

# Consensus and Agreement

**Y. V. Lokeswari**

**Reference:** Ajay Kshemkalyani and  
Mukesh Singhal, Distributed Computing:  
Principles, Algorithms, and Systems



# Agreement

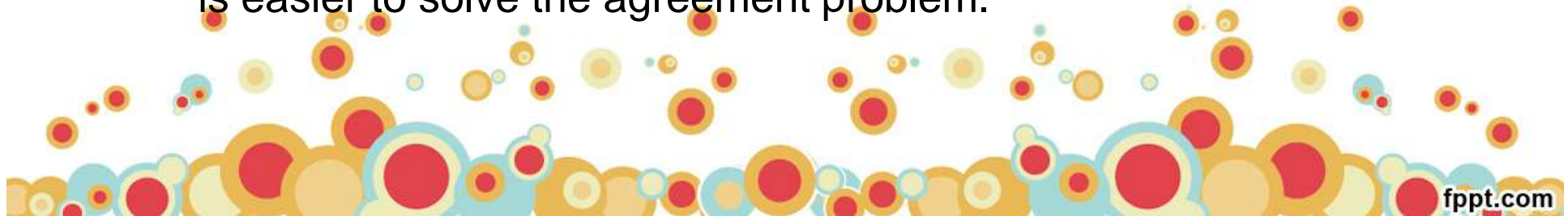
- Co-ordination require the **processes** to **exchange information** to negotiate with one another and eventually reach a common understanding or **agreement**, before taking application-specific actions.
- A classical example is that of the **commit decision** in database systems, processes collectively decide whether to **commit** or **abort** a transaction.
- **Assumptions**
  - Failure models
  - Synchronous / Asynchronous Communication
  - Network Connectivity
  - Sender Identification
  - Channel Reliability
  - Authentication vs Non-Authenticated messages
  - Agreement Variable

# Agreement

- **Failure models**: Among the  $n$  processes in the system, at most  $f$  processes can be faulty.
- The various failure models – **fail-stop, send omission and receive omission and Byzantine failures**.
- It may send a message to only a **subset** of the **destination set** before crashing.
- In **Byzantine failure** model, a process may **behave arbitrarily**.
- **Synchronous/asynchronous communication**: If a Failure-prone process chooses to send a message to process  $P_i$  but fails, then  $P_i$  cannot detect the **non-arrival** of the message in an asynchronous system because this scenario is indistinguishable from the scenario in which the **message takes a very long time in transit**.

# Agreement

- **Network connectivity**: The system has full **logical connectivity**, i.e., each process can communicate with any other by direct message passing.
- **Sender identification**: A process that receives a message always knows the **identity** of the **sender** process.
- **Channel reliability**: The channels are **reliable**, only the **processes** may **fail**.
  - **With unauthenticated messages**, when a faulty process relays a message to other processes, it can **forge** and claim that it was received from another processor or **tamper** the **contents** of the message.
  - Using **authentication** via techniques such as **digital signatures**, it is easier to solve the agreement problem.

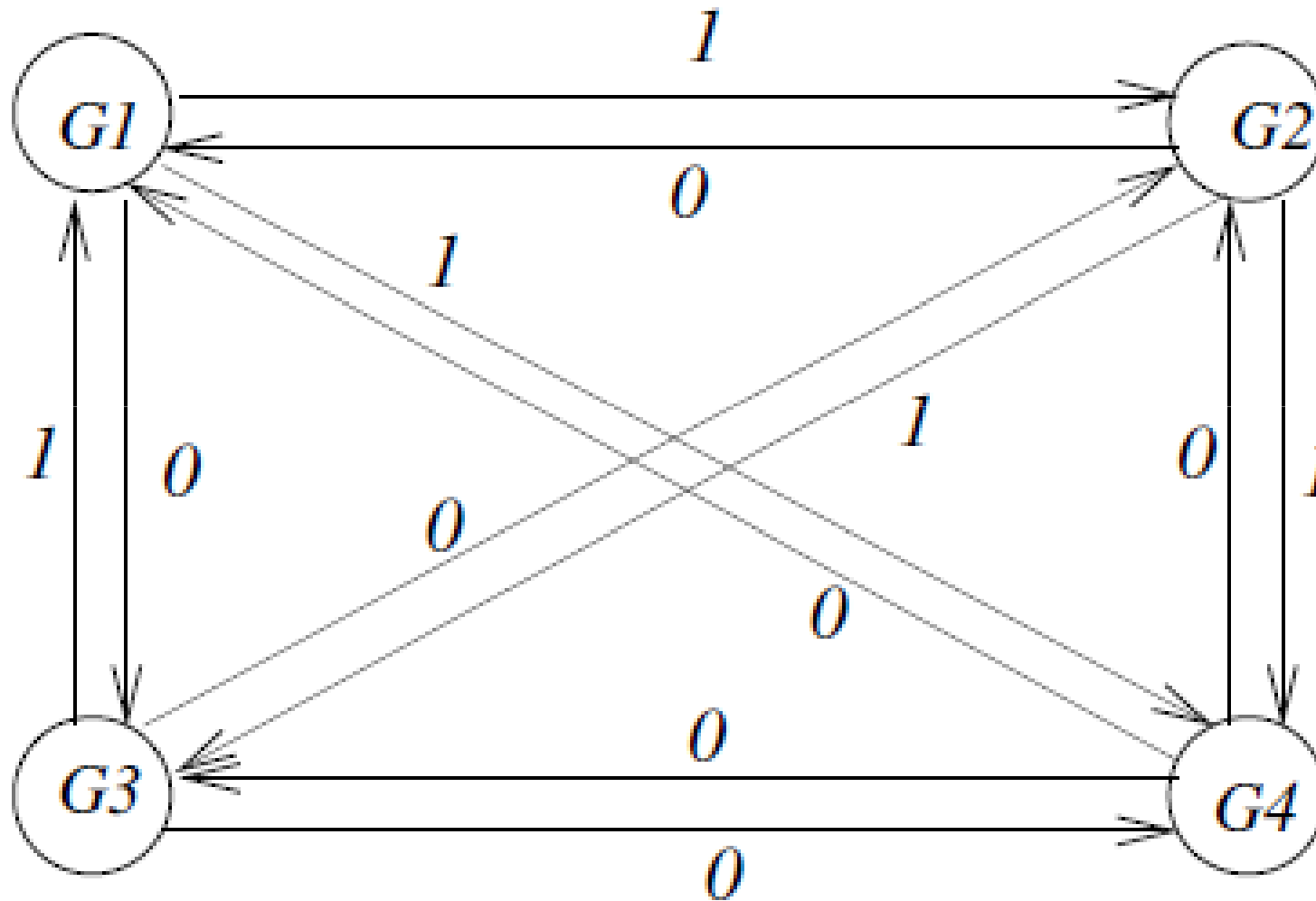


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- **Agreement variable** The agreement variable may be **Boolean** or **multi-valued** and **need not** be an **integer**.



# Byzantine General sending Confusing Messages





# Problem Specification

Byzantine Agreement (single source has an initial value)

**Agreement:** All non-faulty processes must agree on the same value.

**Validity:** If the source process is non-faulty, then the agreed upon value by all the non-faulty processes must be the same as the initial value of the source.

**Termination:** Each non-faulty process must eventually decide on a value.

Consensus Problem (all processes have an initial value)

**Agreement:** All non-faulty processes must agree on the same (single) value.

**Validity:** If all the non-faulty processes have the same initial value, then the agreed upon value by all the non-faulty processes must be that same value.

**Termination:** Each non-faulty process must eventually decide on a value.

Interactive Consistency (all processes have an initial value)

**Agreement:** All non-faulty processes must agree on the same array of values  $A[v_1 \dots v_n]$ .

**Validity:** If process  $i$  is non-faulty and its initial value is  $v_i$ , then all non-faulty processes agree on  $v_i$  as the  $i$ th element of the array  $A$ . If process  $j$  is faulty, then the non-faulty processes can agree on any value for  $A[j]$ .

**Termination:** Each non-faulty process must eventually decide on the array  $A$ .



# Overall Results

Failure mode	Synchronous system (message-passing and shared memory)	Asynchronous system (message-passing and shared memory)
No failure	agreement attainable; common knowledge also attainable	agreement attainable; concurrent common knowledge attainable
Crash failure	agreement attainable $f < n$ processes $\Omega(f + 1)$ rounds	agreement not attainable
Byzantine failure	agreement attainable $f \leq \lfloor (n - 1)/3 \rfloor$ Byzantine processes $\Omega(f + 1)$ rounds	agreement not attainable

**Table:** Overview of results on agreement.  $f$  denotes number of failure-prone processes.  $n$  is the total number of processes.

In a failure-free system, consensus can be attained in a straightforward manner





# Agreement in a failure-free system (synchronous or asynchronous)

- In a **failure-free** system, **consensus** can be **reached** by **collecting information** from the **different processes**, arriving at a “**decision**,” and **distributing** this **decision** in the **system**.
- A distributed mechanism would have each process **broadcast** its **values** to others, and each **process computes** the **same function** on the **values received**.
- Examples being the **majority, max, and min functions**.
- Distribute the decision may be based on the **token circulation** on a **logical ring**, or the **three-phase tree-based broadcast, convergecast–broadcast**, or **direct communication** with all nodes.

# Agreement in a failure-free system (synchronous or asynchronous)

- In a **synchronous system**, this can be done simply in a **constant number of rounds**.
- **common knowledge** of the decision value can be obtained using an **additional round**.
- In an **asynchronous system**, consensus can similarly be reached in a **constant number of message hops**.
- **concurrent common knowledge** of the **consensus** value can also be attained, **using** the **algorithms**.
- **Reaching agreement** is **straightforward** in a **failure-free system**.
- **Focus** on **failure-prone** systems.



# Summary

- Agreement.
- Problem Definition:
  - Byzantine Problem.
  - Consensus.
  - Interactive Consistency.
- Agreement in a failure-free system.



# Thank You

