

# MATH110 ASSIGNMENT-02

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SECTION:09

SET:C

1.1st derivative:

$$f'(x) = \frac{1}{2\sqrt{x-1}}$$

2nd derivative:

$$f''(x) = \frac{1}{2} \cdot -\frac{1}{2}(x-1)^{-\frac{1}{2}-1}$$

$$= -\frac{1}{4}(x-1)^{-\frac{3}{2}}(\text{Ans})$$

$$\mathbf{2(a)} \cdot \frac{d}{dx}[\ln(\sin x - \cot x)]$$

$$= \frac{d}{d(\sin x - \cot x)}[\ln(\sin x - \cot x)] \cdot \frac{d}{dx}(\sin x - \cot x)$$

$$= \frac{\cos x + \operatorname{cosec}^2 x}{\sin x - \cot x}(\text{Ans})$$

$$\mathbf{2(b)} \cdot \frac{d}{dz} [\tan^4(z^2 + 1)]$$

$$= \frac{d}{d(\tan(z^2 + 1))} \cdot [\tan^4(z^2 + 1)] \cdot \frac{d}{d(z^2 + 1)} \cdot [\tan(z^2 + 1)] \cdot \frac{d}{dz} \cdot (z^2 + 1)$$

$$= 4\tan^3(z^2 + 1) \cdot \sec^2(z^2 + 1) \cdot 2z$$

$$= 8z\tan^3(z^2 + 1) \cdot \sec^2(z^2 + 1) (\text{Ans})$$

**3.** As,

$$y = \ln \frac{1}{x}$$

$$\text{if } x = 1; y = \ln \frac{1}{1}$$

so,

$$x = 1; y = 0$$

The slope will be

$$\frac{d}{dx} \left( \ln \frac{1}{x} \right)$$

$$= \frac{1}{x^{-1}} \cdot (-1)(x^{-2})$$

$$= -\frac{1}{x}$$

$$= -\frac{1}{1} \text{ [at } x=1]$$

$$= -1$$

so the slope will be  $m=-1$  [when  $x=1$ ]

so the equation of tangent line:

$$y - 0 = -1(x - 1) \text{ [x= 1 ; y= 0 ; m=-1]}$$

$$y = -x + 1 \text{ (Ans)}$$

4.1st derivative:

$$f'(x) = -\sin(\ln x) \cdot \frac{1}{x}$$

$$f'(x) = -\frac{\sin(\ln x)}{x} (\text{Ans})$$

### BONUS QUESTIONS

5(a) The derivative of even function is an odd function:

we know even function is  $f(-x) = f(x)$

so the derivative of both side

$$\frac{d}{d(x)} f(-x) = \frac{d}{dx} f(x)$$

$$\frac{d}{d(x)} f(-x) \cdot \frac{d}{d(x)} (-x) = \frac{d}{dx} f(x)$$

$$\text{or, } f'(-x) \cdot (-1) = f'(x)$$

$$\text{or, } f'(-x) = -f'(x)$$

$f'(-x) = -f'(x)$  is a odd function(Proved)

**5(b)**The derivative of odd function is an even function:

we know even function is  $f(-x) = -f(x)$

so the derivative of both side

$$\frac{d}{d(x)}f(-x) = \frac{d}{dx} - f(x)$$

$$\frac{d}{d(x)}f(-x) \cdot \frac{d}{d(x)}(-x) = \frac{d}{dx}(-f(x))$$

$$\text{or, } f'(-x) \cdot (-1) = -f'(x)$$

$$\text{or, } f'(-x) = f'(x)$$

$f'(-x) = f'(x)$  is a even function(Proved)

6. Find the first and second derivative of the following function with respect to b

$$\cos \left( \frac{r}{2} \left[ \frac{b^4}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

$$\cos \left( (b^4)^{\frac{1}{4}} \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

$$\cos \left( b \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

1st derivative:

$$= -\sin \left( b \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right) \cdot \left( b^{1-1} \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

$$= -\sin \left( b \cdot \frac{r}{2} \left[ \frac{b^4}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right) \cdot \left( \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

2nd derivative:

$$= -\cos \left( b \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right) \cdot \left( b^{1-1} \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right) \\ \cdot \left( \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)$$

$$= -\cos \left( b \cdot \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right) \cdot \left( \frac{r}{2} \left[ \frac{1}{4} \left( 1 - \frac{2\sinh^2(8\pi l_s Q)}{\sinh^2(9\pi l_s Q)} \right) \right]^{\frac{1}{4}} \right)^2 \text{ (Ans)}$$