

1) Liang Barsky Line Clipping Algorithm:

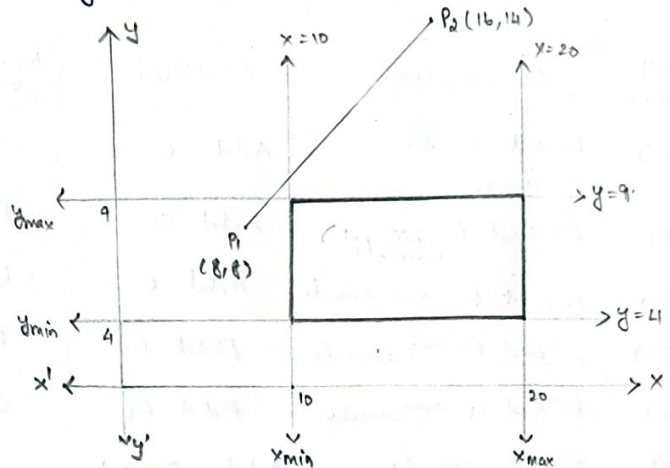
Given:

$$(x_{\min}, x_{\max}) = (10, 20)$$

$$(y_{\min}, y_{\max}) = (4, 9)$$

$$P_1 = (8, 8)$$

$$P_2 = (16, 14)$$



$$\Rightarrow \Delta x = x_2 - x_1 = 16 - 8 = 8$$

$$\Delta y = y_2 - y_1 = 14 - 8 = 6$$

W.K.T,

for an integer k , P_k and q_k are defined as

$$k=1 \Rightarrow -u\Delta x \leq x_1 - x_{\min} \Rightarrow P_1 = -\Delta x \quad q_1 = x_1 - x_{\min} \Rightarrow u_1 = q_1/P_1$$

$$k=2 \Rightarrow +u\Delta x \leq x_{\max} - x_1 \Rightarrow P_2 = \Delta x \quad q_2 = x_{\max} - x_1 \Rightarrow u_2 = q_2/P_2$$

$$k=3 \Rightarrow -v\Delta y \leq y_1 - y_{\min} \Rightarrow P_3 = -\Delta y \quad q_3 = y_1 - y_{\min} \Rightarrow v_3 = q_3/P_3$$

$$k=4 \Rightarrow v\Delta y \leq y_{\max} - y_1 \Rightarrow P_4 = \Delta y \quad q_4 = y_{\max} - y_1 \Rightarrow v_4 = q_4/P_4$$

If k , we have $P_k \neq 0 \Rightarrow$ we find all the intersection points (r_k)

k	q_k	P_k	$r_k = \frac{q_k}{P_k}$
1	$8 - 10 = -2$	-8	$1/4$
2	$20 - 8 = 12$	8	$3/2$
3	$8 - 4 = 4$	-6	$-2/3$
4	$9 - 8 = 1$	$+6$	$1/6$

W.K.T, for any k , $r_k \leq 1$ and $r_k \geq 0$ \Rightarrow We ignore r_2 ($\because r_2 > 1$) and r_3 ($\because r_3 < 0$)Now, for which $P_k < 0$, $u_{\min} = \max(0, r_k)$

$$\Rightarrow u_{\min} = \max(0, r_1) \quad (\because P_1 < 0)$$

$$\Rightarrow \boxed{u_{\min} = 1/4 = 0.25} \quad (r_1 = 1/4)$$

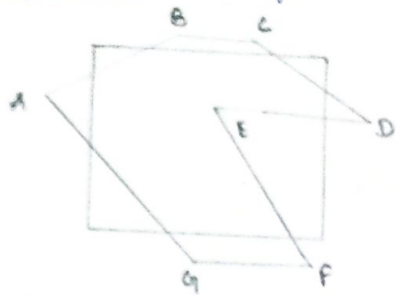
for which $P_k > 0$, $u_{\max} = \min(1, r_k)$

$$\Rightarrow u_{\max} = \min(1, r_4) \quad (\because P_4 > 0)$$

$$\Rightarrow \boxed{u_{\max} = 1/6 = 0.17} \quad (r_4 = 1/6)$$

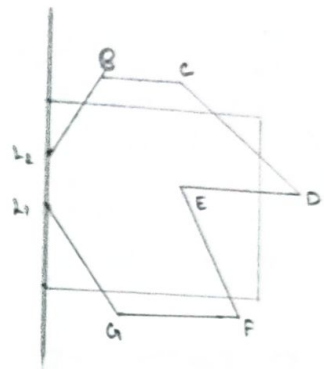
Here, $u_{\min} > u_{\max} \Rightarrow$ The line connecting points $P_1(8, 8)$ and $P_2(16, 14)$ is outside the clipping window.

