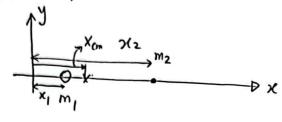
## "Center of Mass and Lineah Momentum"

Center of Mass ( mass - weighted mean)



$$\chi_{Cm} = \frac{m_1 \chi_1 + m_2 \chi_2}{m_1 + m_2}$$

For 2-number of printicles, 
$$x_{cm} = \frac{m_{j+1} m_{j} x_{1} + \cdots + m_{m}}{m_{j} + m_{j} + \cdots + m_{m}}$$

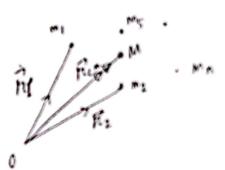
$$= \frac{1}{M} \iint_{i} m_{j} x_{i}$$

$$\vec{R}_{cm} = \chi_{cm} \hat{i} + y_{cm} \hat{j} + z_{cm} \hat{k}$$

$$= \frac{1}{M} \sum_{i} m_{i} \chi_{i} \hat{i} + \frac{1}{M} \sum_{i} m_{i} y_{i} \hat{j} + \frac{1}{M} \sum_{i} m_{i} z_{i} \hat{k}$$

$$= \frac{1}{M} \sum_{i} m_{i} (\chi_{i} \hat{i} + y_{i} \hat{j} + z_{i} \hat{k})$$

$$\vec{R}_{cm} = \frac{1}{M} \left[ i m_i \vec{n}_i \right]$$

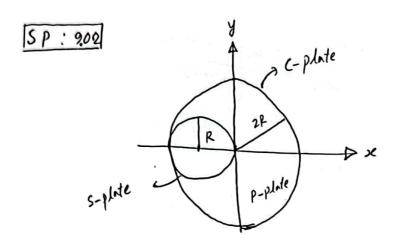


$$\vec{R}_{cm} = \frac{1}{M} \int \vec{R} dm$$

$$\chi_{cm} = \frac{1}{M} \int \chi dm, \quad y_{cm} = \frac{1}{M} \int \gamma dm, \quad z_{cm} = \frac{1}{M} \int \chi dm$$

elemity, 
$$s = \frac{dm}{dV} = \frac{M}{V} \Rightarrow dm = \frac{M}{V} dv$$

$$x_{\ell m} = \frac{1}{\nu} \int x dv$$
,  $y_{cm} = \frac{1}{\nu} \int y dv$ ,  $z_{cm} = \frac{1}{\nu} \int z dv$ 



$$x_{s+p} = \frac{m_s x_s + m_p x_p}{m_s + m_p} \qquad ----(1)$$

$$x_{S+P} = 0$$

$$x_s = -R$$

From eqn. (1),
$$0 = \frac{m_S x_S + m_p x_p}{m_S + m_p}$$

$$= m_5 x_p + m_p x_p = 0$$

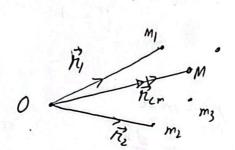
$$=) \quad \chi_{\rho} = -\frac{m_{s}}{m\rho} \chi_{s}$$

$$= -\frac{m_{s}}{m\rho} (-\rho)$$

$$= \frac{m_s}{mp} R$$

$$\frac{m_s}{m_p} = \frac{g_s V_s}{g_p V_p} = \frac{g_s (Area)_s}{g_s (Area)_p} + \frac{g_s (Area)_s}{f_s (Area)_p} = \frac{\pi R^2}{\pi g_s^2 - \pi R^2} = \frac{\pi R^2}{3\pi R^2} = \frac{\pi R^2}{3\pi R^2}$$

$$2. \sqrt{\chi_{p}} = \frac{1}{3} R$$



$$\vec{R}_{cm} = \frac{1}{M} \underbrace{\vec{\xi}_{m_1} \vec{R}_{i}}_{i}$$

$$\Rightarrow M \vec{R}_{cm} = \underbrace{\vec{\xi}_{m_1} \vec{R}_{i}}_{i} = m_1 \vec{R}_1 + m_2 \vec{R}_2 + \dots + m_n \vec{R}_n$$

