

- Railway network
- Airway network across the world
- Telecom network
- Friends / contacts in social websites

SSN<sup>14</sup>

5) ~~powerful but not central~~ ~~central but not powerful~~  $\Rightarrow$  State cap among country  
President of a country **SSN**<sup>15</sup>

3) degree centrality

$$v_1 = \frac{d(v_1)}{n-1} = \frac{2}{5-1} = \frac{1}{2} = 0.5$$

$$v_2 = \frac{3}{5-1} = \frac{3}{4} = 0.75$$

$$v_3 = \frac{2}{5-1} = 0.5$$

$$v_4 = \frac{3}{5-1} = \frac{3}{4} = 0.75$$

$$v_5 = \frac{2}{5-1} = \frac{1}{2} = 0.5$$

4) Since one ~~country~~ country shares boundaries with all other countries, the graph has to be undirected to allow sharing boundaries.  
maximum possible boundaries

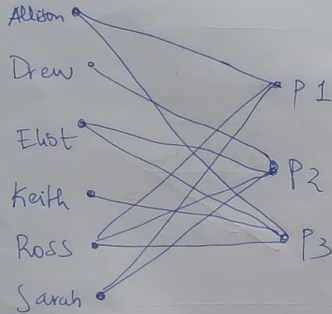
$$= \frac{n(n-1)}{2} \Rightarrow \frac{5(4)}{2}$$

$$\text{where } n=5 \text{ countries} = 10 \text{ boundaries}$$

6) social network notation Schemes

i) matrix notation using adjacency matrix  $\begin{bmatrix} a & b \\ 1 & 2 \end{bmatrix}$

ii) Lines notation and node  
where L represents a line ( $\vec{n_1} \rightarrow n_2$ )  
W represents a node



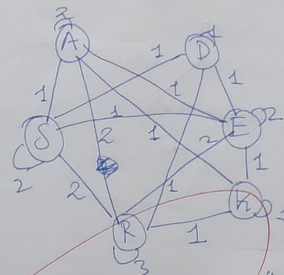
Converting to one mode Affiliation h/w  
having only the actors

	A	D	E	K	R	S
A	2	0	1	1	2	1
D	0	1	1	0	1	1
E	1	1	2	1	2	1
K	1	0	1	1	1	0
R	2	1	2	1	3	2
S	1	1	1	0	2	2

The connections (tie) to other actors are  
done on the basis of the same parties  
they go.

So the new one-mode affiliation network

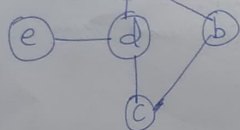
is



where the number on the edge gives no. of  
relations.

Part-A

- 1) - Social Network Analysis is the study of social groups which are a collection of actors and have relationship among them (ties).  
- It is used find relationship and other useful data if two find if two actor are in same groups,...



### Betweenness Centrality

node	edges with node b/w	Total no. of shortest paths	betweenness
a	bc cd de bd be ce	1 1 1 2 2 1	0/1=0 0 0 $\frac{1}{2}=0.5$ 0.5 0

for node a betweenness = 1  $\leftarrow \sum = 1$

b	ac ad ae cd ce de	1 0 0 0 0 0	2 1 1 1 1 1	0.5 0 0 0 0 0
---	----------------------------------	----------------------------	----------------------------	------------------------------

for node b betweenness = 0.5  $\leftarrow \sum = 0.5$

Similarly since c is symmetrical to a  
node c betweenness = 1

### node d

d	ab ac de bc be ce	0 1 1 0 2 1	1 2 1 2 1 1	0.5 1 0 1 1 1
---	----------------------------------	----------------------------	----------------------------	------------------------------

node d betweenness = 3.5  $\leftarrow \sum = 3.5$

### node e

e	ab ac ad bc bd cd	0 0 0 0 0 0	1 1 1 1 1 1	0 0 0 0 0 0
---	----------------------------------	----------------------------	----------------------------	----------------------------

node e betweenness = 0  $\leftarrow \sum = 0$

node	betweenness
a	1
b	0.5
c	1
d	3.5
e	0

### Closeness Centrality

#### Distance matrix

	a	b	c	d	e	Sum of distance	inverse of distance gives Closeness
a	0	1	2	1	2	=6	$\frac{1}{6} = 0.166$
b	1	0	1	2	3	=7	$\frac{1}{7} = 0.1428$
c	2	1	0	1	2	=6	$\frac{1}{6} = 0.166$
d	1	2	1	0	1	=5	$\frac{1}{5} = 0.2$
e	2	3	2	1	0	=8	$\frac{1}{8} = 0.125$

7)

## Graph models for Social Network

SSN

- i) Random graph
- ii) Alpha graph
- iii) Beta graph
- iv) Scale graphs

### i) Random graph

- the relationship between nodes are random in nature

Pros - Any node (Actor) can be related to another node.

