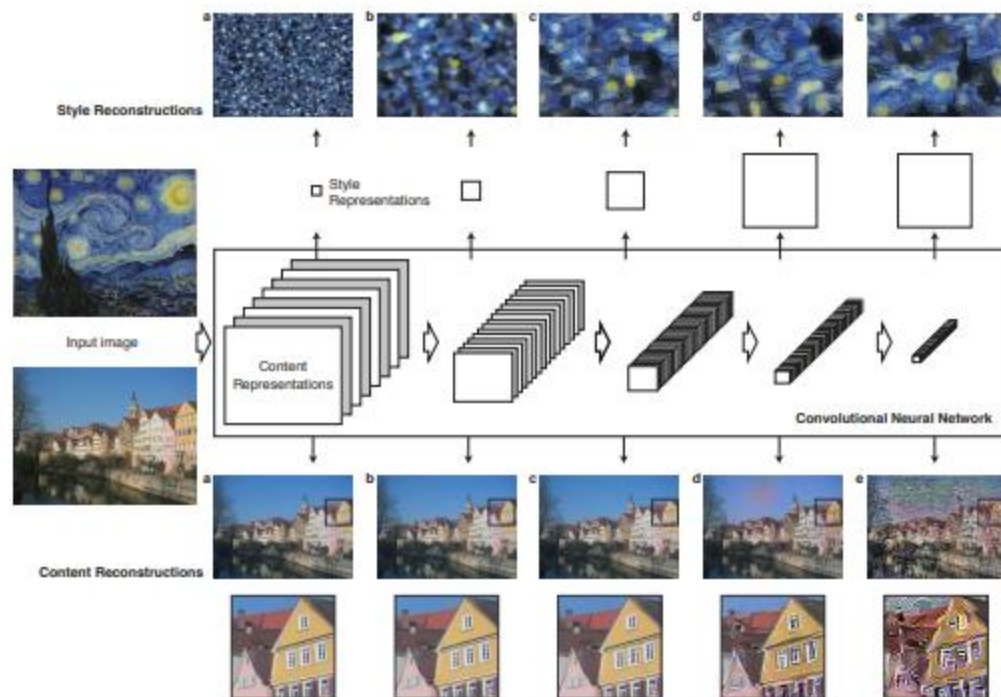


# Style Transfer

By Wei Gao

# Optimization Method

## Image Style Transfer Using Convolutional Neural Networks



$$G_{ij}^l = \sum_k F_{ik}^l F_{jk}^l.$$

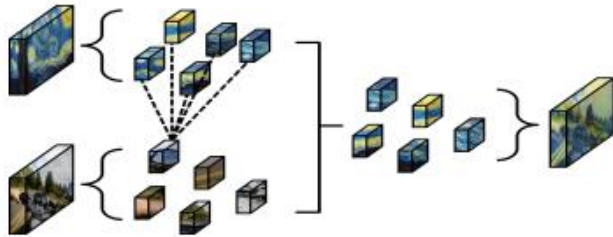
$$E_l = \frac{1}{4N_l^2 M_l^2} \sum_{i,j} (G_{ij}^l - A_{ij}^l)^2$$

# Swap Method

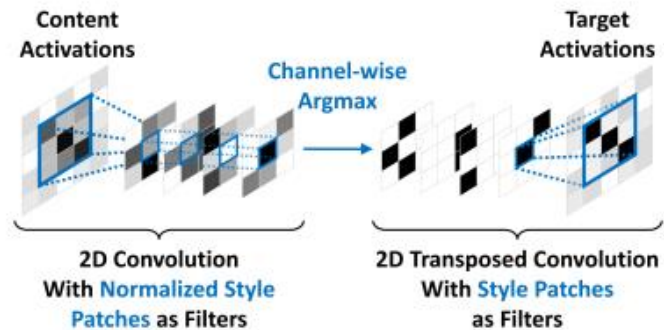
## Fast Patch-based Style Transfer of Arbitrary Style

For every content patch, **swap** it with the **best matching** style patch, which we define using the normalized cross-correlation:

$$\text{BestMatch}(c) = \arg \max_{s \in S} \frac{\langle c, s \rangle}{\|c\| \cdot \|s\|}$$



This operation can be **implemented efficiently** using a 2D convolutional layer and a 2D transposed convolutional layer.