$$\int_{aking} \frac{d}{dt}$$

$$\Rightarrow M \frac{d\vec{R}_{cm}}{dt} = m_1 \frac{d\vec{R}_i}{dt} + m_2 \frac{d}{dt} \vec{R}_2 + \dots + m_n \frac{d}{dt} \vec{R}_n$$

$$\Rightarrow M \vec{V}_{cm} = m_1 \vec{V}_1 + m_2 \vec{V}_2 + \dots + m_n \vec{V}_n$$

$$\int_{aking} \frac{d}{dt}$$

$$\Rightarrow M \vec{Q}_{cm} = m_1 \vec{Q}_1 + m_2 \vec{Q}_2 + \dots + m_n \vec{Q}_n$$

$$\Rightarrow M \vec{Q}_{cm} = m_1 \vec{Q}_1 + m_2 \vec{Q}_2 + \dots + m_n \vec{Q}_n$$

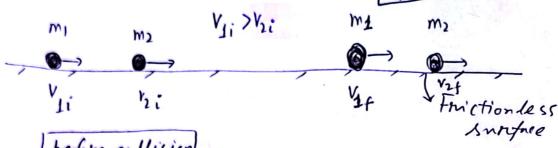
$$\Rightarrow M \vec{Q}_{cm} = \vec{R}_1 + \vec{R}_2 + \dots + m_n \vec{Q}_n$$

$$\Rightarrow M \vec{Q}_{cm} = \vec{R}_1 + \vec{R}_2 + \dots + m_n \vec{Q}_n$$

Linear momentum; P = mV Linear momentum of a particle, where m = mass of the particle V = relouty of the particle Newton's 2nd Law, F = m à  $= m \frac{d\vec{v}}{dt}$ 一点的功  $\vec{F}_{he+} = \frac{d}{dt}(\vec{P})$ If  $\vec{F}_{Net} = 0$ ,  $\vec{p} = constant$ . So, Pi = Pf (conservation of Linear momentum) Lineur momentum for a system of Particles,  $\vec{P}_{cm} = \vec{P}_1 + \vec{P}_2 + \cdots + \vec{P}_n$ Newton's 2nd Law.  $\vec{F}_{ret} = \frac{d}{dt}(\vec{P}_{cm})$ If  $\vec{P}_{\text{ret}} = 0$ ;  $\vec{P}_{\text{cm}} = \text{comfant}$  $= > \vec{P}_1 + \vec{P}_2 + \cdots + \vec{P}_n = Combant$  $\vec{P}_{cm_i} = \vec{P}_{cm_f}$   $\vec{P}_{1i} + \vec{P}_{2i} + \cdots + \vec{P}_{ni} = \vec{P}_{1f} + \vec{P}_{2f} + \cdots + \vec{P}_{nf}$ 

Consenvation of Linear Momentum for a system of particles 10

after collision



before collision

According to conservation of Linear momentum.

$$\vec{P}_{i} = \vec{P}_{f}$$

$$\Rightarrow \vec{P}_{ii} + \vec{P}_{2i} = \vec{P}_{if} + \vec{P}_{2f}$$

$$=> P_{1i} + P_{2i} = P_{1f} + P_{2f}$$

$$| m_1 V_{1i} + m_2 V_{2i} | = m_1 V_{1f} + m_2 V_{2f}$$

For elastic Collision, Kii + Kzi = Kif + K1f =)  $\frac{1}{2} m_1 V_{11}^2 + \frac{1}{2} m_2 V_{21}^2 = \frac{1}{2} m_1 V_{1f}^2 + \frac{1}{2} m_2 V_{2f}^2$ 

