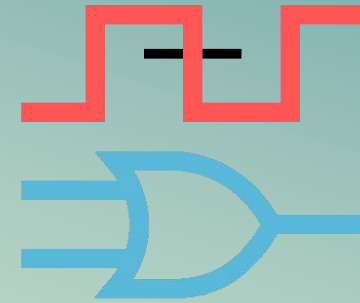


Digital Electronics

Class X
lab 18



1's complement

One's Complement

Invert all bits. Each 1 becomes a 0, and each 0 becomes a 1.

Original Value

One's Complement

0 → 1
1 → 0

1010 → 0101
1111 → 0000

11110000 → 00001111
10100011 → 01011100

11110000 10100101 → 00001111 01011010

transforming the 0 bit
to 1 and the 1 bit to 0

1's complement Examples

1's complement of 7 (0111) is 8 (1000)

1's complement of 12 (1100) is 3 (0011)

2's complement Examples

Example #1

$$\begin{array}{r} 5 = 00000101 \\ \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 11111010 \\ +1 \\ \hline -5 = 11111011 \end{array}$$

Complement Digits

Add 1

Example #2

$$\begin{array}{r} -13 = 11110011 \\ \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 00001100 \\ +1 \\ \hline 13 = 00001101 \end{array}$$

Complement Digits

Add 1

1 is added to the 1's complement of the binary number

Boolean Postulates

(1)	$A + 0 = A$	$A \cdot 1 = A$	identity
(2)	$A + \text{NOT}[A] = 1$	$A \cdot \text{NOT}[A] = 0$	complement
(3)	$A + B = B + A$	$A \cdot B = B \cdot A$	commutative law
(4)	$A + (B + C) = (A + B) + C$	$A \cdot (B \cdot C) = (A \cdot B) \cdot C$	associative law
(5)	$A + (B \cdot C) = (A + B) \cdot (A + C)$	$A \cdot (B + C) = (A \cdot B) + (A \cdot C)$	distributive law

Boolean Algebra

(6)	$A + A = A$	$A \cdot A = A$	
(7)	$A + 1 = 1$	$A \cdot 0 = 0$	
(8)	$A + (A \cdot B) = A$	$A \cdot (A + B) = A$	
(9)	$A + (\text{NOT}[A] \cdot B) = A + B$	$A \cdot (\text{NOT}[A] + B) = A \cdot B$	
(10)	$(A \cdot B) + (\text{NOT}[A] \cdot C) + (B \cdot C) = (A \cdot B) + (\text{NOT}[A] \cdot C)$	$A \cdot (B + C) = (A \cdot B) + (A \cdot C)$	
(11)	$\text{NOT}[A + B] = \text{NOT}[A] \cdot \text{NOT}[B]$	$\text{NOT}[A \cdot B] = \text{NOT}[A] + \text{NOT}[B]$	de Morgan's theorem

Thank You