Advanced image synthesis

Romain Vergne – 2014/2015

What is it?

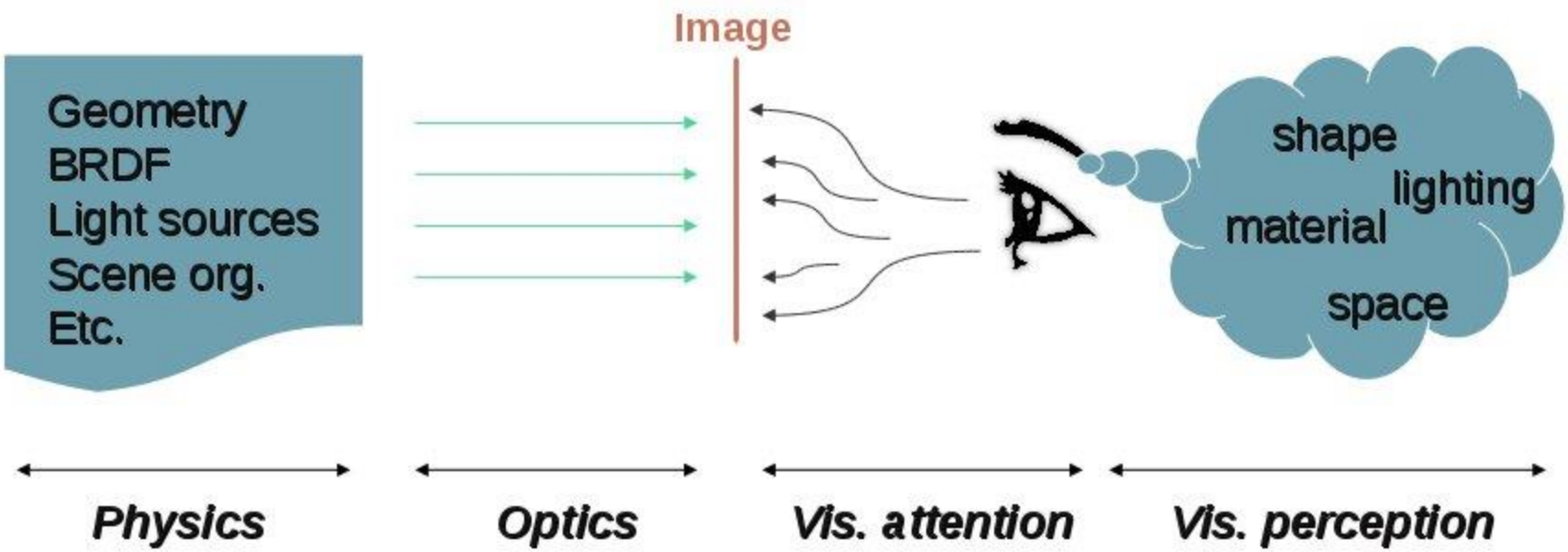
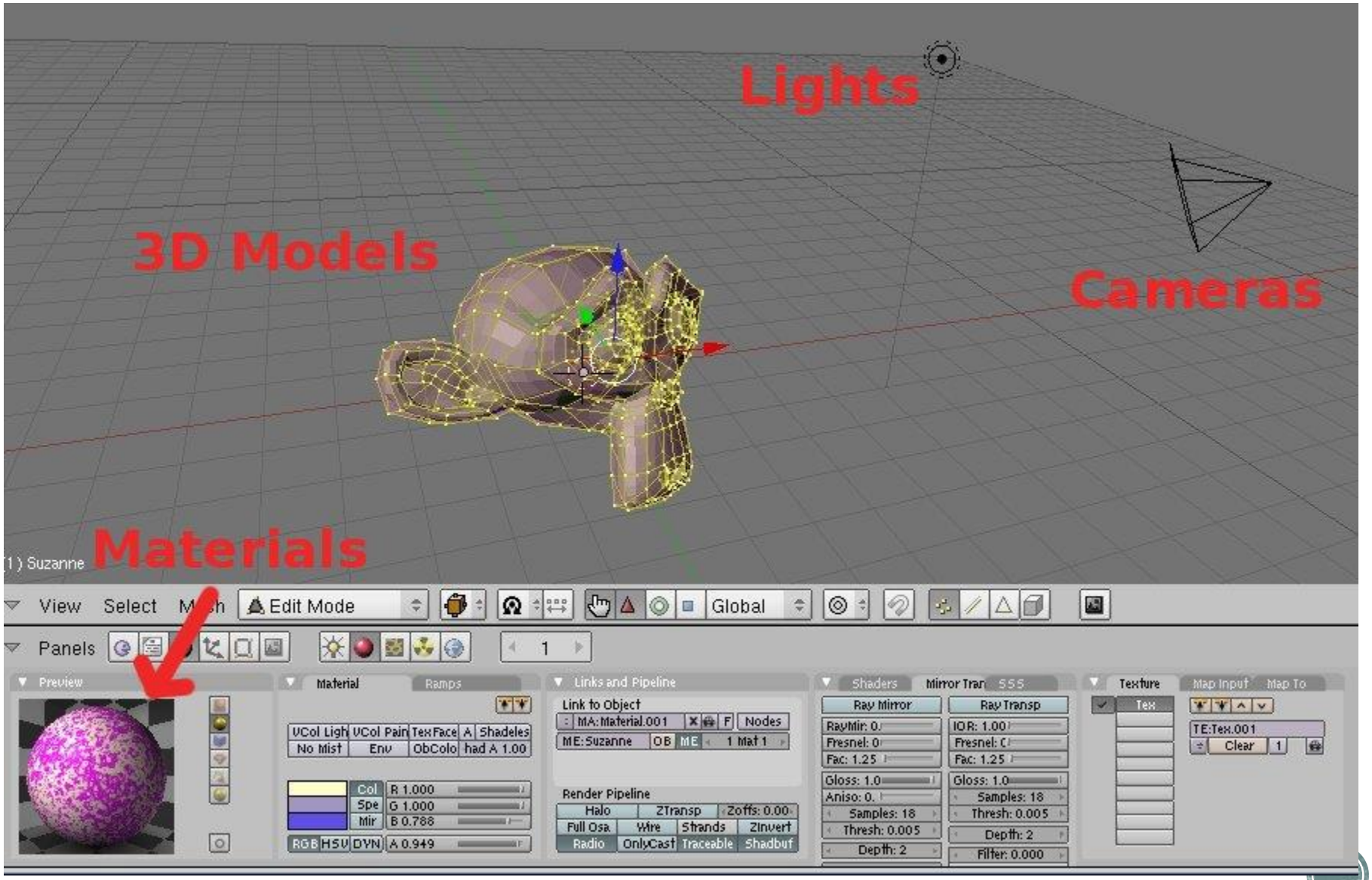