20

V11 > 121

Before collision velocity of m, and m2 one v, and v2; hespectively After collision relocity of m, and m, are Vit and Vit respectively

According to Conservation of Linear Momentum.

$$\vec{P}_{i} = \vec{P}_{f}$$

$$=) \vec{P}_{1i} + \vec{P}_{2i} = \vec{P}_{f} + \vec{P}_{2f}$$

$$=) \vec{P}_{1i} + \vec{P}_{2i} = \vec{P}_{f} + \vec{P}_{2f}$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2}$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2}$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \sin \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \sin \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \sin \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \sin \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \sin \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1f} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{1i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

$$= P_{1i} + P_{2i} = P_{2i} \cos \theta_{1} + P_{2f} \cos \theta_{2} - \cdots (2)$$

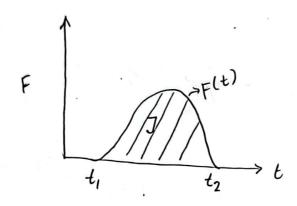
$$= P_{1i} + P_{2i} = P_{2i} \cos \theta_{1} + P_{2i} \cos \theta_{2} - \cdots (2)$$

$$= P_{2i} + P_{2i} \cos \theta_{1} + P_{$$

For elastic Collision,

## Impulse: (Change of the momentum)

Impulsive Fonce Large amount of Force in infinitesimal time

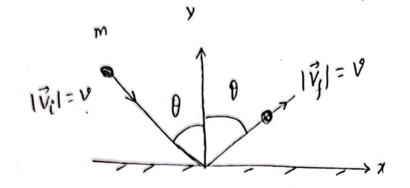


Impulse, 
$$\vec{j} = \int_{t_1}^{t_2} \vec{f} dt$$

$$\Rightarrow \int_{\vec{P}_i}^{\vec{P}_f} d\vec{P} = \int_{t_i}^{t_i} \vec{F} dt$$

$$\Rightarrow |\vec{p}_f - \vec{p}_i| = \vec{j}$$

9mpnuse, 
$$\vec{j} = \vec{j} + \vec{k} + \vec{k}$$



\* 9 mpulse 
$$\vec{j} = \Delta \vec{p} = \vec{P_f} - \vec{P_i} = \vec{P_f} + (-\vec{P_i})$$

$$\vec{P}_{f} = |\vec{P}_{f}| \cos(90-\theta) \hat{i} + |\vec{P}_{f}| \sin(90-\theta) \hat{j}$$

$$= m v \sin \theta \hat{i} + m v \cos \theta \hat{j}$$

$$(-\vec{p}_i) = |-\vec{p}_i| \cos(9\vec{i} + \theta) \hat{i} + |-\vec{p}_i| \sin(9\vec{i} + \theta) \hat{j}$$

$$= -mv \sin\theta \hat{i} + mv \cos\theta \hat{j}$$

9mpn/se, 
$$\vec{j} = \vec{P}_{j} + (\vec{P}_{i})$$

$$= (mv \sin \theta \ \hat{i} + mv \cos \theta \ \hat{j}) + (-mv \sin \theta \ \hat{i} + mv \cos \theta \ \hat{j})$$

$$\vec{j} = 2mv \cos \theta \ \hat{j}$$

## Chapten-9

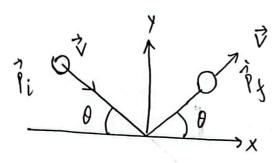
$$\begin{array}{lll}
 & M_1 = 3 \, kg \\
 & M_2 = 4 \, kg \\
 & M_3 = 8 \, kg \\
 & M_1 = 0 \, m, \quad y_1 = 0 \, m \\
 & M_2 = 2 \, m, \quad y_2 = 1 \, m \\
 & M_3 = 1 \, m, \quad y_3 = 2 \, m
\end{array}$$