Cons - does not guarantee a relation between any pair of node since it is random.

### ii) Alpha graph

- ~~with~~ with given parameter  $\alpha$ , it determines if a node is connected to another node.

Pros - can generate a graph based on alpha parameter

Cons - alpha value determines which two nodes have relation and may not be accurate.

SSN

### iii) Beta graph

- Based on the ~~beta~~ beta parameter, it gives an estimate of relationship between two nodes

Pros

- ~~can~~ can be used to generate better graphs than alpha.

Cons

- All 3 (random, alpha, beta) graphs are not scalable.

### iv) Scale graph

- with increase and constant change in the social network, we need a graph which is dynamic

Pros

- can accommodate changes in scale dynamically unlike other graph models.

Cons

- Relationship can't be generated based on other node relations.



d) Tour is ~~the~~ a walk in which it covers all the nodes atleast once.

$n_0 \rightarrow n_1 \rightarrow n_2 \rightarrow n_3 \rightarrow n_0 \rightarrow n_4 \rightarrow n_5 \rightarrow n_6$   
 $\rightarrow n_7 \rightarrow n_8 \rightarrow n_5 \rightarrow n_4 \rightarrow n_9 \rightarrow n_{10} \rightarrow n_4$

e) Nodal degree  
 no. of edges incident on a node

node	degree	$(d - \bar{d})^2$
$n_0$	3	0.449
$n_1$	2	0.109
$n_2$	2	0.109
$n_3$	2	0.109
$n_4$	3	0.449
$n_5$	3	0.449
$n_6$	2	0.109
$n_7$	2	0.109
$n_8$	2	0.109
$n_9$	3	0.449
$n_{10}$	2	0.109
$n_{11}$	2	0.109

$\sum (d \geq 8) \quad \bar{d} = 10.516$

f) mean nodal deg  $= \frac{\sum d}{n} = \frac{28}{12} = 2.33$

g) variance  $= \frac{\sum (d - \bar{d})^2}{n} = \frac{10.516}{12}$   
 $= 0.8763$

h) density of graph  $= \frac{2L}{g(g-1)}$   
 where  $L$  is no. of lines  
 $g$  is no. of nodes

$L=14$   
 $g=12 \Rightarrow A = \frac{2(14)}{12(11)} = 0.21$

i) Cut-point

min no. of cuts  $= 1$  <sup>node</sup>  
 to make graph into subgraphs  
~~cut node 4 makes 3 components~~

j) Edge connectivity

min no. of cuts of edge  $= 1$   
 to make graph into subgraph

~~either cut the edges~~

$n_0 \rightarrow n_4$  or  $n_4 \rightarrow n_5$  or  $n_4 \rightarrow n_9$   
 cutting the edge makes 2 components

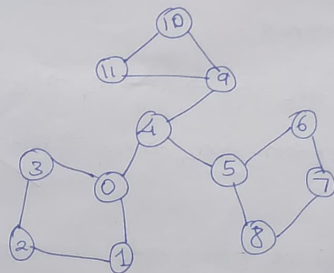
there are large number of ties with each node making it difficult to store data of each person in the node.

SSN

- such complex social networks need other alternative ways for data collection.

### Alternatives

- Consider to check if there is already existing databases for a part (subgraph) of the social network.
- Each individual part of existing databases can be combined to make the data collection of the whole social network.
- Considering Ebooks and online library for data collection (data bases might already have some information of the nodes)
- Online databases can be used to collect data of each individual node rather than doing it manually which ~~waste~~ are the efficiency and ~~save~~ saves time.



SSN

### a) Eccentricity of node 3

it is the longest geodesic distance with node 3 and any other node.

$$\Rightarrow \max (d[3, j]) \text{ and } j \neq 3$$

$\Rightarrow$  from node 3 to node 7

$$\text{Eccentricity of nodes} = 5$$

### b) Walk = collection of sequence of nodes which are adjacent.

$$n_0 \rightarrow n_1 \rightarrow n_2 \rightarrow n_3 \rightarrow n_4 \rightarrow n_5 \rightarrow n_6 \rightarrow n_7 \rightarrow n_8 \rightarrow n_9 \rightarrow n_{10}$$