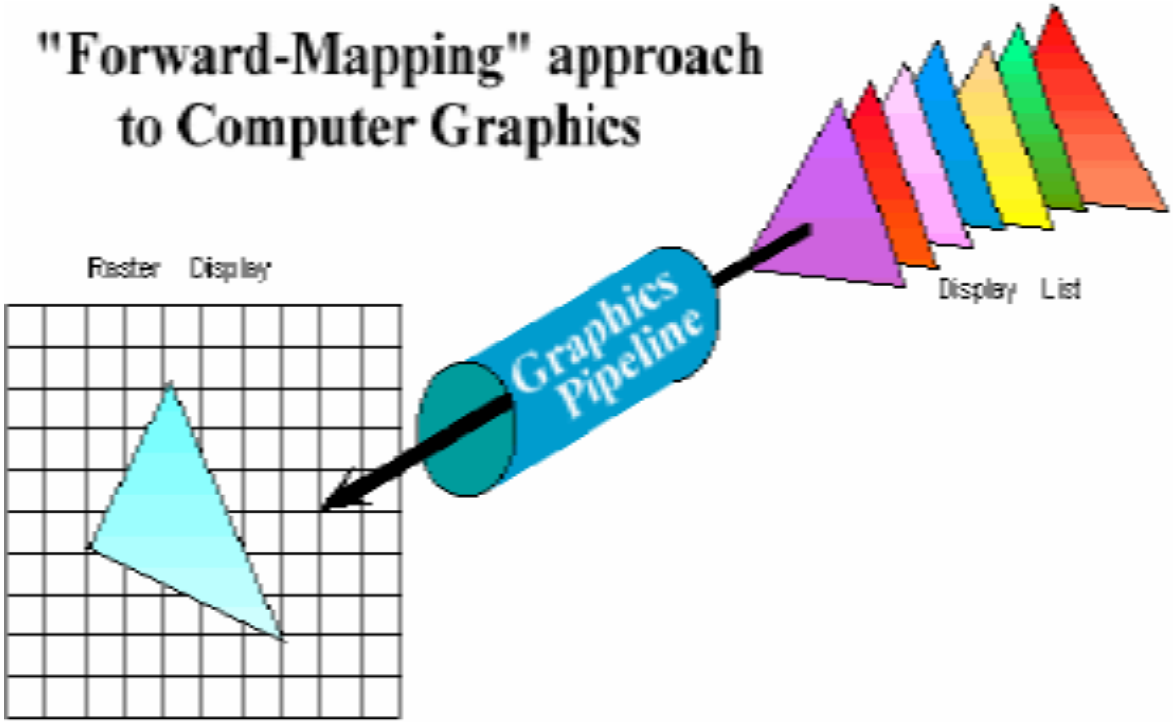
Image
Geometry
BRDF
Light sources
Scene org.
Etc.
shape
lighting
material
space
Physics
Optics
Vis. attention
Vis. perception

Which color in each pixel?

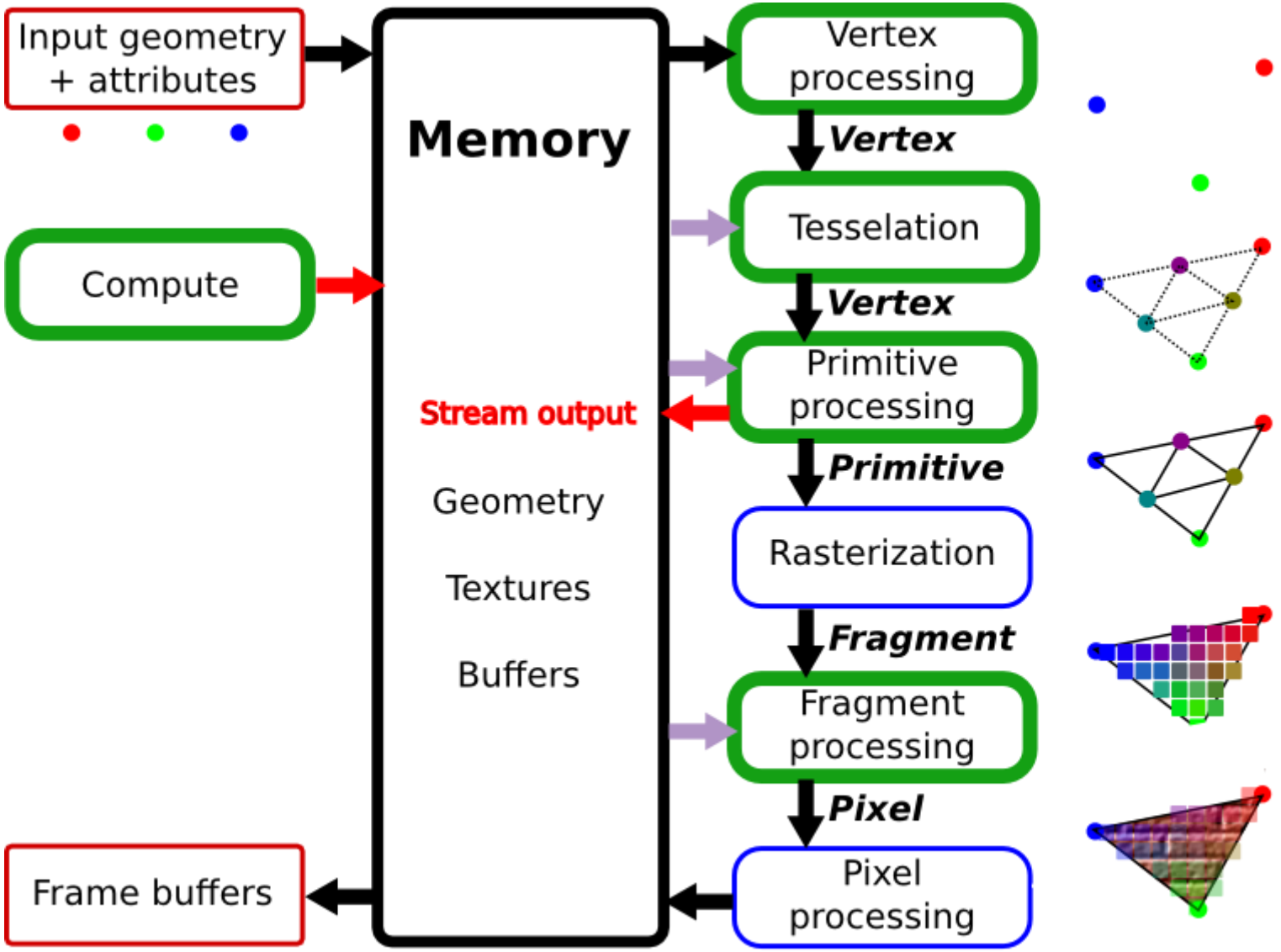


Rasterization pipeline

- For each triangle
  - Project triangle to image plane
  - For each pixel
    - Check pixel in triangle
    - Resolve visibility with z-buffer