(a) Center of mass, 
$$\chi_{cm} = \frac{m_1 \chi_1 + m_2 \chi_2 + m_3 \chi_3}{m_1 + m_2 + m_3}$$

$$= (\frac{3 \times 0 + 4 \times 2 + 8 \times 4}{3 + 4 + 8}) m$$

(b) 
$$and, y_{1} = \frac{m_{1}y_{1} + m_{2}y_{2} + m_{3}y_{3}}{m_{1} + m_{1} + m_{3}}$$

$$= \left(\frac{3 \times 0 + 4 \times 1 + 8 \times 2}{3 + 4 + 8}\right) m_{1}$$



 $m = 3009 = \frac{3 \times 10^{-3} \text{ kg}}{300 \times 10^{-3} \text{ kg}} = 0.3 \text{ kg} = 3 \times 10^{-1} \text{ kg}$ 

$$= \frac{3\times10^{-1} \times 6\times 0.033}{5.2i} - 3.0i] \times 3ms^{-1}$$

(3)

9m pn/se, 
$$\vec{j} = P_{\vec{i}} - P_{\vec{i}}$$

$$= 3x/0^{-1} \left[ 5.2 \hat{i} + 3.0 \hat{j} - 5.2 \hat{i} + 3.0 \hat{j} \right] kgms^{-1}$$

$$= (3 x/0^{-1} x 6) \hat{j} kgms^{-1}$$

$$= (1.8 Ns) \hat{j}$$

(b) Avenage For 1e on the ball,
$$\vec{f} = \frac{\vec{J}}{\Delta t}$$

$$= \frac{(1.8 \text{ Ns}) \hat{J}}{10 \times 10^{-3} \text{ s}}$$

$$= 180 \text{ N} \hat{J}$$

Average Fonce on the wall (- 180 Nj)

y = 3 000 L= 2000/2

$$m_1 = 2ky$$

$$m_2 = 1ky$$

$$v_1 = 4m/s$$

$$v_2 = 0m/s$$

According to consentation of Linear momentum,

$$m_{1}V_{1} + m_{2}V_{2} = [m_{1} + m_{2})V$$

$$= > (2x 4 + 1x0) = (2+1)V$$

$$= > \frac{2x4}{2+1} m/s$$

$$= 2.7 m/s$$

According to confrontion of sungy,

$$\frac{1}{2}(m_1+m_2) V^2 = -\frac{1}{2} L N^2$$

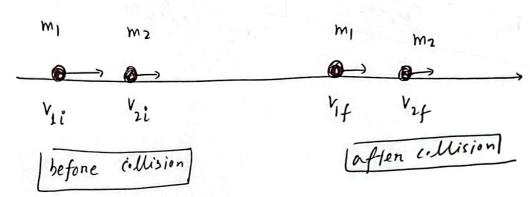
$$= \sqrt{\frac{m_1+m_2}{K}} V$$

$$= \sqrt{\frac{3}{200}} (2.7) M$$

$$= \sqrt{0.33} M$$

Note: For problem 68 and 70

3



According to Consentation of Linear momentum,

$$\vec{P}_i = \vec{P}_f$$

$$=) \vec{P}_{1i} + \vec{P}_{2i} = \vec{P}_{1f} + \vec{P}_{2f}$$

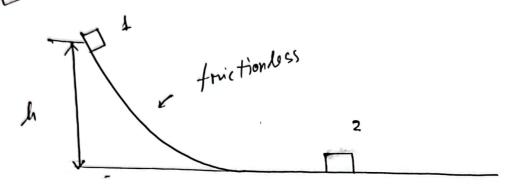
=) 
$$m_1 V_{1i} + m_2 V_{2i} = m_1 V_{1f} + m_2 V_{2f}$$
 (1)