# Learning Method

## Arbitrary Style Transfer in Real-time with Adaptive Instance Normalization

Replacing BN layers with IN layers:

$$\text{IN}(x) = \gamma \left( \frac{x - \mu(x)}{\sigma(x)} \right) + \beta$$

$$\text{AdaIN}(x, y) = \sigma(y) \left( \frac{x - \mu(x)}{\sigma(x)} \right) + \mu(y) \quad (8)$$

Replacing BN layers with CIN layers:

$$\text{CIN}(x; s) = \gamma^s \left( \frac{x - \mu(x)}{\sigma(x)} \right) + \beta^s \quad (7)$$

# Learning Method

Perceptual Losses for Real-Time Style Transfer and Super-Resolution

$$\ell_{feat}^{\phi,j}(\hat{y}, y) = \frac{1}{C_j H_j W_j} \|\phi_j(\hat{y}) - \phi_j(y)\|_2^2$$

$$G_j^{\phi}(\mathbf{x})_{c,c'} = \frac{1}{C_j H_j W_j} \sum_{h=1}^{H_j} \sum_{w=1}^{W_j} \phi_j(\mathbf{x})_{h,w,c} \phi_j(\mathbf{x})_{h,w,c'}.$$

# Zero-Shot Method

## Universal Style Transfer via Feature Transforms

**Whitening transform.** Before whitening, we first center  $f_c$  by subtracting its mean vector  $m_c$ . Then we transform  $f_c$  linearly as in (2) so that we obtain  $\hat{f}_c$  such that the feature maps are uncorrelated ( $\hat{f}_c \hat{f}_c^\top = I$ ),

$$\hat{f}_c = E_c D_c^{-\frac{1}{2}} E_c^\top f_c, \quad (2)$$

where  $D_c$  is a diagonal matrix with the eigenvalues of the covariance matrix  $f_c f_c^\top \in \mathbb{R}^{C \times C}$ , and  $E_c$  is the corresponding orthogonal matrix of eigenvectors, satisfying  $f_c f_c^\top = E_c D_c E_c^\top$ .

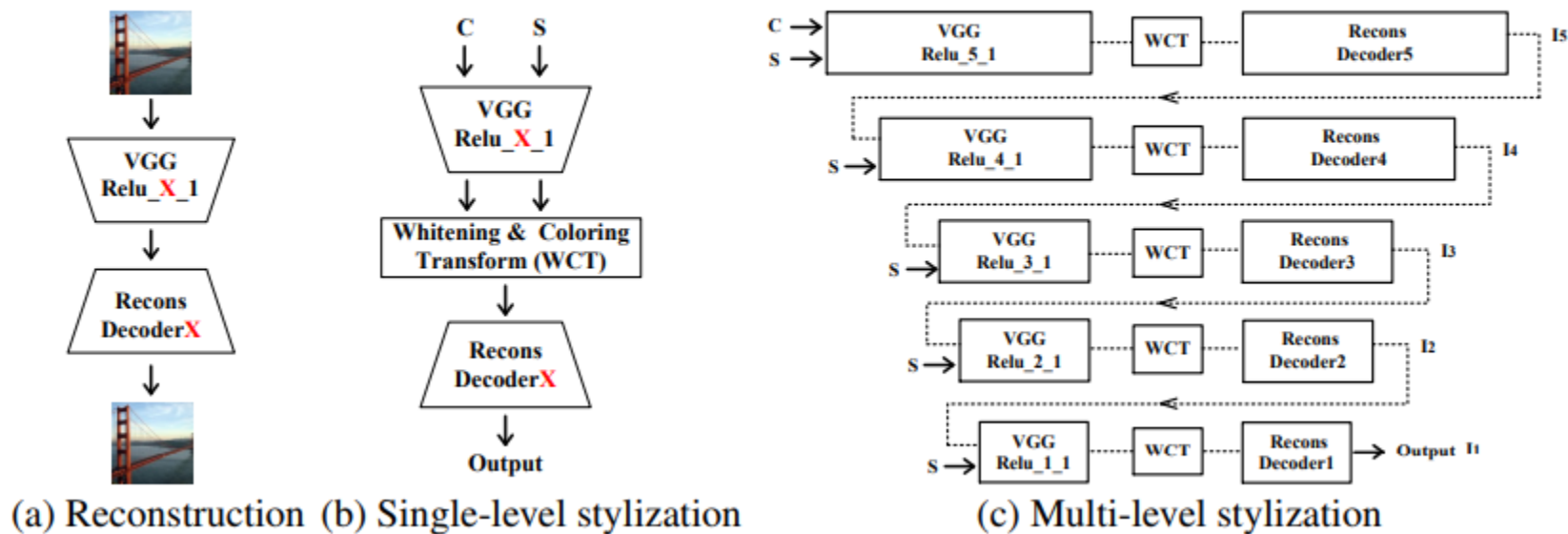
**Coloring transform.** We first center  $f_s$  by subtracting its mean vector  $m_s$ , and then carry out the coloring transform [14], which is essentially the inverse of the whitening step to transform  $\hat{f}_c$  linearly as in (3) such that we obtain  $\hat{f}_{cs}$  which has the desired correlations between its feature maps ( $\hat{f}_{cs} \hat{f}_{cs}^\top = f_s f_s^\top$ ),

