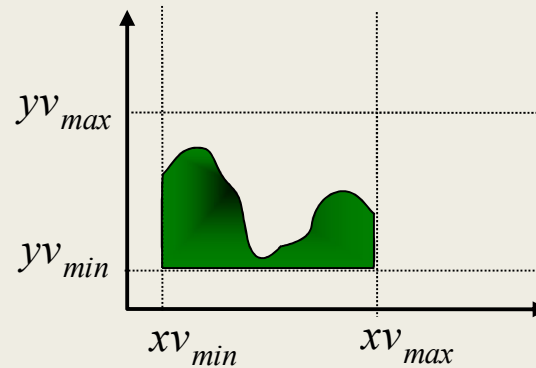
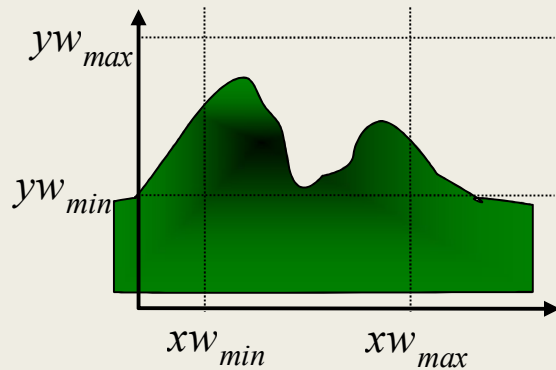


Two Dimensional Viewing

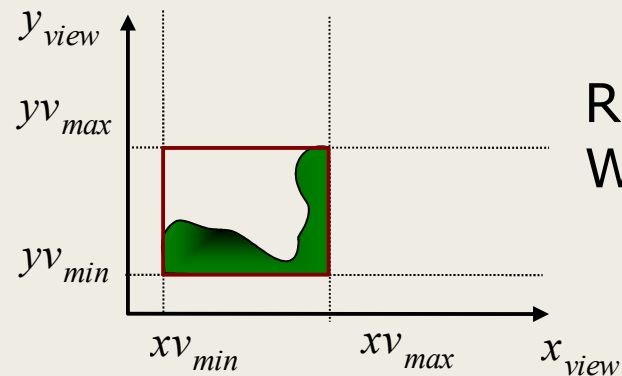
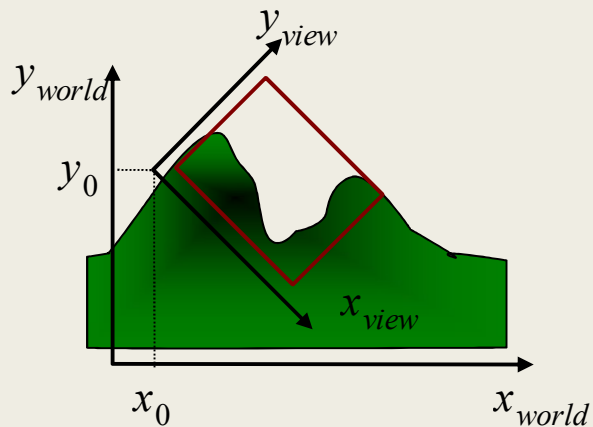
The Viewing Pipeline

- Graphics package allows the user to specify which part of a defined picture to be displayed where that part is to be displayed on the display device
- **Window**
 - *A world-coordinate area selected for display.
defines what is to be viewed*
- **Viewport**
 - *An area on a display device to which a window is mapped.
defines where it is to be displayed*
- **Viewing transformation**
 - *The mapping of a part of a world-coordinate scene to device coordinates.*
 - *The two dimensional viewing transformation is referred as windowing transformations.*

Two-Dimensional Viewing



Rectangular Window



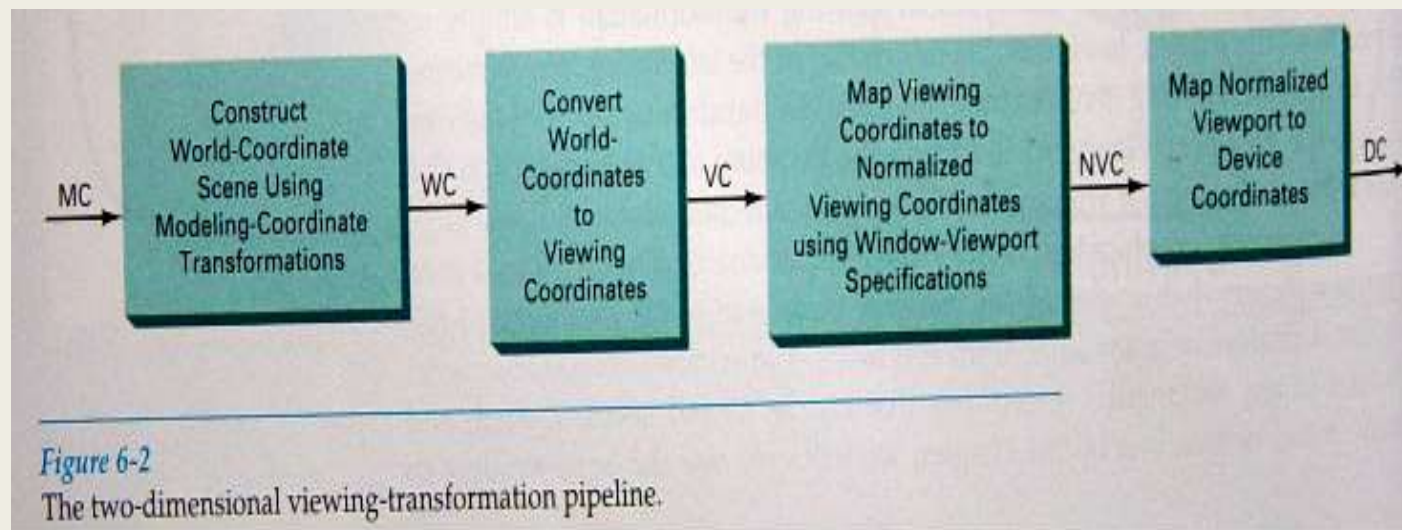
Rotated Window

Two-Dimensional Viewing

- Rectangular window of different orientation viewing transformations follows the following steps
- Construct the scene in world coordinates using the output primitives and attributes.
- Obtain the particular orientation for the window, set up a two dimensional viewing coordinate system in the world coordinate plane and define a window in the viewing coordinate system.
- Once the reference frame is established transform the descriptions in world coordinates to viewing coordinates.
- We then define a viewport in normalized coordinates and map the viewing coordinate of the scene to normalized coordinates

The Viewing Pipeline

- All parts of the picture that lie outside the viewport are clipped .
- Contents of the viewport are transferred to device coordinates.

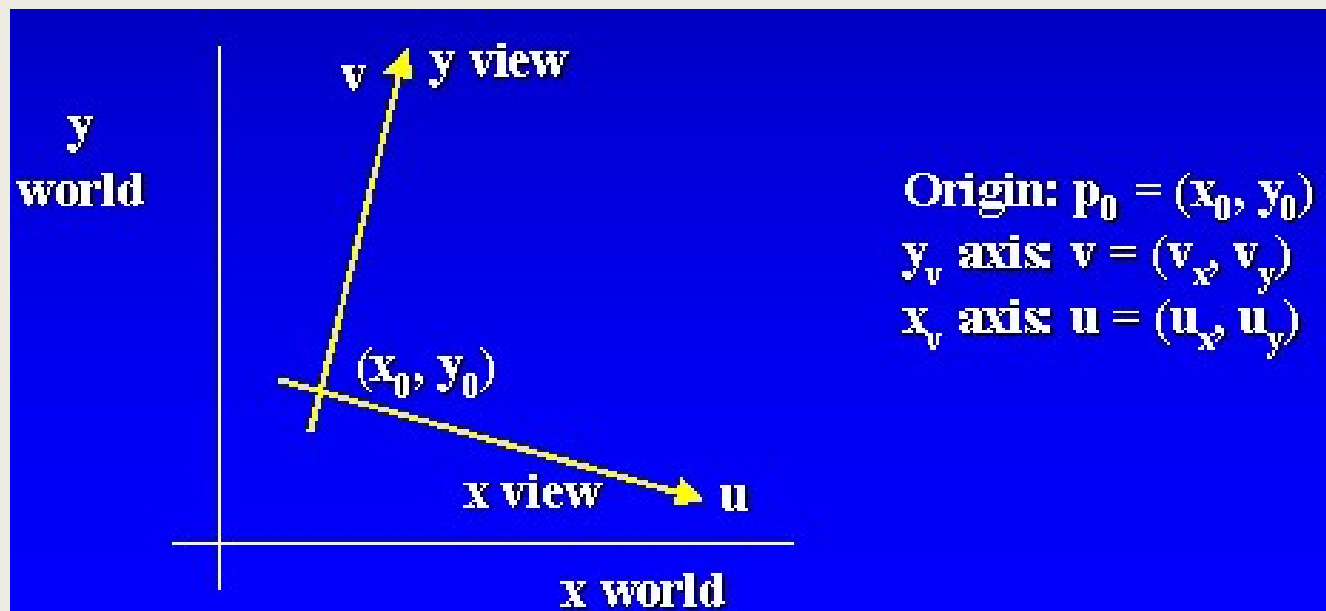


Two-Dimensional Viewing

- By changing the position of the viewport we can view objects at different positions on the display area of the output device.
- **Zooming effects**
 - *Successively mapping different-sized windows on a fixed-sized viewports.*
- **Panning effects**
 - *Moving a fixed-sized window across the various objects in a scene.*
- **Device independent**
 - *Viewports are typically defined within the unit square. (normalized coordinates)*
 - *This provides means for separating the viewing and other transformations from specific output device requirements.*

Viewing Coordinate Reference Frame

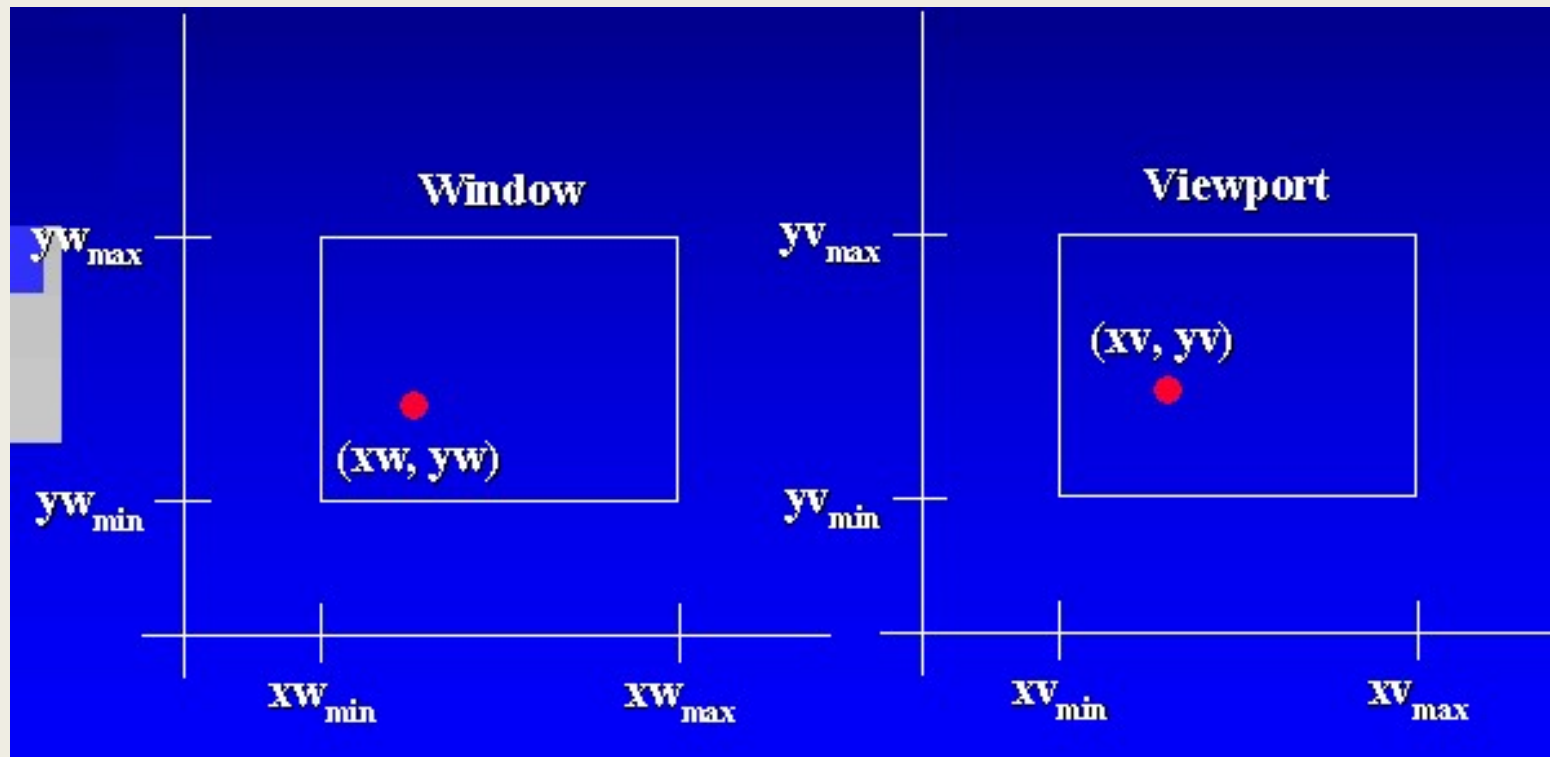
- The reference frame for specifying the world-coordinate window.
 - *Viewing-coordinate origin: $P_0 = (x_0, y_0)$*
 - *Establish the orientation or rotation of this reference frame.*
 - *Specify View up vector V : Define the viewing y_v direction*



Viewing Coordinate Reference Frame

- Given V calculate the components of unit vectors v_x, v_y and u_x, u_y for the viewing y_v and X_v .
- These unit vectors aligns the viewing x_v, y_v axes with world axes x_w, y_w
- The composite two dimensional transformation to convert world coordinates to viewing coordinates is
- Translate the viewing origin to the world origin
- Rotate to align the two coordinate reference frames.
 - $M_{wc,vc} = R.T$

Window-to-Viewport Coordinate Transformation



Window-to-Viewport Coordinate Transformation

$$\frac{x_v - x_{v_{\min}}}{x_{v_{\max}} - x_{v_{\min}}} = \frac{x_w - x_{w_{\min}}}{x_{w_{\max}} - x_{w_{\min}}} \quad \frac{y_v - y_{v_{\min}}}{y_{v_{\max}} - y_{v_{\min}}} = \frac{y_w - y_{w_{\min}}}{y_{w_{\max}} - y_{w_{\min}}}$$

$$x_v = x_{v_{\min}} + (x_w - x_{w_{\min}})sx$$

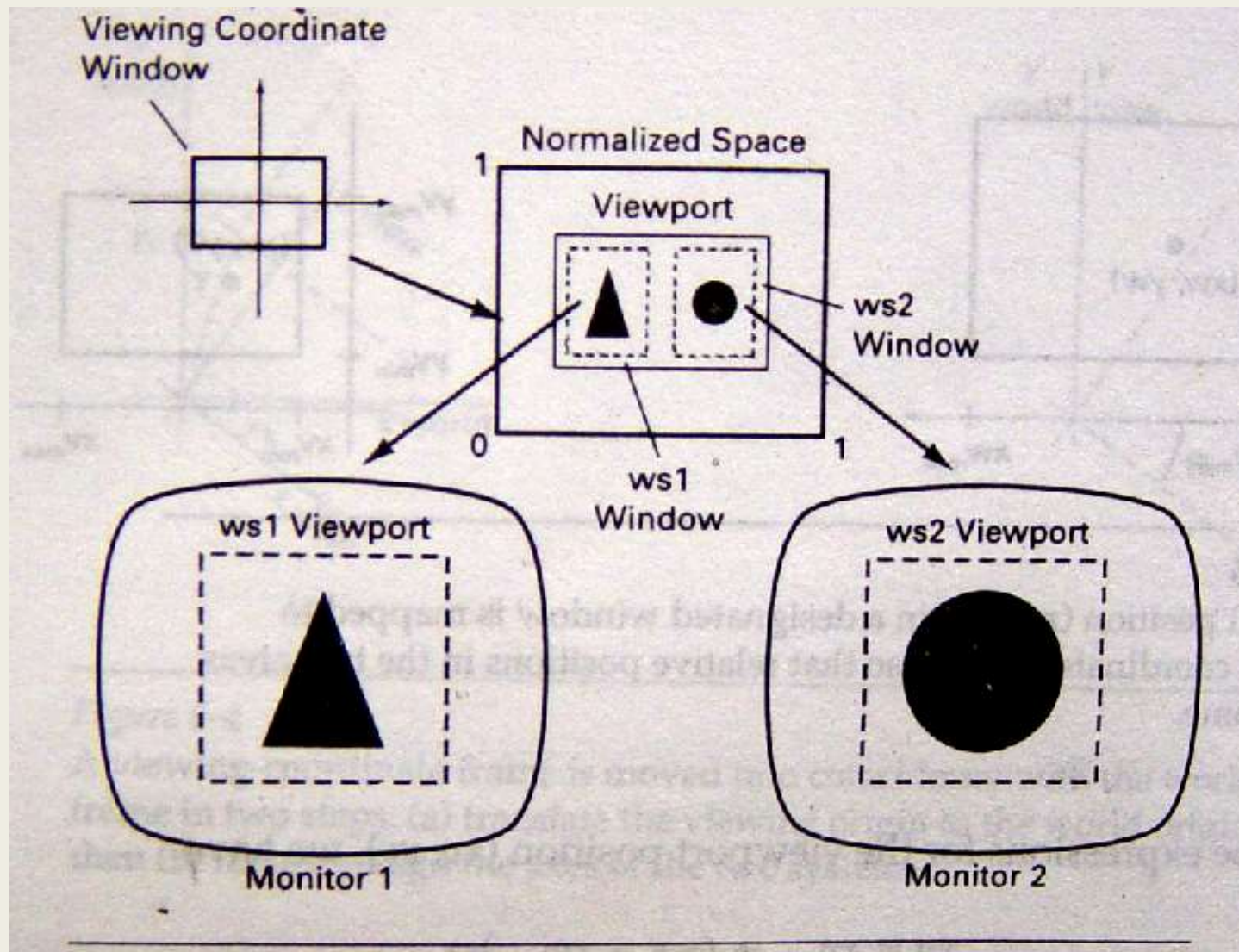
$$y_v = y_{v_{\min}} + (y_w - y_{w_{\min}})sy$$

$$sx = \frac{x_{v_{\max}} - x_{v_{\min}}}{x_{w_{\max}} - x_{w_{\min}}}$$

$$sy = \frac{y_{v_{\max}} - y_{v_{\min}}}{y_{w_{\max}} - y_{w_{\min}}}$$

A point at position (x_w, y_w) is mapped into position (x_v, y_v)

Workstation transformation



Workstation Transformaton

- From normalized coordinates , object description are mapped to various display devices.
- Any no of output devices can be used and window to viewport transformation can be performed for each open output device.
- This mapping called the **workstation transformation**.
- Window area in normalized space and viewport area in the coordinates of the display device.
- Controls the positioning of parts of a scene on individual output devices.

Clipping Operations

■ Clipping

- *Identify those portions of a picture that are either inside or outside of a specified region of space.*

■ Clip window

- *The region against which an object is to be clipped.*
- *The shape of clip window*

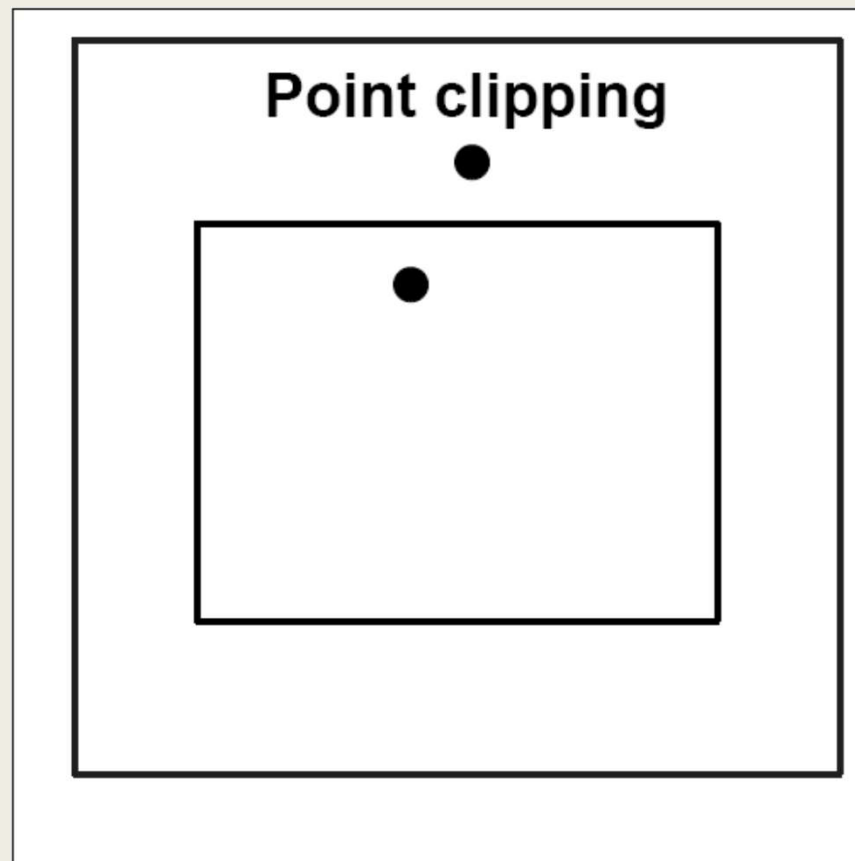
■ Applications of clipping :extracting part of the defined scene for viewing , identifying visible surfaces in 3d views etc.