Modern graphics pipeline



Rasterization advantages

- Modern scenes more complicated than images
  - 1920x1080 frame (1080p)
  - 64-bit color and 32-bit depth
  - 24 Mb memory
- Rasterization can stream over triangles
  - One triangle at a time
  - Parrallelism
  - Memory optimization

Rasterization limitations

- Restricted to scan-convertible primitives (triangles)
- No unified handling of
  - Shadows
  - Reflection
  - Transparency
- Potential problem of overdraw
  - Depth complexity
  - Each pixel touched many times

Rasterization VS ray-casting

- For each triangle
  - Project triangle to image plane
  - For each pixel
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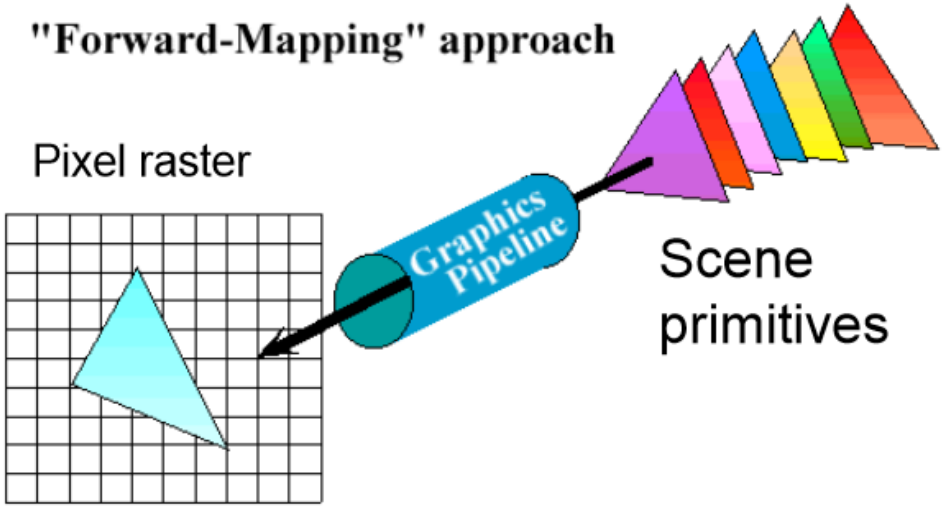
    - Resolve visibility with z-buffer



Rasterization VS ray-casting

- For each triangle
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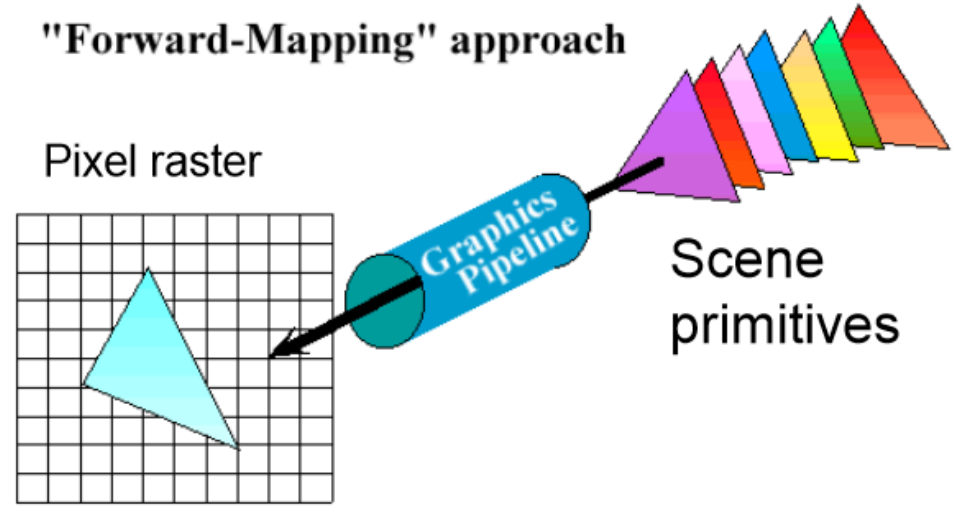
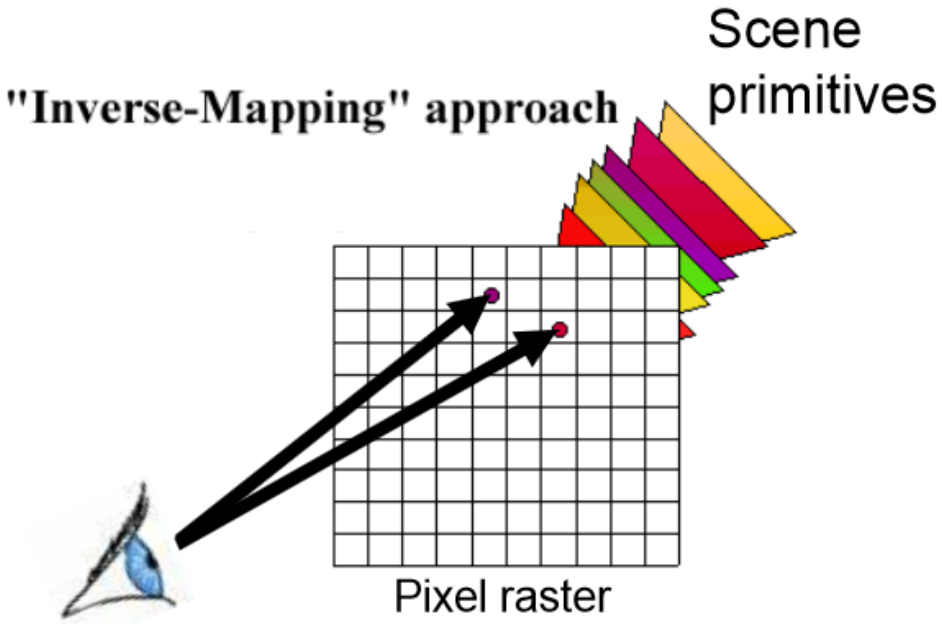
- For each pixel
  - Compute pixel ray
  - For each triangle
    - Check ray-triangle intersection
    - Get closest intersection