$$\hat{f}_{cs} = E_s D_s^{\frac{1}{2}} E_s^\top \hat{f}_c, \quad (3)$$

where  $D_s$  is a diagonal matrix with the eigenvalues of the covariance matrix  $f_s f_s^\top \in \mathbb{R}^{C \times C}$ , and  $E_s$  is the corresponding orthogonal matrix of eigenvectors. Finally we re-center the  $\hat{f}_{cs}$  with the mean vector  $m_s$  of the style, i.e.,  $\hat{f}_{cs} = \hat{f}_{cs} + m_s$ .

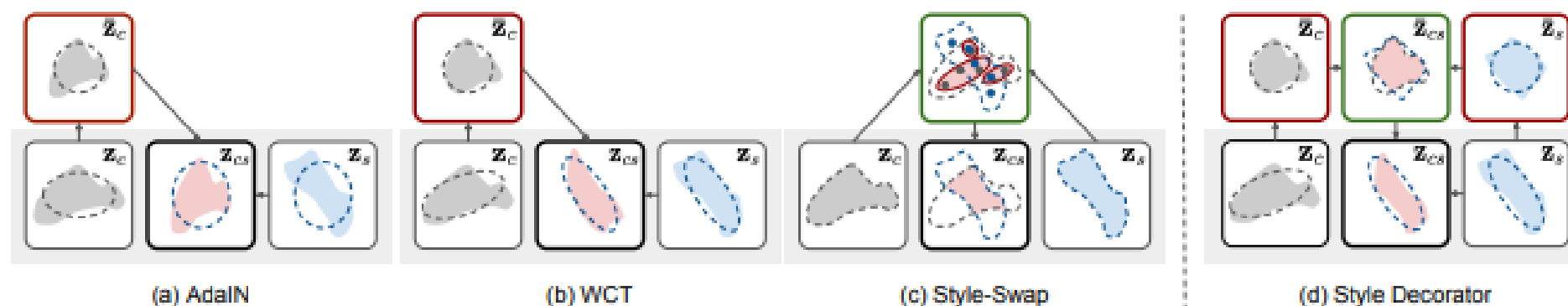
# Zero-Shot Method

## Universal Style Transfer via Feature Transforms



# Zero-Shot Method

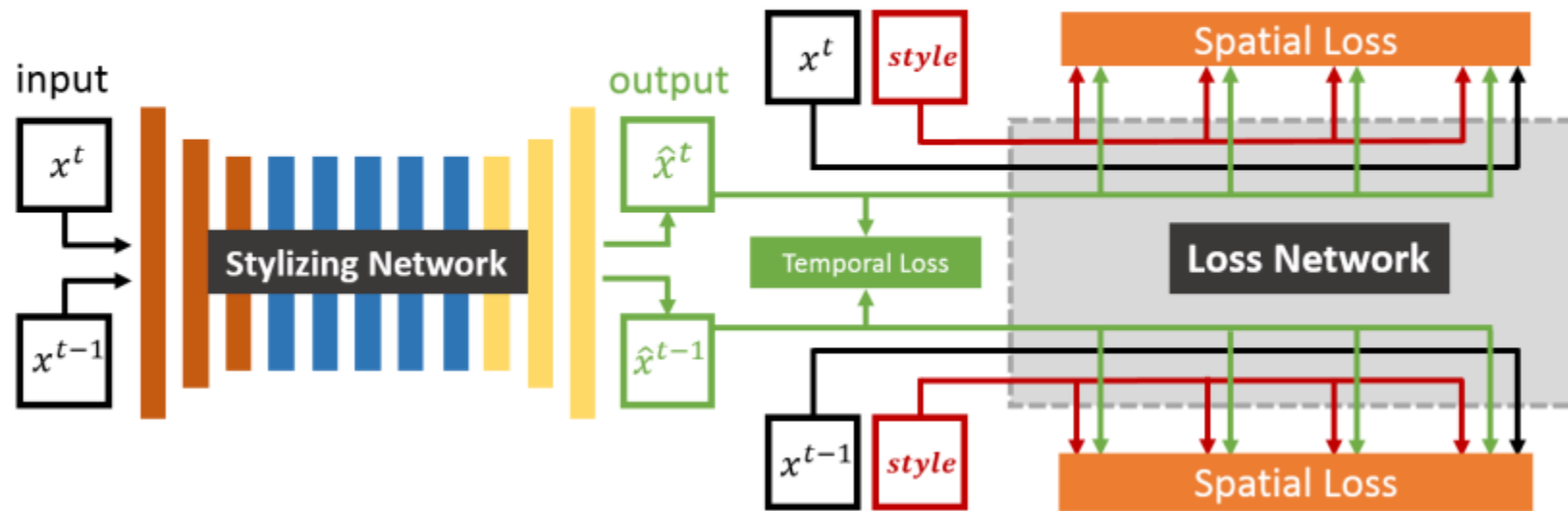