# For completely in elastic collision, (panticle will stick

tigether). Let Then,

$$V_{1f} = \frac{m_1 - m_2}{m_1 + m_2} V_{1i} + \frac{2 m_2}{m_1 + m_2} V_{2i}$$

$$V_{2f} = \frac{2 m_1}{m_1 + m_2} V_{1i} + \frac{m_2 - m_1}{m_1 + m_2} V_{2i}$$



$$m_1gh = \frac{1}{2}m_1v_1^2$$

=> 
$$V_{1i} = \sqrt{29h}$$
  
=  $\sqrt{2\times9.8\times2.5}$  m/s

$$V_{2f} = \frac{2m_1}{m_1 + m_2} V_{1i} + \frac{m_2 - m_1}{m_1 + m_2} V_{2i}$$

$$V_{2i} = \frac{2m_{1}}{V_{2i}} = \frac{2m_{1}}{m_{1} + 2m_{1}} V_{1i} + \frac{2m_{1} - m_{1}}{m_{1} + 2m_{1}} \times D$$

$$= \frac{2}{3} \times \sqrt{2 \times 9.8 \times 2.5} m/s$$

V11 = 1229.507.5

$$= \frac{y_{2f}^{2}}{2 \times M_{K} g} = \frac{\left(\frac{2}{3} \times \sqrt{2 \times 9.8 \times 2.5}\right)^{2}}{2 \times 0.5 \times 9.8}$$

$$= 2.2 \text{ M} \text{ Am}.$$

$$m_1 V_{1i} + m_2 V_{2i} = (m_1 + m_2) V$$

$$= \frac{m_1 V_{1i} + m_2 V_{2i}}{m_{1} + m_2}$$

$$= \frac{m_1}{3 m_1} \times \sqrt{2 \times 9 \cdot 8 \times 2 \cdot 5} m_5$$

$$=\frac{m_1}{3 m_1} \times \sqrt{229.852.5} m/s$$

$$=\frac{\sqrt{2\times9.8\times7.5}}{3}$$
 m/s

$$=) \frac{1}{2} (m_1 + m_2) v^2 = M_K (m_1 + m_3) \int_{V_1}^{2} dv$$

$$= \frac{1}{2} (m_1 + m_2) v^2 = M_K (m_1 + m_2) \int_{0}^{2} \frac{1}{2x \cdot 9 \cdot 8 \times 1.5}$$

$$= \frac{1}{2} (m_1 + m_2) v^2 = \frac{1}{2x \cdot 9 \cdot 8 \times 1.5}$$

$$= \frac{1}{2x \cdot 9 \cdot 8 \times 1.5}$$

$$= \frac{1}{2x \cdot 9 \cdot 8 \times 1.5}$$

$$= \frac{1}{2x \cdot 9 \cdot 8 \times 1.5}$$

$$V_{ij} = \frac{m_{i} - m_{i}}{m_{i} + m_{i}} V_{ii} + \frac{2m_{i}}{m_{i} + m_{i}} V_{ii} - (2)$$

$$V_{ij} = \frac{2m_{i}}{m_{j} + m_{i}} V_{ii} + \frac{m_{i} - m_{i}}{m_{j} + m_{i}} V_{ii} - (2)$$

$$V_{ii} = 0 m/s$$

$$M_{ij} = 0.7 M_{ij}$$

$$+ V_{1f} = -\left(\frac{m_{1}-m_{2}}{m_{1}+m_{2}} V_{1i}\right)$$

$$V_{2f} = \frac{2m_1}{m_1+m_2} V_{1i}$$

$$\begin{array}{c} 1 \\ 2 \\ 2 \\ d \end{array}$$

$$(3) \div (4) = ) \frac{2d}{d} = \frac{V_{1}f}{V_{2}f} \frac{4f}{4f}$$

$$= \frac{-\left(\frac{m_{1}-m_{2}}{m_{1}+m_{2}}\right)V_{1}^{\prime}}{\left(\frac{2m_{1}}{m_{1}+m_{2}}\right)V_{1}^{\prime}}$$

$$= \frac{m_2 - m_1}{m_1 + m_2} \times \left(\frac{m_1 + m_2}{2 m_1}\right) = \frac{m_2 - m_1}{2 m_1}$$