Rasterization VS ray-casting

- For each triangle
  - Project triangle to image plane
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Triangle-centric

- For each pixel
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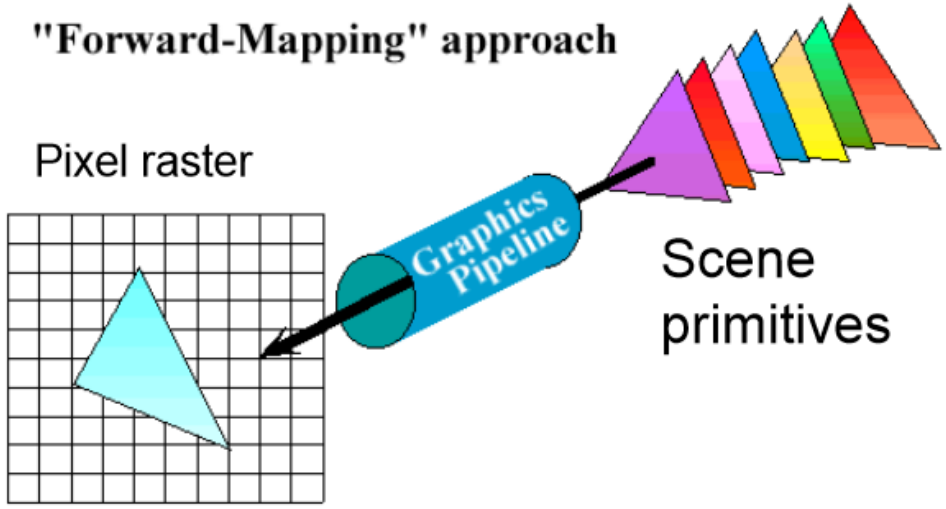
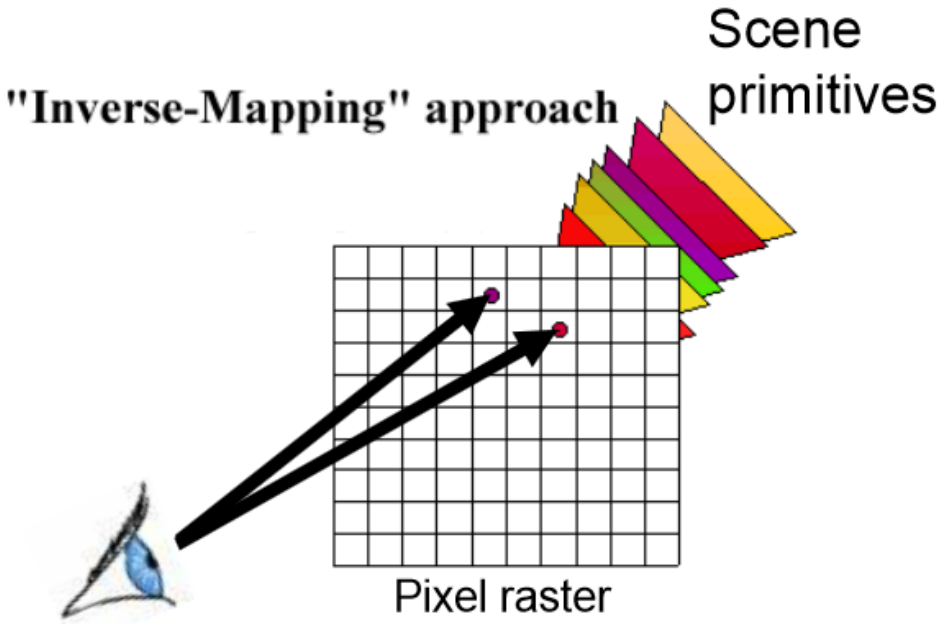
Ray-centric





Images from: http://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-837-computer-graphics-fall-2012/lecture-notes/MIT6_837F12_Lec21.pdf

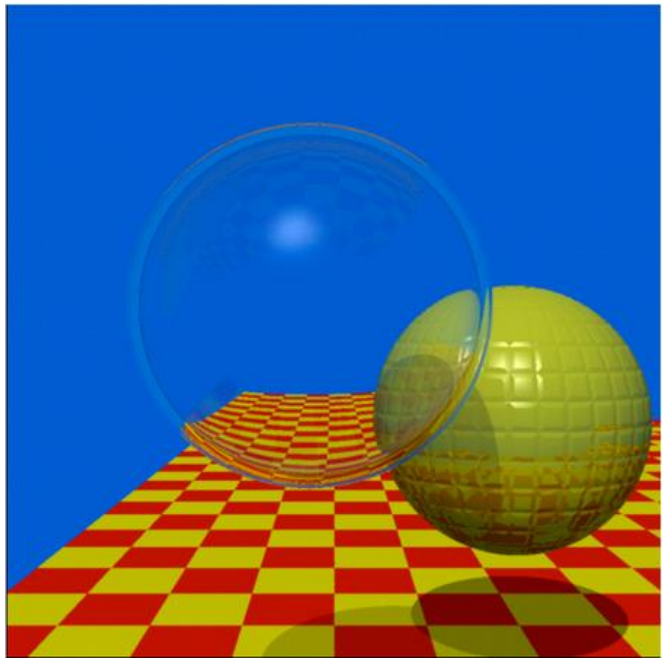
Ray-casting advantages

- Generality
  - Not limited to triangles: can render anything
  - Polygons, implicit, b-rep, etc…
- Shadows, reflection, refraction
  - Uniform handling
  - Directly obtained via recursion
- Base for many advanced algorithms
  - Path tracing, photon mapping, etc…

Ray-casting limitations

- Can be hard to implement
  - Entire scene in memory
- Can be slow with large scenes
  - But…