② Sutherland-Hodgeman Clipping Algorithm:



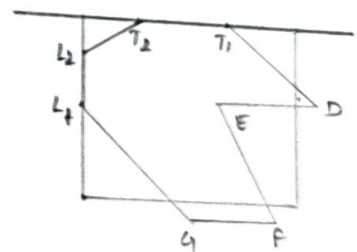
Pair of vertices	Description	Condition	New vertex list
(B, C)	B and C are inside	Add C	C
(C, D)	C and D are inside	Add D	D
(D, E)	D and E are inside	Add E	E
(E, F)	E and F are inside	Add F	F
(F, G)	F and G are inside	Add G	G
(G, A)	G is inside A is outside	Add intersection point, L1	L1
(A, B)	A is outside B is inside	Add intersection point, L2 and B	L2 B

Left:



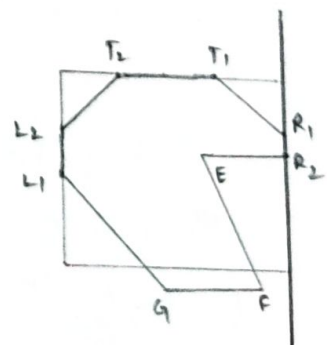
(B, C)	B and C are outside	Nothing	
(C, D)	C is outside D is inside	Add intersection point, T1 and D	T1 D
(D, E)	Both are inside	Add E	E
(E, F)	E and F are inside	Add F	F
(F, G)	F and G are inside	Add G	G
(G, L1)	G and L1 are inside	Add L1	L1
(L1, L2)	L1 and L2 are inside	Add L2	L2
(L2, B)	L2 is inside B is outside	Add intersection point, T2 and B	T2 B

Top:



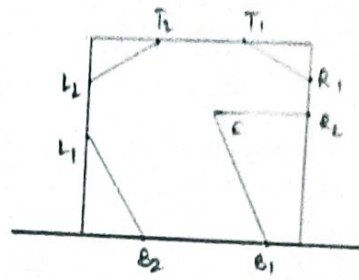
(T2, T1)	T2 and T1 are inside	Add T1	T1
(T1, D)	T1 is inside D is outside	Add intersection point, R1 and D	R1 D
(D, E)	D is outside E is inside	Add intersection point, R2 and E	R2 E
(E, F)	E and F are inside	Add F	F
(F, G)	F and G are inside	Add G	G
(G, L1)	G and L1 are inside	Add L1	L1
(L1, L2)	L1 and L2 are inside	Add L2	L2
(L2, T2)	L2 and T2 are inside	Add T2	T2

Right:

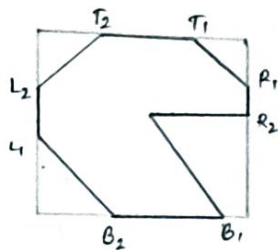


(T_0, T_1)	T_0 and T_1 are inside	Add T_1	T_1
(T_1, R_1)	R_1 and T_1 are inside	Add R_1	R_1
(R_1, R_2)	R_1 and R_2 are inside	Add R_2	R_2
(R_2, E)	R_2 and E are inside	Add E	E
(E, F)	E is inside F is outside	Add intersection point, B_1	B_1
(F, G)	F and G are outside	-	
(G, L_1)	G is outside L_1 is inside	Add intersection point, B_2 & L_1	B_2 L_1
(L_1, L_2)	L_1 and L_2 are inside	Add L_2	L_2
(L_2, T_2)	L_2 and T_2 are inside	Add T_2	T_2

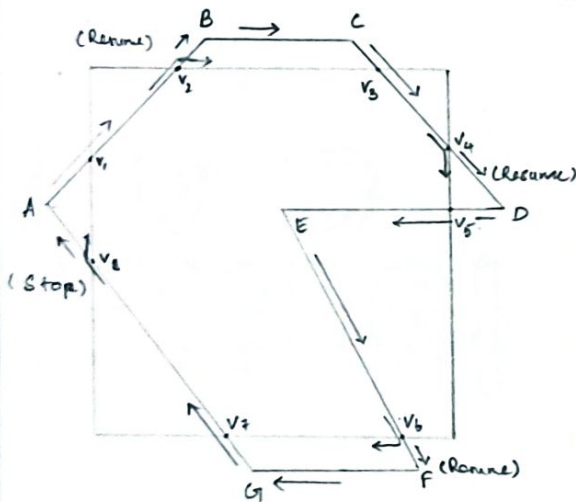
Bottom:



Clipped Polygon



③ Weiler - Atherton Clipping Algorithm:



For the given polygon, mark the intersection points of the sides with the clipping window as $V_1, V_2, V_3, V_4, V_5, V_6, V_7$ and V_8 . Inside the clipping window,

(1) $V_1 \rightarrow V_2$ is going from outside to inside,
 \Rightarrow follow the polygon boundary ($V_1 - V_2$)

(2) $V_2 \rightarrow B$ is going from inside to outside,
 \Rightarrow follow the clipping window ($V_2 - V_3$)

(3) $V_3 \rightarrow V_4$ is going from outside to inside,
 \Rightarrow follow the polygon ($V_3 - V_4$)

(4) $V_4 \rightarrow D$ is going from inside to outside \Rightarrow follow the window ($V_4 - V_5$)

(5) $V_5 \rightarrow E$ is going from outside to inside \Rightarrow follow the polygon ($V_5 - E - V_6$)

(6) $V_6 \rightarrow F$ is going from inside to outside \Rightarrow follow the window ($V_6 - V_7$)

(7) $V_7 \rightarrow V_8$ is going from outside to inside \Rightarrow follow the polygon ($V_7 - V_8$)

(8) $V_8 \rightarrow A$ is going from inside to outside \Rightarrow follow the window ($V_8 - V_1$)

$G \rightarrow A$: stop clipping

Clipped Polygon:

