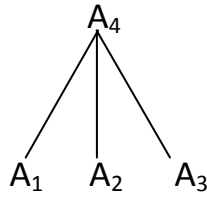


Sample calculation of the Methodology



Ref. value of:

$$A_1 \Rightarrow \text{H M L (3)}$$

$$A_2 \Rightarrow \text{H M L (3)}$$

$$A_3 \Rightarrow \text{H M L (3)}$$

Input for:

$$A_1 \Rightarrow 0.8;$$

Here ,

$$A_2 \Rightarrow 0.6;$$

$$\text{Total Rule} = (\text{Ref. value})^{\text{attribute no.}}$$

$$A_3 \Rightarrow 0.4.$$

$$= 3^3 = 27$$

Initial sub Rule base $A_y \Rightarrow \text{sheet (*)}$ [Sazzad ul vaqil]

Assume that,

All antecedent attributes (High, Medium, Low) in any rule have equal weight (Rule weight)

$$S_k^i = 1; \quad \text{for } k = 1, \dots, 27; 11$$

$$i = 1, 2, 3$$

Input transformation:

$$\text{Let For } H = 1.0; \quad M = 0.5; \quad L = 0.0$$

$h_{i3} = \text{High}$

$h_{i2} = \text{Medium}$

$h_{i1} = \text{Low}$

$$\text{If } h_{i3} \geq \sum i \geq h_{i2} \quad \text{Then } \alpha_{i2} = \frac{h_{i3} - \sum i}{h_{i3} - h_{i2}}$$

$\mathcal{E}_i = \text{Input value}$

$$\alpha_{i3} = (1 - \alpha_{i2})$$

$$\alpha_{i1} = 1 - (\alpha_{i2} + \alpha_{i3})$$

If $h_{i2} > \sum i \geq h_{i1}$ Then .

$$\alpha_{i1} = \frac{h_{i2} - \sum i}{h_{i2} - h_{i1}}$$

$$\alpha_{i2} = (1 - \alpha_{i1});$$

$$\alpha_{i3} = 1 - (\alpha_{i1} + \alpha_{i2})$$

Now, For $(\sum i)_{A_1} = 0.8$:

$$h_3 \geq 0.8 \geq h_2 ; \text{ Then } \alpha_{i2}(M) = \frac{1-0.8}{1-0.5} = \frac{0.2}{0.5} = 0.4$$

$$\alpha_{i3}(H) = (1 - 0.4) = 0.6$$

$$\alpha_{i1}(L) = 0.0$$

For $(\sum i)_{A_{12}} = 0.6$:

$h_{i3} \geq 0.6 \geq h_{i2} ;$ Then .

$$\alpha_{i2}(M) = \frac{1-0.6}{1-0.5} = \frac{0.4}{0.5} = 0.8$$

$$\alpha_{i3}(H) = (1 - 0.8) = 0.2$$

$$\alpha_{i1}(L) = 0.0$$

For $(\sum i)_{A_3} = 0.4$:

$h_{i2} \geq 0.4 \geq h_{i1} ;$ Then

$$\alpha_{i1}(L) = \frac{0.5-0.4}{0.5-0.5} = \frac{0.1}{0.5} = 0.2$$

$$\alpha_{i2}(M) = (1 - 0.2) = 0.8$$

$$\alpha_{i3}(H) = 0.0$$

Hence

Input for:

$$A_1 = \{(H, 0.6); (M, 0.4); (L, 0.0)\}$$

$$A_2 = \{(H, 0.2); (M, 0.8); (L, 0.0)\}$$

$$A_3 = \{(H, 0.0); (M, 0.8); (L, 0.2)\}$$

#Activation Weight:**Matching Degree:**

$$w_k = \frac{\theta_k \alpha_k}{\sum_{i=1}^k \theta_i \alpha_i}$$

$$\therefore \sum_{i=1}^k \theta_i \alpha_i = (\theta_1 \alpha_1 + \dots + \theta_{27} \alpha_{27})$$

$$\alpha_k = \frac{T_k}{\prod} (\alpha_i^k) \overline{\delta_{ki}}$$

$$\alpha_1 = (0.6)^1 * (0.2)^1 * (0.0)^1 = 0.0$$

$$w_1 = \frac{0.0}{1} = 0.0$$

$$\alpha_2 = (0.6)^1 * (0.2)^1 * (0.8)^1 = 0.096$$

$$w_2 = 0.096$$

$$\alpha_3 = (0.6)^1 * (0.2)^1 * (0.2)^1 = 0.024$$

$$w_3 = 0.024$$

$$\alpha_4 = (0.6)^1 * (0.8)^1 * (0.0)^1 = 0.0$$

$$w_4 = 0.0$$

$$\alpha_5 = (0.6)^1 * (0.8)^1 * (0.8)^1 = 0.384$$

$$w_5 = 0.384$$

$$\alpha_6 = (0.6)^1 * (0.8)^1 * (0.2)^1 = 0.096$$

$$w_6 = 0.0096$$

$$\alpha_7 = (0.6)^1 * (0.0)^1 * (0.0)^1 = 0.0$$

$$w_7 = 0.0$$

$$\alpha_8 = (0.6)^1 * (0.0)^1 * (0.8)^1 = 0.0$$

$$w_8 = 0.0$$

$$\alpha_9 = (0.6)^1 * (0.0)^1 * (0.2)^1 = 0.0$$

$$w_9 = 0.0$$

$$\alpha_{10} = (0.4)^1 * (0.2)^1 * (0.0)^1 = 0.0$$

$$w_{10} = 0.0$$

$$\alpha_{11} = (0.4)^1 * (0.2)^1 * (0.8)^1 = 0.064$$

$$w_{11} = 0.064$$

$$\alpha_{12} = (0.4)^1 * (0.2)^1 * (0.2)^1 = 0.016$$

$$w_{12} = 0.016$$

$$\alpha_{13} = (0.4)^1 * (0.8)^1 * (0.0)^1 = 0.0$$

$$w_{13} = 0.0$$

$$\alpha_{14} = (0.4)^1 * (0.8)^1 * (0.8)^1 = 0.256$$

$$w_{14} = 0.256$$

$$\alpha_{15} = (0.4)^1 * (0.8)^1 * (0.2)^1 = 0.064$$

$$w_{15} = 0.064$$

$$\alpha_{16} = (0.4)^1 * (0.0)^1 * (0.0)^1 = 0.0$$

$$w_{16} = 0.0$$

$$\alpha_{17} = (0.4)^1 * (0.0)^1 * (0.8)^1 = 0.0$$

$$w_{17} = 0.0$$

$$\alpha_{18} = (0.4)^1 * (0.0)^1 * (0.2)^1 = 0.0$$

$$w_{18} = 0.0$$

$$\alpha_{19} = (0.0)^1 * (0.2)^1 * (0.0)^1 = 0.0$$

$$w_{19} = 0.0$$

$$\alpha_{20} = (0.0)^1 * (0.2)^1 * (0.8)^1 = 0.0$$

$$w_{20} = 0.0$$

$$\alpha_{21} = (0.0)^1 * (0.2)^1 * (0.2)^1 = 0.0$$

$$w_{21} = 0.0$$

$$\alpha_{22} = (0.0)^1 * (0.8)^1 * (0.0)^1 = 0.0$$

$$w_{22} = 0.0$$

$$\alpha_{23} = (0.0)^1 * (0.8)^1 * (0.8)^1 = 0.0$$

$$w_{23} = 0.0$$

$$\alpha_{24} = (0.0)^1 * (0.8)^1 * (0.2)^1 = 0.0$$

$$w_{24} = 0.0$$

$$\alpha_{25} = (0.0)^1 * (0.0)^1 * (0.0)^1 = 0.0$$

$$w_{25} = 0.0$$

$$\alpha_{26} = (0.0)^1 * (0.0)^1 * (0.8)^1 = 0.0$$

$$w_{26} = 0.0$$

$$\alpha_{27} = (0.0)^1 * (0.0)^1 * (0.2)^1 = 0.0$$

$$w_{27} = 0.0$$

#Belief Degree weight Update:

$$\beta_{ik} = \bar{\beta}_{ik} \frac{\sum_{t=1}^{T_k} (\tau(t,k) \sum_{j=1}^{J_t} \alpha_{tj})}{\sum_{t=1}^{T_k} \tau(t,k)}$$

i= Attribute value k= Rule No

j= Referential Value

β_{ik} = Update Belief

u_t = Set of antecedent

$\tau(t,k) \begin{cases} 1; \text{if } u_t \text{ is used in defining } R_k (t = 1, \dots, T_u) \\ 0; \text{otherwise} \end{cases}$