■ World-coordinate clipping: Clipping algorithm can be applied to the world coordinate , so the contents of the window are mapped to device coordinates.

Clipping Operations

- Viewport clipping
 - *It can reduce calculations by allowing concatenation of viewing and geometric transformation matrices.*
- Types of clipping
 - *Point clipping*
 - *Line clipping*
 - *Area (Polygon) clipping*
 - *Curve clipping*
 - *Text clipping*
- Point clipping (Rectangular clip window)

Point clipping



Point clipping

- Is point (x,y) inside the clip window?
- Considering the clip window is a rectangular window.
- A point is inside if it satisfies the following inequalities are satisfied

- $XW_{win} \leq x \leq XW_{max}$

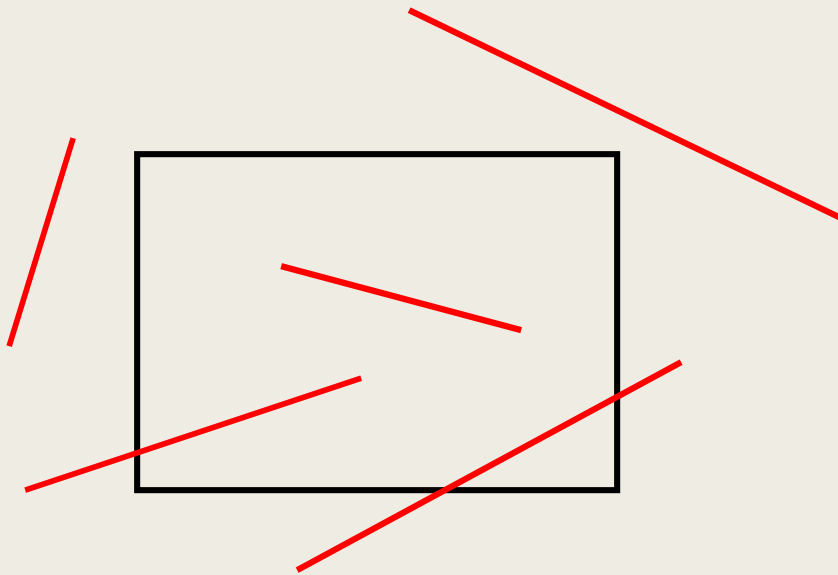
- $YW_{win} \leq y \leq YW_{max}$

where the edges of the clip window can be either world coordinate window boundaries or viewport boundaries

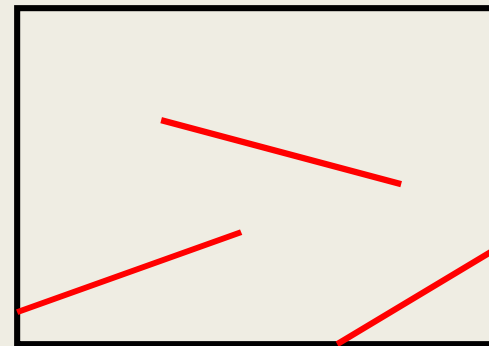
- If any of the inequalities are not satisfied the point is clipped.

Line Clipping

- Possible relationships between line positions and a standard rectangular clipping region



Before clipping



after clipping

Line Clipping

- Possible relationships
 - *Completely inside the clipping window*
 - *Completely outside the window*
 - *Partially inside the window*
- Parametric representation of a line segment with endpoints (x_1, y_1) and (x_2, y_2)
 - $$x = x_1 + u(x_2 - x_1)$$
 - $$y = y_1 + u(y_2 - y_1) \quad 0 \leq u \leq 1$$
- The value of u for an intersection with a rectangle boundary edge
 - *Outside the range 0 to 1, line does not enter the interior of window*
 - *Within the range from 0 to 1, the line segment crosses the clipping area.*