline{X}} \parallel E(PU\text{\underline{y}}, E(PR\text{\underline{x}}, M)) \parallel T])$

- $X$  = sender
- $Y$  = recipient
- $A$  = Arbiter
- $M$  = message
- $T$  = timestamp

# Authentication Protocols

- used to convince parties of each others identity and to exchange session keys
- may be one-way or mutual
- key issues are
  - confidentiality – to protect session keys
  - timeliness – to prevent replay attacks



# Replay Attacks

- where a valid signed message is copied and later resent
  - simple replay
  - repetition that can be logged
  - repetition that cannot be detected
  - backward replay without modification
- countermeasures include
  - use of sequence numbers (generally impractical)
  - timestamps (needs synchronized clocks)
  - challenge/response (using unique nonce)

# Using Symmetric Encryption

- as discussed previously can use a two-level hierarchy of keys
- usually with a trusted Key Distribution Center (KDC)
  - each party shares own master key with KDC
  - KDC generates session keys used for connections between parties
  - master keys used to distribute these to them

# Needham-Schroeder Protocol

- original third-party key distribution protocol
- for session between A B mediated by KDC
- protocol overview is:

1.  $A \rightarrow KDC: ID_A || ID_B || N_1$

2.  $KDC \rightarrow A: E_{K_a}[K_s || ID_B || N_1 ||$   
 $E_{K_b}[K_s || ID_A]]$

3.  $A \rightarrow B: E_{K_b}[K_s || ID_A]$

4.  $B \rightarrow A: E_{K_s}[N_2]$

5.  $A \rightarrow B: E_{K_s}[f(N_2)]$

# Needham-Schroeder Protocol

- used to securely distribute a new session key for communications between A & B
- but is vulnerable to a replay attack if an old session key has been compromised
  - then message 3 can be resent convincing B that is communicating with A
- modifications to address this require:
  - timestamps (Denning 81)
  - using an extra nonce (Neuman 93)

# Using Public-Key Encryption

- have a range of approaches based on the use of public-key encryption
- need to ensure have correct public keys for other parties
- using a central Authentication Server (AS)
- various protocols exist using timestamps or nonces

# Denning AS Protocol

- Denning 81 presented the following:
  1.  $A \rightarrow AS: ID_A \parallel ID_B$
  2.  $AS \rightarrow A: E_{KRas}[ID_A \parallel KU_a \parallel T] \parallel E_{KRas}[ID_B \parallel KU_b \parallel T]$
  3.  $A \rightarrow B: E_{KRas}[ID_A \parallel KU_a \parallel T] \parallel E_{KRas}[ID_B \parallel KU_b \parallel T] \parallel E_{KU_b}[E_{KRas}[K_s \parallel T]]$
- note session key is chosen by A, hence AS need not be trusted to protect it
- timestamps prevent replay but require synchronized clocks

# One-Way Authentication

- required when sender & receiver are not in communications at same time (eg. email)
- have header in clear so can be delivered by email system
- may want contents of body protected & sender authenticated

# Using Symmetric Encryption

- can refine use of KDC but can't have final exchange of nonces, vis:
  1.  $A \rightarrow \text{KDC}: ID_A \parallel ID_B \parallel N_1$
  2.  $\text{KDC} \rightarrow A: E_{K_a}[K_s \parallel ID_B \parallel N_1 \parallel E_{K_b}[K_s \parallel ID_A]]$
  3.  $A \rightarrow B: E_{K_b}[K_s \parallel ID_A] \parallel E_{K_s}[M]$
- does not protect against replays
  - could rely on timestamp in message, though email delays make this problematic



# Public-Key Approaches

- have seen some public-key approaches
- if confidentiality is major concern, can use:  
$$A \rightarrow B: E_{K_{Ub}}[K_s] \parallel E_{K_s}[M]$$
  - has encrypted session key, encrypted message
- if authentication needed use a digital signature with a digital certificate:  
$$A \rightarrow B: M \parallel E_{K_{Ra}}[H(M)] \parallel E_{K_{Ra}}[T \parallel ID_A \parallel KU_a]$$
  - with message, signature, certificate

# Digital Signature Standard (DSS)

- US Govt approved signature scheme FIPS 186
- uses the SHA hash algorithm
- designed by NIST & NSA in early 90's
- DSS is the standard, DSA is the algorithm
- a variant on ElGamal and Schnorr schemes
- creates a 320 bit signature, but with 512-1024 bit security
- security depends on difficulty of computing discrete logarithms

# DSA Key Generation

- have shared global public key values  $(p, q, g)$ :
  - a large prime  $p = 2^L$ 
    - where  $L = 512$  to  $1024$  bits and is a multiple of  $64$
  - choose  $q$ , a  $160$  bit prime factor of  $p-1$
  - choose  $g = h^{(p-1)/q}$ 
    - where  $h < p-1$ ,  $h^{(p-1)/q} \pmod{p} > 1$
- users choose private & compute public key:
  - choose  $x < q$  and compute  $y = g^x \pmod{p}$

# DSA Signature Creation

- to **sign** a message  $M$  the sender:
  - generates a random signature key  $k$ ,  $k < q$
  - nb.  $k$  must be random, be destroyed after use, and never be reused
- then computes signature pair:
$$r = (g^k \pmod p) \pmod q$$
$$s = (k^{-1} \cdot \text{SHA}(M) + x \cdot r) \pmod q$$
- sends signature  $(r, s)$  with message  $M$

# DSA Signature Verification

- having received  $M$  & signature  $(r, s)$
- to **verify** a signature, recipient computes:

$$w = s^{-1} \pmod{q}$$

$$u_1 = (\text{SHA}(M) \cdot w) \pmod{q}$$

$$u_2 = (r \cdot w) \pmod{q}$$

$$v = (g^{u_1} \cdot y^{u_2} \pmod{p}) \pmod{q}$$

- if  $v=r$  then signature is verified
- see book web site for details of proof why

# Summary

- have considered:
  - digital signatures
  - authentication protocols (mutual & one-way)
  - digital signature standard

# Test Your Understanding

- Data Authentication Algorithm (DAA) is based on
  - a) **DES**
  - b) AES
  - c) MD-5
  - d) SHA-1
- Which mode of operation is used in the DAA?
  - a) output feedback mode
  - b) electronic code block mode
  - c) cipher block chaining mode
  - d) cipher feedback mode
- DSS uses \_\_\_\_\_ hash algorithm