## Avatar-Net: Multi-scale Zero-shot Style Transfer by Feature Decoration





# Video Style Transfer

## Real-Time Neural Style Transfer for Videos



# Video Style Transfer

## Characterizing and Improving Stability in Neural Style Transfer

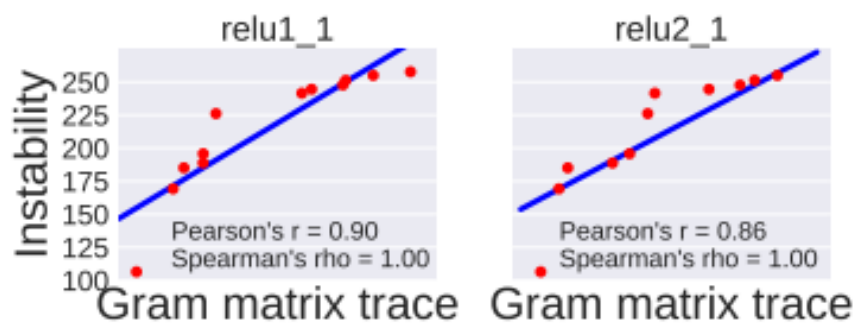
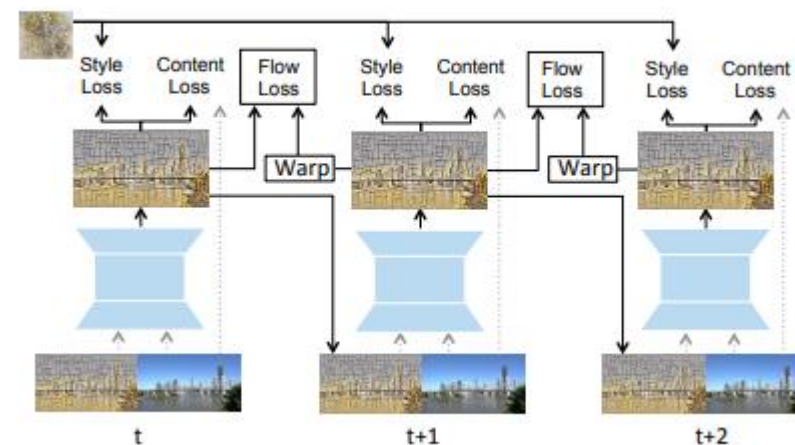


Figure 3. We train feedforward style transfer models for twelve styles, and define the *instability* of a style as the mean squared error between stylized adjacent frames over a dataset of videos with a static camera and no motion. We also compute the trace of the Gram matrix at two layers of the VGG-16 loss network for each style; styles with larger trace tend to be more unstable.