$$4 m_{1} = m_{2} - m_{1} = 0 \quad 5 m_{1} = m_{2}$$

$$= 0 \quad m_{2} = 5 \times 0.2 \times 9$$

$$= 1 \times 9$$

$$V_{1} = 100 \text{ m/s}$$

$$V_{2} = 500 \text{ m/s}$$

$$V_{2} = 500 \text{ m/s}$$

$$V_{3} = 7$$

$$V_{3} = 7$$

$$V_{4} = 100 \text{ m/s}$$

$$V_{4} = 100 \text{ m/s}$$

$$V_{4} = 100 \text{ m/s}$$

$$V_{3} = 7$$

(a) A cconding to Conservation of Linear momentum,
$$\vec{P}_1 = \vec{P}_f \Rightarrow \vec{P} = \vec{P}_{2f} + \vec{P}_{2f} + \vec{P}_{3f}$$

$$\Rightarrow M\vec{V}_0 = m_1 \vec{V}_1 + m_2 \vec{V}_2 + m_3 \vec{V}_3$$

$$\Rightarrow M(V_0 \hat{i}) = m_1 (V_1 \hat{j}) + m_2 (V_2 (-\hat{i})) + m_3 \vec{V}_3$$

$$\Rightarrow 20 \times 200 \hat{i} = 10 \times 100 \hat{j} - 4 \times 500 \hat{i} + 6 \vec{V}_3$$

$$\Rightarrow 4000 \hat{i} - 1000 \hat{j} + 2000 \hat{i} = 6 \vec{V}_3$$

$$\Rightarrow 6 \vec{V}_3 = 6000 \hat{i} - 1000 \hat{j}$$

$$\Rightarrow \vec{V}_3 = \left[\frac{6000}{6} \hat{i} - \frac{1000}{6} \hat{j}\right] m/s$$

$$\vec{V}_3 = (10^3 \hat{i} - 0/1(7 \times 10^3 \hat{j})) m/s$$
Magnitude, 
$$|\vec{V}_3| = \sqrt{(10^3)^2 + (-0.167 \times 10^3)^2} = \sqrt{(101 \times 10^3 m/s)}$$
Angle  $\theta = \tan^{-1} \left(\frac{-0.167 \times 10^3}{10^3}\right) = \sqrt{-9.48^2}$ 

$$\Delta k = k_f - k_1^{\circ} = \frac{1}{2} M V_0^2 - \frac{1}{2} m_1 k_1^2 - \frac{1}{2} m_2 k_2^2 - \frac{1}{2} m_3 k_3^2$$

$$= \left[\frac{1}{2} \times 20.0 \times 200^{2} - \frac{1}{2} \times 10 \times 100^{2} - \frac{1}{2} \times 4 \times 500^{2} - \frac{1}{2} 6 \times (1.01 \times 10^{3})^{2}\right]$$

(a) 
$$v_{Af} = ?$$

According to Conservation of Linear momentum,

$$\vec{P}_{l} = \vec{P}_{f}$$

$$\vec{P}_{i} = \vec{P}_{f}$$

$$=) \vec{P}_{Ai} + \vec{P}_{Bi} = \vec{P}_{Af} + \vec{P}_{Bf}$$

$$=) V_{Af} = \frac{m_A V_{Ai} + m_B V_{Bi} - m_B V_{Bf}}{m_A}$$

$$= \frac{1.6x5.5 + 2.4 \times 2.5 - .24 \times 4.9}{1.6}$$

- (b) Direction of the valuity, VAf is from left to right.
- Before GMision, Kinetic Energy,  $K_{i} = \frac{1}{2} m_{A} V_{A i}^{2} + \frac{1}{2} m_{B} V_{B i}^{2}$   $= \left[\frac{1}{2} \times 1.6 \times 5.5^{2} + \frac{1}{2} \times 2.4 \times (2.5)^{2}\right] \times \left[\frac{1.7}{2} \times 1.7 \times 5.5^{2} + \frac{1}{2} \times 2.4 \times (2.5)^{2}\right] \times \left[\frac{1.7}{2} \times 1.7 \times 5.5^{2} + \frac{1}{2} \times 2.4 \times (2.5)^{2}\right] \times \left[\frac{1.7}{2} \times 1.7 \times 5.5^{2} + \frac{1}{2} \times 2.4 \times (2.5)^{2}\right]$