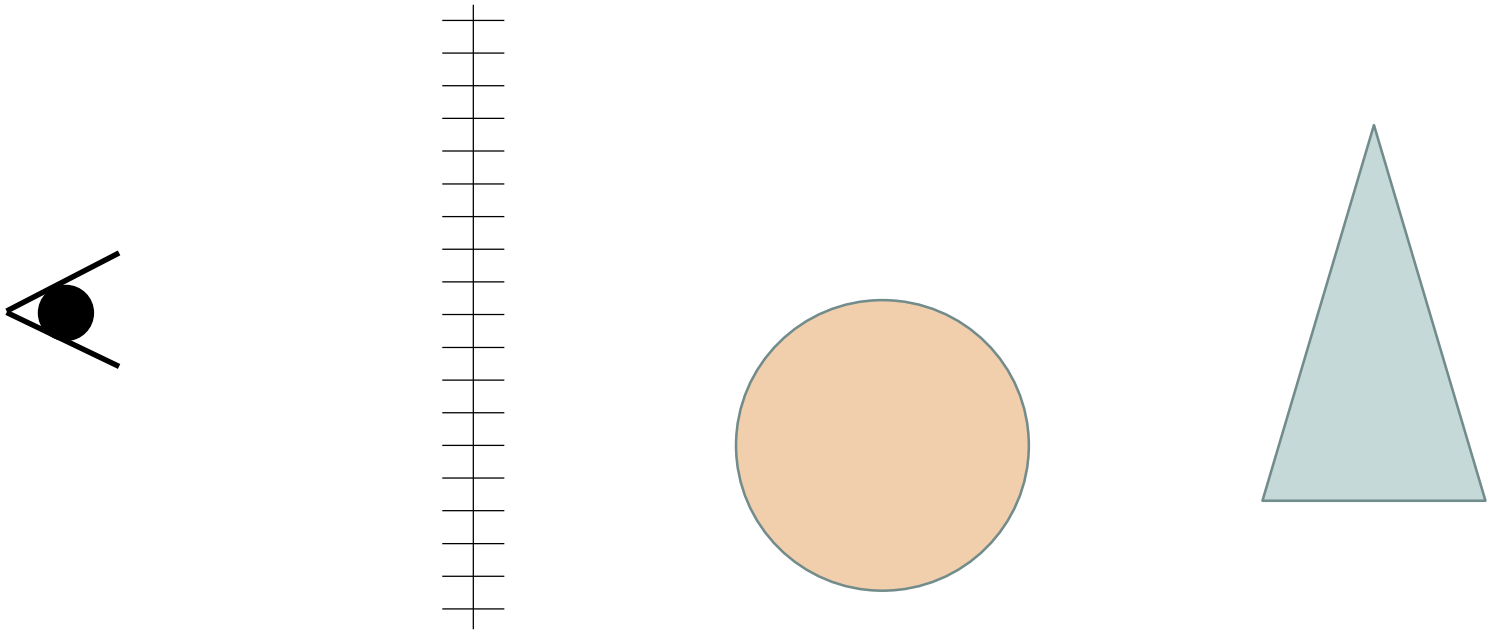
[T. Whitted, 1980]



- VAX 11/780 (1979): 74 min
- PC (2006): 6 sec
- GPU (2009): 30 fps
- GPU (2014): > 60 fps

Ray-casting basics

- For each pixel
  - Compute pixel ray
  - For each object
    - Check ray-object intersection
    - Get closest intersection



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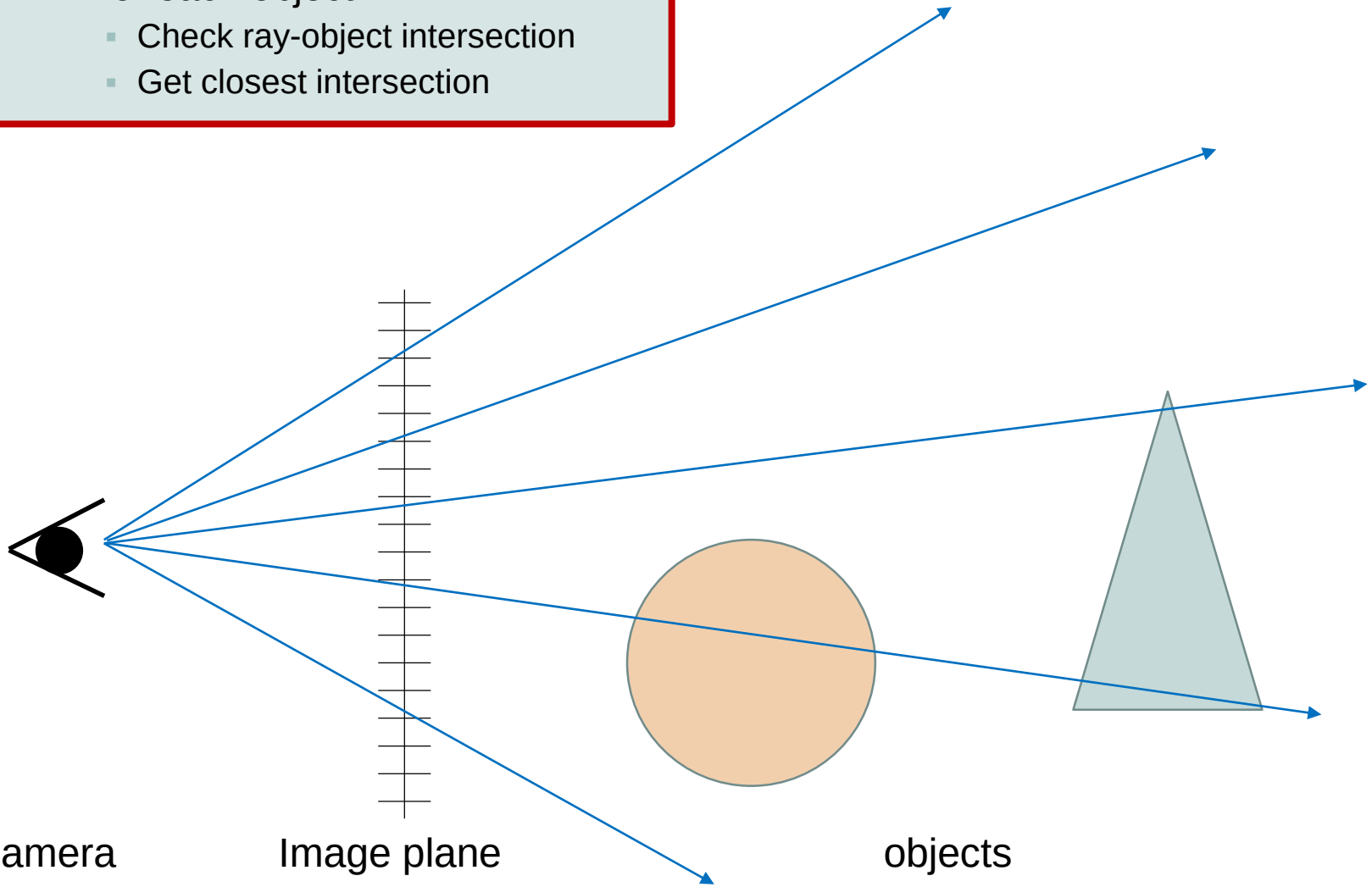

