

Week 4

$y_{\text{-test}}$

4 samples:

0, 2, 1, 0

real or ground truth

Train a model

1

2

1

0

$y$

$$\begin{bmatrix} 5 \\ 1 \\ 0 \end{bmatrix}$$

$$y = w^T x$$



Train the model:  $w^T$

$x_{\text{-train}}, y_{\text{-train}}$

$$w=5 \Rightarrow y=5x$$

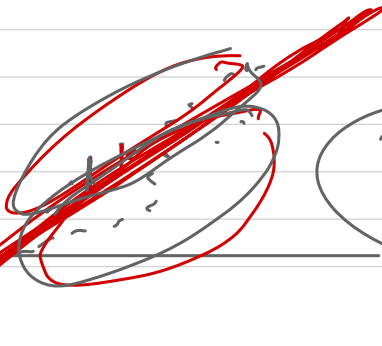
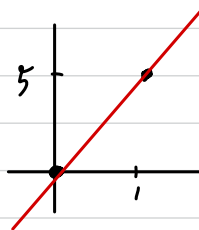
if  $x=1 \rightarrow y=5$   
 $x=0 \rightarrow y=0$

$x_{\text{-test}}$

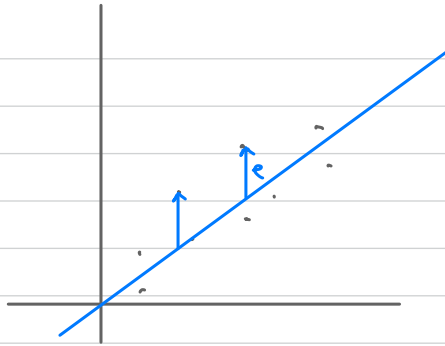
$y$

$y_{\text{-test}}$

$(x, y)$



$x_{\text{-train}}$   
 $y_{\text{-train}}$



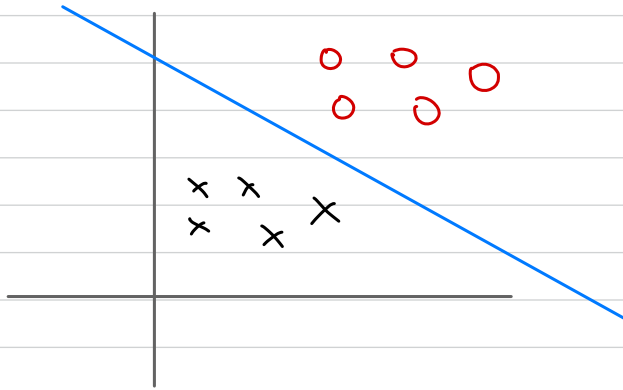
$$F(x_i) = w^T x_i$$

$$\mathcal{E}(w) = \frac{1}{N} \sum_{i=1}^N (w^T x_i - y_i)^2$$

$$\frac{\partial \mathcal{E}(w)}{\partial w} = \frac{2}{N} \sum_{i=1}^N (w^T x_i - y_i) x_i$$

$$w = w - \alpha * \frac{\partial \mathcal{E}(w)}{\partial w}$$

# Classification



Dataset : 150 Samples

120 samples  
TRAIN

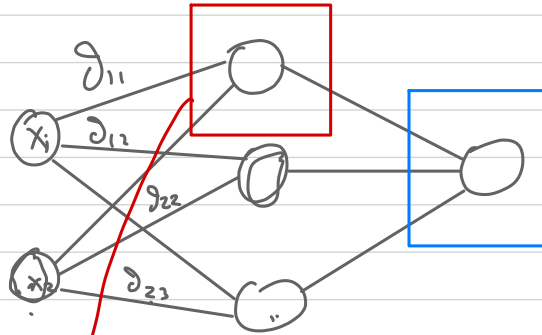
30 Samples  
TEST

$$\sigma = \frac{1}{1 + e^{-x}}$$

$$\sigma(w^T x) = \frac{1}{1 + e^{-w^T x}}$$

$$y[i] \stackrel{?}{=} y_{\text{test}}[i]$$

# Neural Networks



$$g_{11}x_1 + g_{12}x_2 \rightarrow \sigma(g_{11}x_1 + g_{12}x_2)$$

$$\sigma(g_{11}x_1 + g_{12}x_2) + \sigma(g_{21}x_1 + g_{22}x_2) + \sigma(g_{31}x_1 + g_{32}x_2)$$