

*Heaven's Light is Our Guide*

## **Rajshahi University of Engineering & Technology**



*Department of Electrical & Computer Engineering*

**Course No:** ECE 4124

**Course Name:** Digital Signal Processing

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## Experiment No: 05

**Experiment Name:** Z transform and Inverse Z transform of Causal, Non Causal and Anti-Causal system

### Theory:

A mathematical technique called the Z-transform is used to translate differential equations in the time domain into algebraic equations in the z-domain.

The analysis of a linear shift invariant (LSI) system is the Z-transform. Difference equations are used to model an LSI discrete time system. These time-domain difference equations are solved by first converting them into algebraic equations in the z-domain using the Z-transform, manipulating the algebraic equations in the z-domain, and then converting the results back into the time domain using the inverse Z-transform.

The Z-transform formula

$$X(z) = \sum_{n=-\infty}^{\infty} x[n]Z^{-n}$$

The method of determining the time domain signal  $x(n)$  from its Z-transform  $X(z)$  is known as the inverse Z-transform.

The symbol for the inverse Z-transform is-  $x(n) = Z^{-1} [X(z)]$

**Required software:** MATLAB

### Code:

#### Causal System:

```
clc;
clear all;
x=input('array: ');b=0;
y=sym('z');
n=length(x);
for i=1:n
    b=b+x(i)*y^(1-i);

end
b
z=[];
p=[0]
zplane(z,p)
```

## Output:

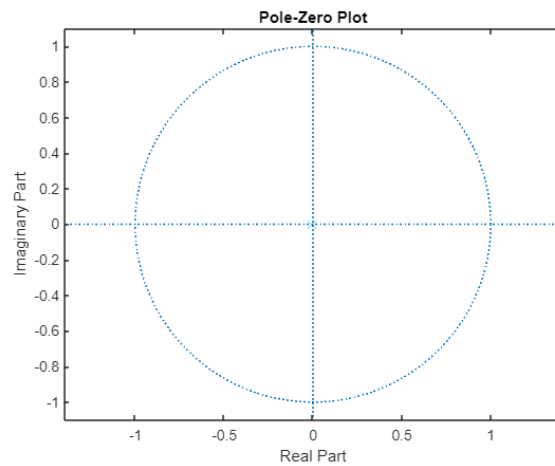
```
array:
[2 3 3 4]

b =

3/z + 3/z^2 + 4/z^3 + 2

p =

0
```



## Non causal System:

```
clc;

clear all;
x=input('array: ');
b=0;
y=sym('z');
n=length(x);
m=input('index: ')
for i=1:n
    b=b+x(i)*y^(m-i);

end
b
z=[];
p=[0]
zplane(z,p)
```

## Output:

```
array:
[1 2 3 4]
index:
4

m =

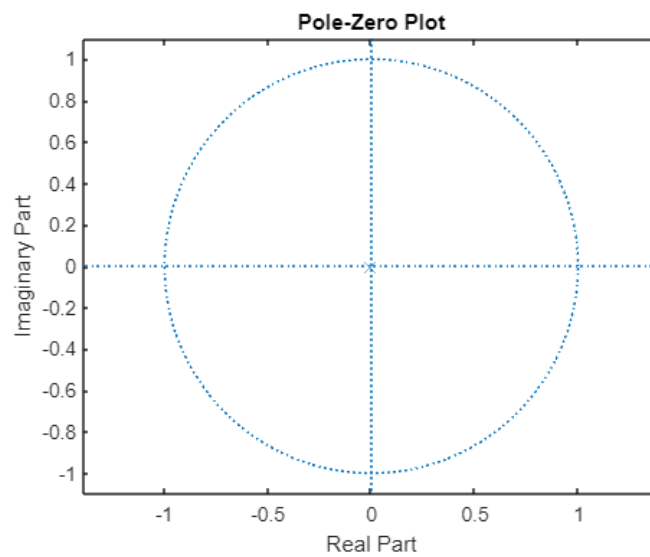
4

b =

z^3 + 2*z^2 + 3*z + 4

p =

0
```



### Anti causal System:

```
clc;
clear all;
x=input('array: ');b=0;
y=sym('z');
n=length(x);
for i=1:n
    b=b+x(i)*y^(-(i-n));

end
b
z=[];
p=[]
zplane(z,p)
```

### Output:

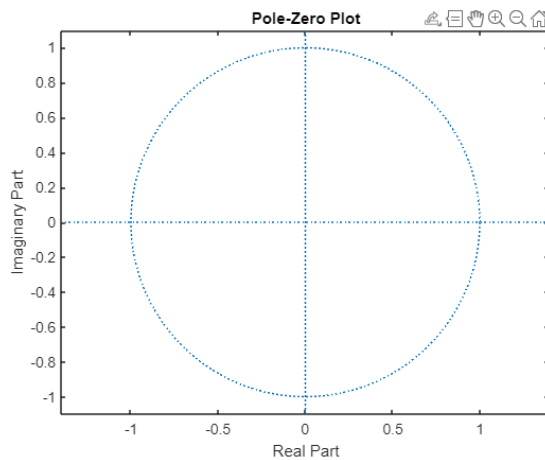
```
array:
[1 2 3 4]

b =

z^3 + 2*z^2 + 3*z + 4

p =

[]
```



### Inverse Z transform:

```
clc;
clear all;
y=sym('z');syms n;
%f=exp(-2*n);
f=2^-n;
F=ztrans(f)
t=iztrans(F);
t=simplify(t);
disp(t);z=[0];
%p=poles(F);
%zplane(z,p);
%grid
b = [1];
a = [1 -1/2];

[b,a] = eqtflength(b,a);
[z,p,k] = tf2zp(b,a)
```

```

zplane(b,a)
text(real(z)+0.1,imag(z),"Zero")
text(real(p)+0.1,imag(p),"Pole")

```

### Output:

```

F =

z/(z - 1/2)

1/2^n

z =

0

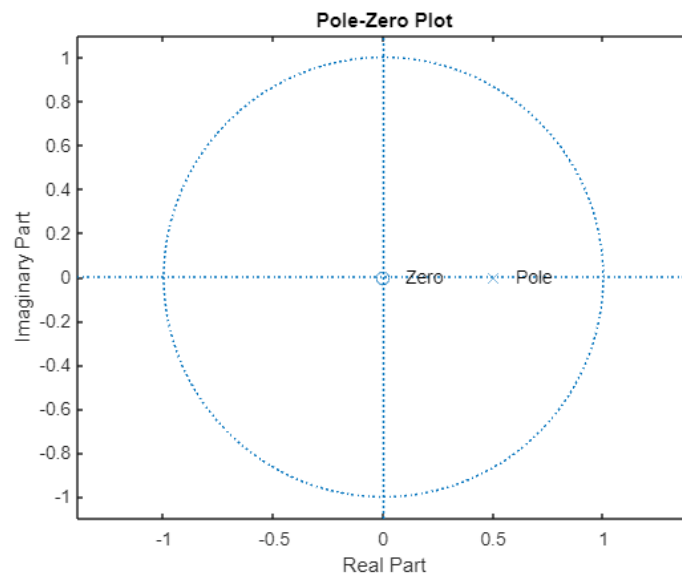
p =

0.5000

k =

1

```



### Conclusion:

The experiment was done successfully as we have achieved the expected output which matches theoretical analysis.