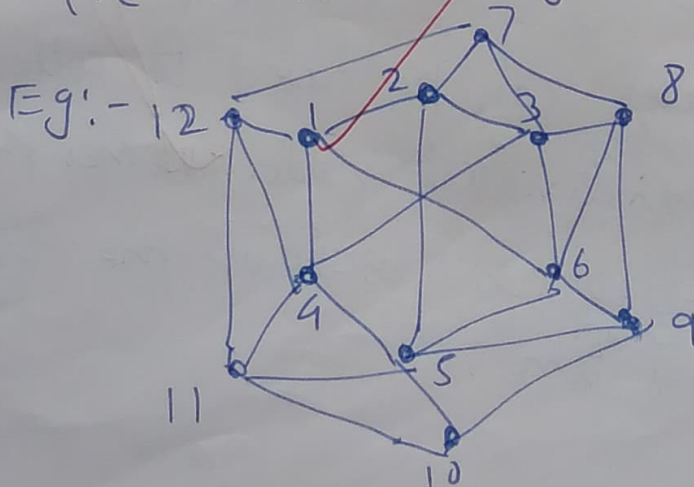
### c) Trail = Sequence of nodes which are adjacent and visit the ~~node~~ edges exactly once (can visit nodes multiple times)

$$n_0 \rightarrow n_3 \rightarrow n_2 \rightarrow n_1 \rightarrow n_0 \rightarrow n_4 \rightarrow n_5$$

11)

Data collection complexities in social networks

- i) social network is a large collection of nodes and relations.
- ii) Since there are large number of nodes in social networks, collection of data is also large.
- iii) when manually collecting such huge number of data becomes very hard.
- iv) The efficiency for collection is very low which is 50%.
- v) Since the efficiency is very less, it takes a lot of time to collect all the data.
- vi) The collected data also has to be stored somewhere which is capable of collecting large data i.e. we need large storage boxes.



A social network  
of 12 nodes



# SRI SIVASUBRAMANIYA NADAR COLLEGE OF ENGINEERING

(An Autonomous Institution, Affiliated to Anna University, Chennai)

Rajiv Gandhi Salai (OMR), Kalavakkam - 603 110

## THEORY EXAMINATIONS

Register Number	205001102		
Name of the Student	Shrijith M.R		
Degree and Branch	BE . CSE	Semester	VII
Subject Code and Name	VCS1722 - social network Analysis		
Assessment Test No.	Cat - 1	Date	13/9/2023

Details of Marks Obtained									
Part A		Part B				Part C			
Question No.	Marks	Question No.	(a) Marks	(b) Marks	Total Marks	Question No.	(a) Marks	(b) Marks	Total Marks
1	2	7	5			10			
2	✓								
3	2	8	6			11	9		
4	✓						12		
5	2	9	6			13	9		
6	1								
Total (A)		Total (B)				Total (C)			<div>44 50</div>
Grand Total (A+B+C)					Marks (In Words)				
Signature of the Faculty					<div>✓</div>				



④  $\Rightarrow$  It will be an undirected graph since the borders shared among the countries will be bidirectional.

SSN 4

$\Rightarrow$  Maximum possible borders

$${}^5C_2 = \frac{5!}{2! \times 3!} = \frac{5 \times 4 \times 3!}{2 \times 2!} = 10 //$$

⑤ Notational schemes for social network

- \* Graphical
- \* Semantic
- \* Algebraic

⑤ Case 1: Actor powerful, not central

Eg. User in a social platform.

Case 2: Actor central, not powerful

Eg. Social media applications which are used by all users.

PART-B

⑦

Graph Models

SSN 5

④ Random graph model

$\Rightarrow$  As the name suggests, the points or nodes are connected based on certain random probability.

$\Rightarrow$  The points are chosen at random and are assigned to be connected with other nodes using random probability.

Pros

$\Rightarrow$  Randomly generated points and node connections.

$\Rightarrow$  Less dense graph will be created.

Cons

$\Rightarrow$  Not suitable for complex social network analysis.

## ① Social Network Analysis

Social network analysis is defined as analysing of social networking in terms of graphs, nodes and edges including networking among the nodes.

## ② Global structures of Social Networks

- \* Graphs structure
- \* Sociometric structure
- \* Algebraic structure

③

$$\text{Degree Centrality} = \frac{d(i)}{n-1}$$

$$d_c(v_1) = 2/4 = 0.5$$

$$d_c(v_2) = 3/4 = 0.75$$

$$d_c(v_3) = 2/4 = 0.5$$

$$d_c(v_4) = 3/4 = 0.75$$

$$d_c(v_5) = 2/4 = 0.5$$

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## THEORY EXAMINATIONS

Register Number	205001085		
Name of the Student	V. Sabarivasan		
Degree and Branch	BE CSE	Semester	VII
Subject Code and Name	UCS17R2 Social Network Analysis		
Assessment Test No.	I	Date	

Details of Marks Obtained									
Part A		Part B				Part C			
Question No.	Marks	Question No.	(a) Marks	(b) Marks	Total Marks	Question No.	(a) Marks	(b) Marks	Total Marks
1	2	7				10			
2	✓								
3	2	8	6			11	5		
4	2						12	8	
5	2	9	1			13			
6	2								
Total (A)		Total (B)				Total (C)			
Grand Total (A+B+C)					Marks (In Words)				30/50
Signature of the Faculty					