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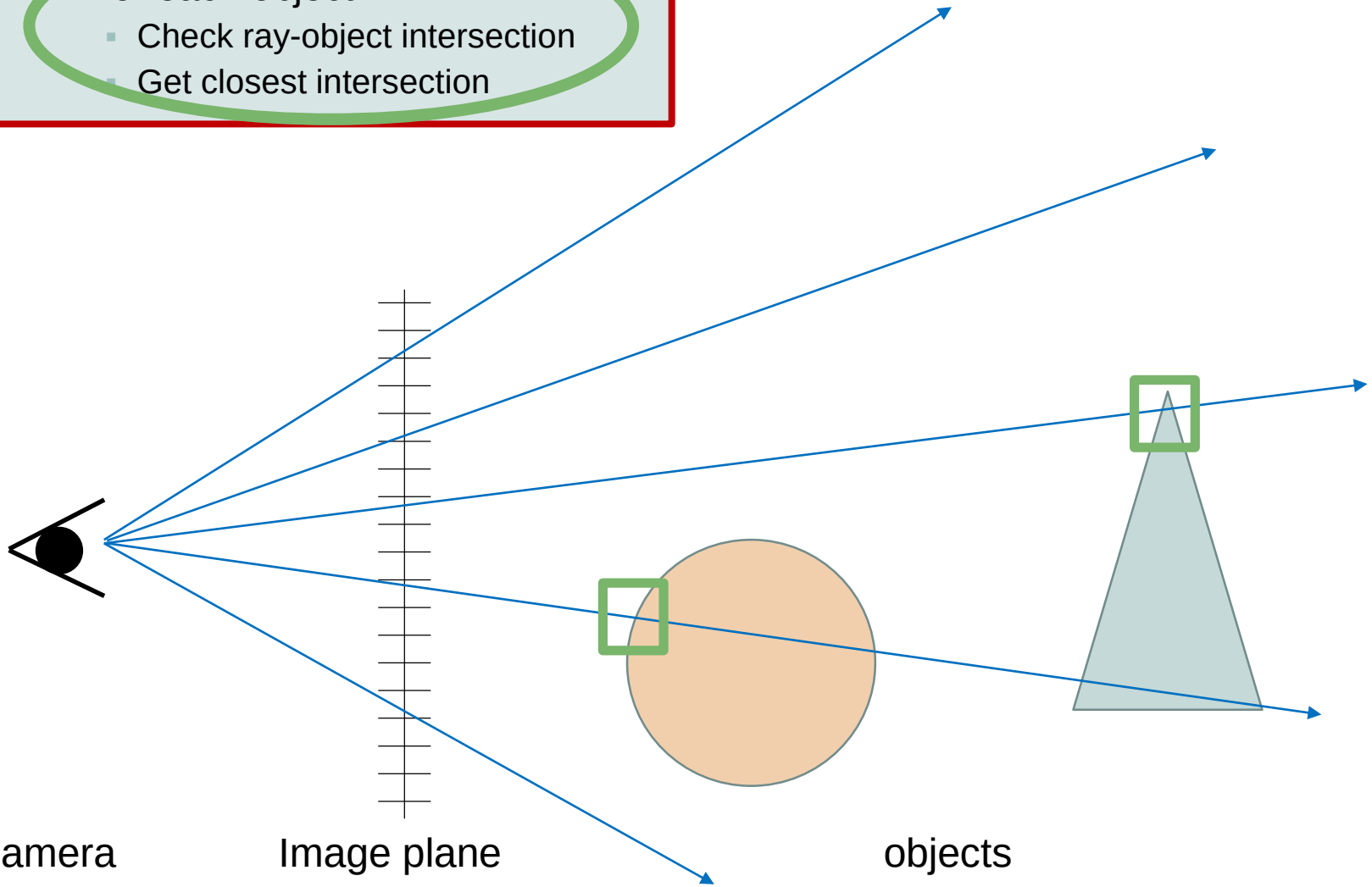

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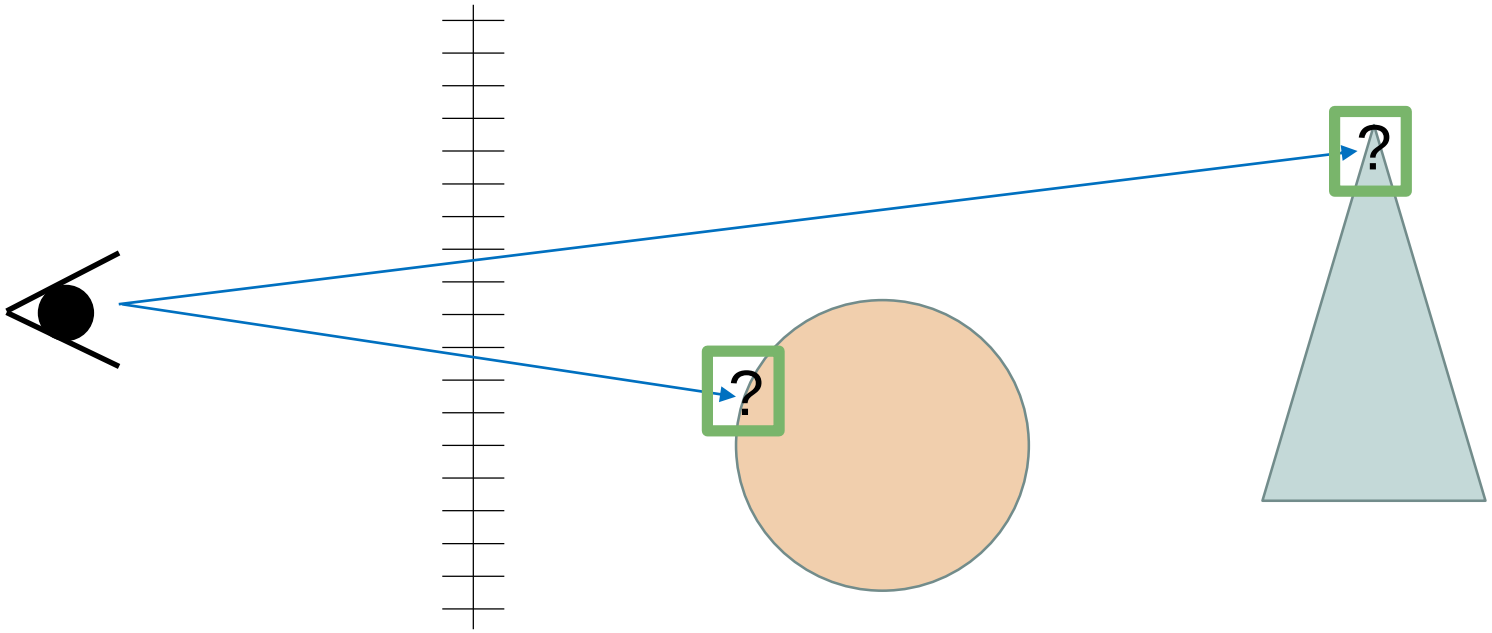
And then?