After collision, kinetic Energy

$$k_{f} = \frac{1}{2} m_{A} k_{Af}^{2} + \frac{1}{2} m_{B} k_{Af}^{2}$$

$$= \left[\frac{1}{2} \times 1.6 \times (1.9)^{2} + \frac{1}{2} \times 2.4 \times (4.9)^{2}\right]$$

$$= \left[\frac{31.73}{1.73}\right]$$

ki = ki so, the collision is elestic.

 $V_{Ai} = V$   $V_{Ai} = V$   $V_{Bi} = V$   $V_{Bf} = \frac{1}{2}$ 

Applying Conservation of Linear momentum along x-ands.

Applying consensation of Linear momentum along y-amis,

$$=) m_g \frac{V}{2} = m_A r_{af} \sin D - (2)$$

(2) 
$$\div$$
 (1)  $\tan \theta = \frac{1}{2}$ 

$$= \frac{1}{27} \left(\frac{1}{2}\right)$$

$$= \frac{1}{27} \left(\frac{1}{2}\right)$$

Patting Hene, From equation (1) and (2), ma, ma and Vaf are unknown. So, We can't solve these two equations. That's why we can't find Vaf. Am

$$M_{A} = 2 + 9$$
 $V_{A_{i}} = (15 i + 30 j) m/s$ 
 $m_{B_{i}} = 2 + 89$ 
 $V_{B_{i}} = (-10 i + 5 j) m/s$ 

$$V_{A} = (-10 \ i + 5)) \text{ m/s}$$
 $V_{A}' = (-5 \hat{i} + 20 \hat{j}) \text{ m/s}$ ;  $V_{B}' = )$ 

$$(*)$$

According to consummation of Linear momentum,

$$m_A \vec{v}_A + m_S \vec{v}_S = m_A \vec{v}_A' + m_S \vec{v}_B'$$

$$\vec{v}_A = m_B \vec{v}_A = m_B \vec$$

$$\vec{V}_A + \vec{V}_S = \vec{V}_A' + \vec{V}_S'$$

$$= \overrightarrow{V}_{A} + \overrightarrow{V}_{A} - \overrightarrow{V}_{A}'$$

$$= [(15\hat{i} + 30\hat{j}) + (-10\hat{i} + 5\hat{j}) - (-5\hat{i} + 20\hat{j})] m/s$$

$$= [(15-10+5)\hat{i} + (30+5-29)\hat{j}] m/s$$

(b) gritial kinetic Every,

$$k_i = \frac{1}{2} m_A \vec{V}_A^2 + \frac{1}{2} m_B \vec{V}_B^2$$

$$= \left[ \frac{1}{5} \times 2 \times \left( \frac{15^2 + 30^2}{5^2} \right) + \frac{1}{5} \times 2 \times \left( \frac{10}{5} + \frac{5^2}{5^2} \right) \right]$$

$$= \left[ \frac{1}{5} \times 2 \times \left( \frac{15^2 + 30^2}{5^2} \right) + \frac{1}{5} \times 2 \times \left( \frac{10}{5} + \frac{5^2}{5^2} \right) \right]$$

$$= \left[\frac{1}{2} \times 2 \times \left( (-5)^{2} + (20)^{2} \right) + \frac{1}{2} \times 2 \times \left[ 10^{2} + 15^{2} \right] \right]$$

Change of the kinetic queryy,  $\Delta k = k_f - k_i'$   $= (8x10^2 - 1.3x10^3) T$   $= [-5x10^2]$