$\bar{\beta}_{ik}$ = Original belief degree

$$\begin{aligned} \# \beta_{11} &= (\bar{\beta}_{11}) \frac{\sum_{t=1}^3 (\tau(t,k) \sum_{j=1}^{J_t} \alpha_{tj})}{\sum_{t=1}^3 \tau(t,k)} \\ &= 1 \times \frac{(1 \cdot \sum_{j=1}^3 \alpha_{1j})}{\tau(1,k) + \tau(2,k) + \tau(3,k)} \\ &= \frac{(\alpha_{11} + \alpha_{12} + \alpha_{13}) + (\alpha_{21} + \alpha_{22} + \alpha_{23}) + (\alpha_{31} + \alpha_{32} + \alpha_{33})}{1 + 1 + 1} \\ &= \frac{(0.6 + 0.4 + 0.0) + (0.2 + 0.8 + 0.0) + (0.0 + 0.8 + 0.2)}{3} \\ &= \frac{1 + 1 + 1}{3} \\ &= \frac{3}{3} \\ &= 1 \end{aligned}$$

Recursive Method/ Evedential Reasoning

#Aggregation:

	$D_1(M_{1+27})$	$D_2(M_{2+027})$	$D_2(M_{3,1+27})$	$M_D(M_{D,1+027})$
A_1	$M_{1,1} = 0.0$	$M_{2,10.0}$	$M_{3,10.0}$	$M_{4,11.0}$
	$M_{1,2} = 0.0768$	0.0192	0.0	0.940
A_2	$M_{1,3} = 0.0192$	0.0	0.0048	0.966
A_3	$M_{1,4} = 0.0$	0.0	0.0	1.0
A_4	$M_{1,5} = 0.15536$	0.2304	0.0	0.626
A_5	$M_{1,6} = 0.048$	0.0288	0.0192	0.904
A_6	$M_{1,7} = 0.0$	0.0	0.0	1.0
A_7	$M_{1,8} = 0.0$	0.0	0.0	1.0
A_8	$M_{1,9} = 0.0$	0.0	0.0	1.0
A_9	$M_{1,10} = 0.0$	0.0	0.0	1.0
A_{10}	$M_{1,11} = 0.0256$	0.0384	0.0	0.936
A_{11}	$M_{1,12} = 0.0008$	0.0048	0.0032	0.948
A_{12}	$M_{1,13} = 0.0$	0.0	0.0	1.0
A_{13}	$M_{1,14} = 0.0$	0.256	0.0	0.744
A_{14}	$M_{1,15} = 0.0$	0.0512	0.0128	0.936
	$M_{1,16} = 0.0$	0.0	0.0	1.01
	$M_{1,17} = 0.0$	0.0	0.0	1.0
	$M_{1,18} = 0.0$	0.0	0.0	1.0
	$M_{1,19} = 0.0$	0.0	0.0	1.0
	$M_{1,20} = 0.0$	0.0	0.0	1.0
	$M_{1,21} = 0.0$	0.0	0.0	1.0
	$M_{1,22} = 0.0$	0.0	0.0	1.0
	$M_{1,23} = 0.0$	0.0	0.0	1.0
	$M_{1,24} = 0.0$	0.0	0.0	1.0
	$M_{1,24} = 0.0$	0.0	0.0	1.0
	$M_{1,25} = 0.0$	0.0	0.0	1.0
	$M_{1,26} = 0.0$	0.0	0.0	1.0
	$M_{1,27} = 0.0$	0.0	0.0	1.0