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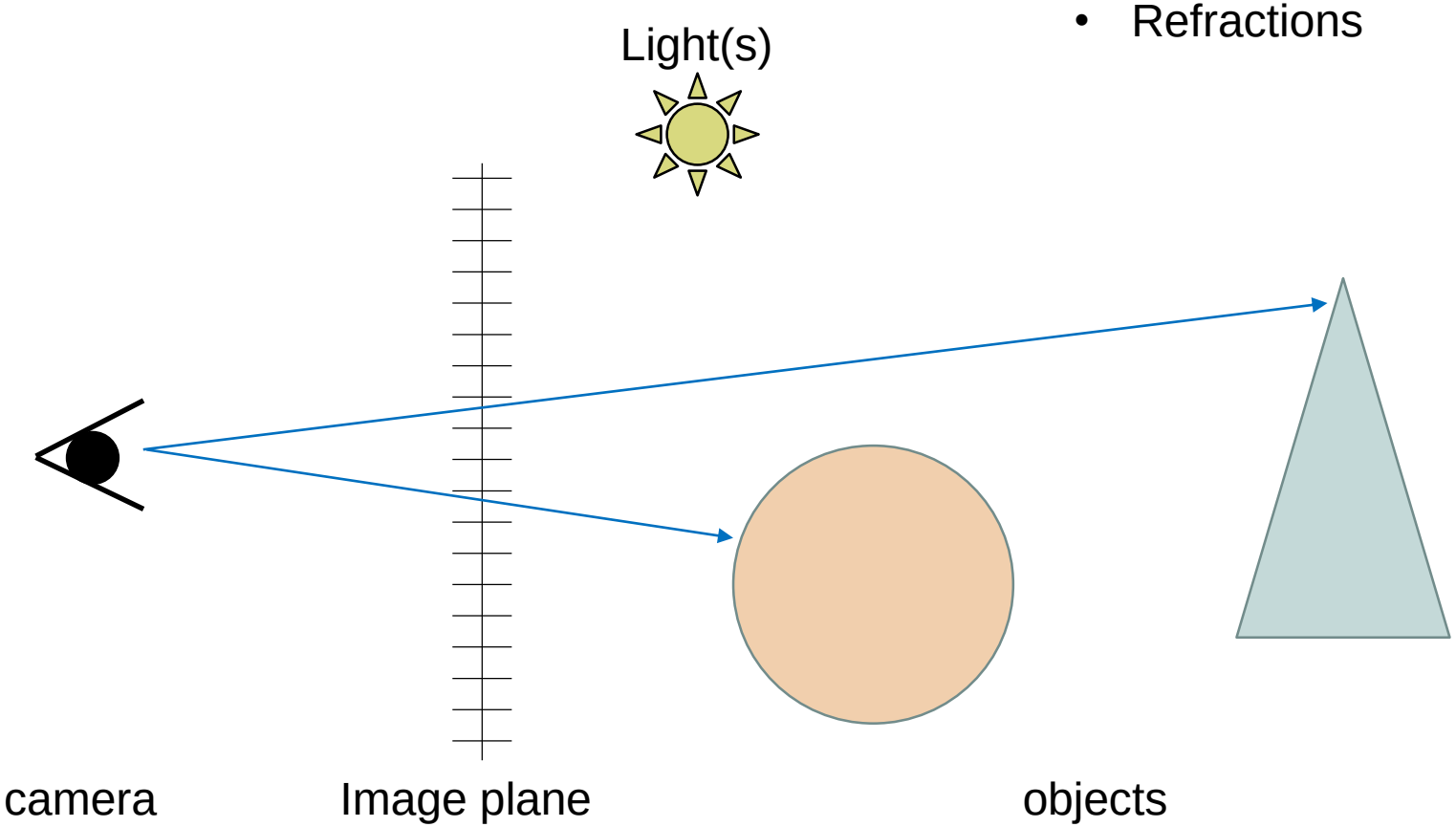
And then?
Shade!