# Photorealistic Style Transfer

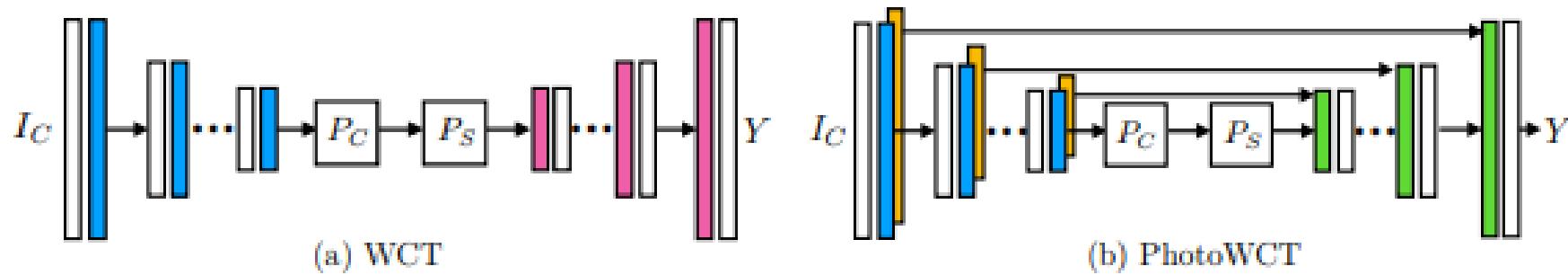
## Deep Photo Style Transfer

Formally, we build upon the Matting Laplacian of Levin et al. [9] who have shown how to express a grayscale matte as a locally affine combination of the input RGB channels. They describe a least-squares penalty function that can be minimized with a standard linear system represented by a matrix  $\mathcal{M}_I$  that only depends on the input image  $I$  (We refer to the original article for the detailed derivation. Note that given an input image  $I$  with  $N$  pixels,  $\mathcal{M}_I$  is  $N \times N$ ). We name  $V_c[O]$  the vectorized version ( $N \times 1$ ) of the output image  $O$  in channel  $c$  and define the following regularization term that penalizes outputs that are not well explained by a locally affine transform:

$$\mathcal{L}_m = \sum_{c=1}^3 V_c[O]^T \mathcal{M}_I V_c[O] \quad (2)$$

# Photorealistic Style Transfer

## A Closed-form Solution to Photorealistic Image Stylization



# Photorealistic Style Transfer

## A Closed-form Solution to Photorealistic Image Stylization

$$\operatorname{argmin}_r \frac{1}{2} \left( \sum_{i,j=1}^N w_{ij} \left\| \frac{r_i}{\sqrt{d_{ii}}} - \frac{r_j}{\sqrt{d_{jj}}} \right\|^2 + \lambda \sum_{i=1}^N \|r_i - y_i\|^2 \right), \quad (4)$$

where  $y_i$  is the pixel color in the PhotoWCT-stylized result  $Y$  and  $r_i$  is the pixel color in the desired smoothed output  $R$ . The variable  $d_{ii} = \sum_j w_{ij}$  is the diagonal element in the degree matrix  $D$  of  $W$ , i.e.,  $D = \operatorname{diag}\{d_{11}, d_{22}, \dots, d_{NN}\}$ . In (4),  $\lambda$  controls the balance of the two terms.

which encourages consistent stylization within semantically similar regions. The above optimization problem is a simple quadratic problem with a closed-form solution, which is given by

$$R^* = (1 - \alpha)(I - \alpha S)^{-1}Y, \quad (5)$$

where  $I$  is the identity matrix,  $\alpha = \frac{1}{1+\lambda}$  and  $S$  is the normalized Laplacian matrix computed from  $I_C$ , i.e.,  $S = D^{-\frac{1}{2}}WD^{-\frac{1}{2}} \in \mathbb{R}^{N \times N}$ . As the constructed graph is often sparsely connected (i.e., most elements in  $W$  are zero), the inverse operation in (5) can be computed efficiently. With the closed-form solution, the smoothing step can be written as a function mapping given by:

$$R^* = \mathcal{F}_2(Y, I_C) = (1 - \alpha)(I - \alpha S)^{-1}Y. \quad (6)$$