- Shadow rays
- Reflections
- Refractions



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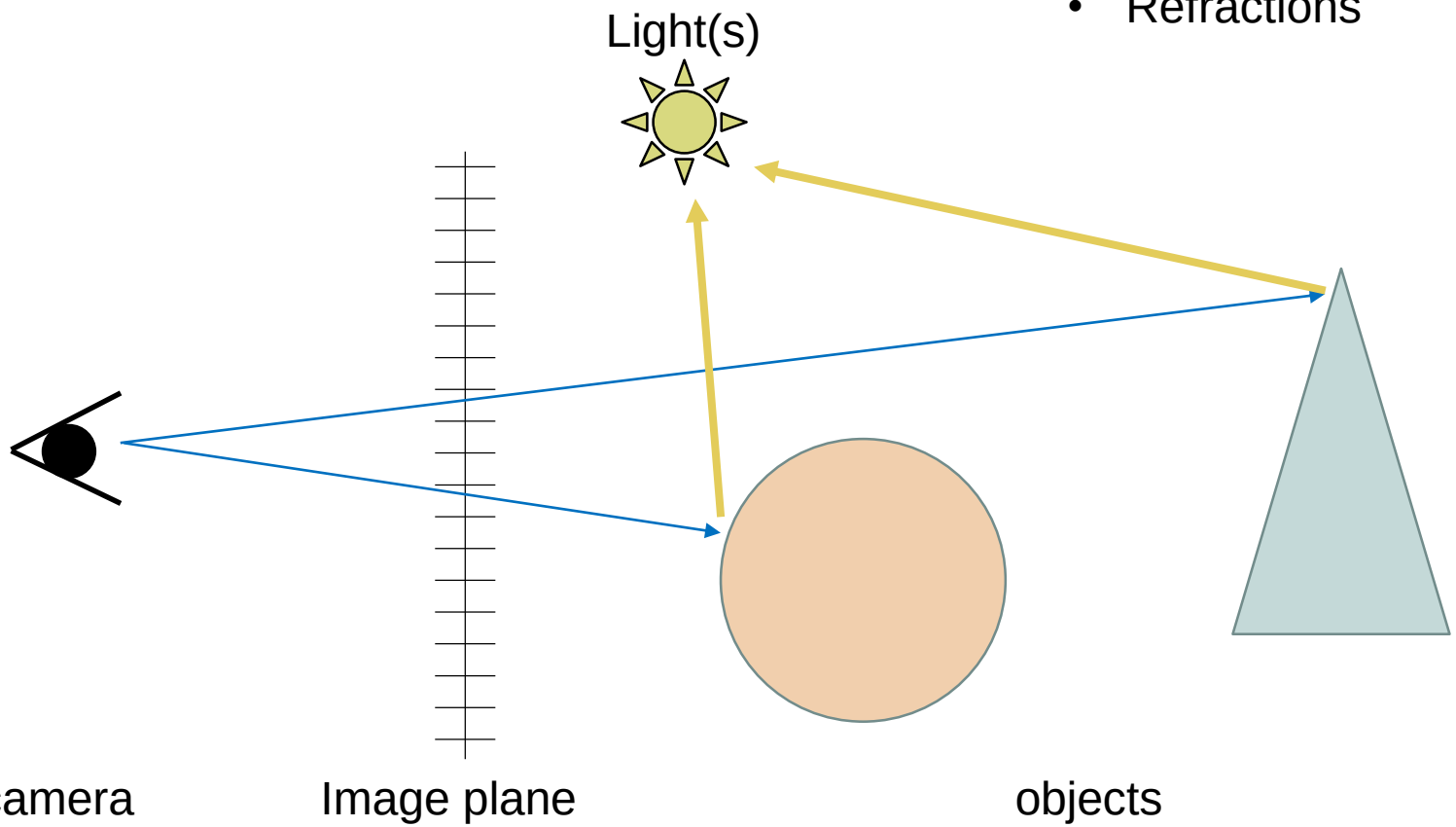

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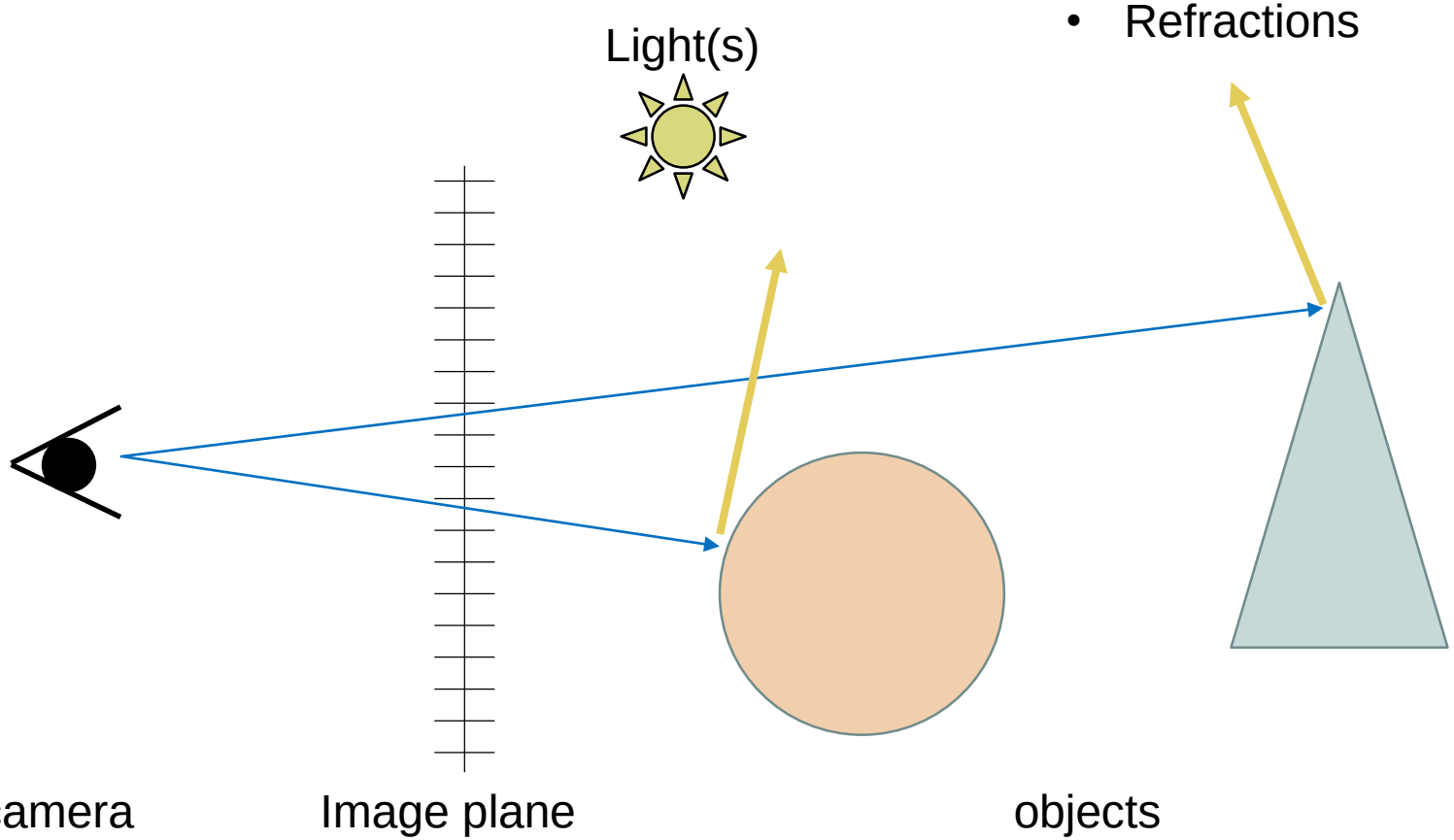

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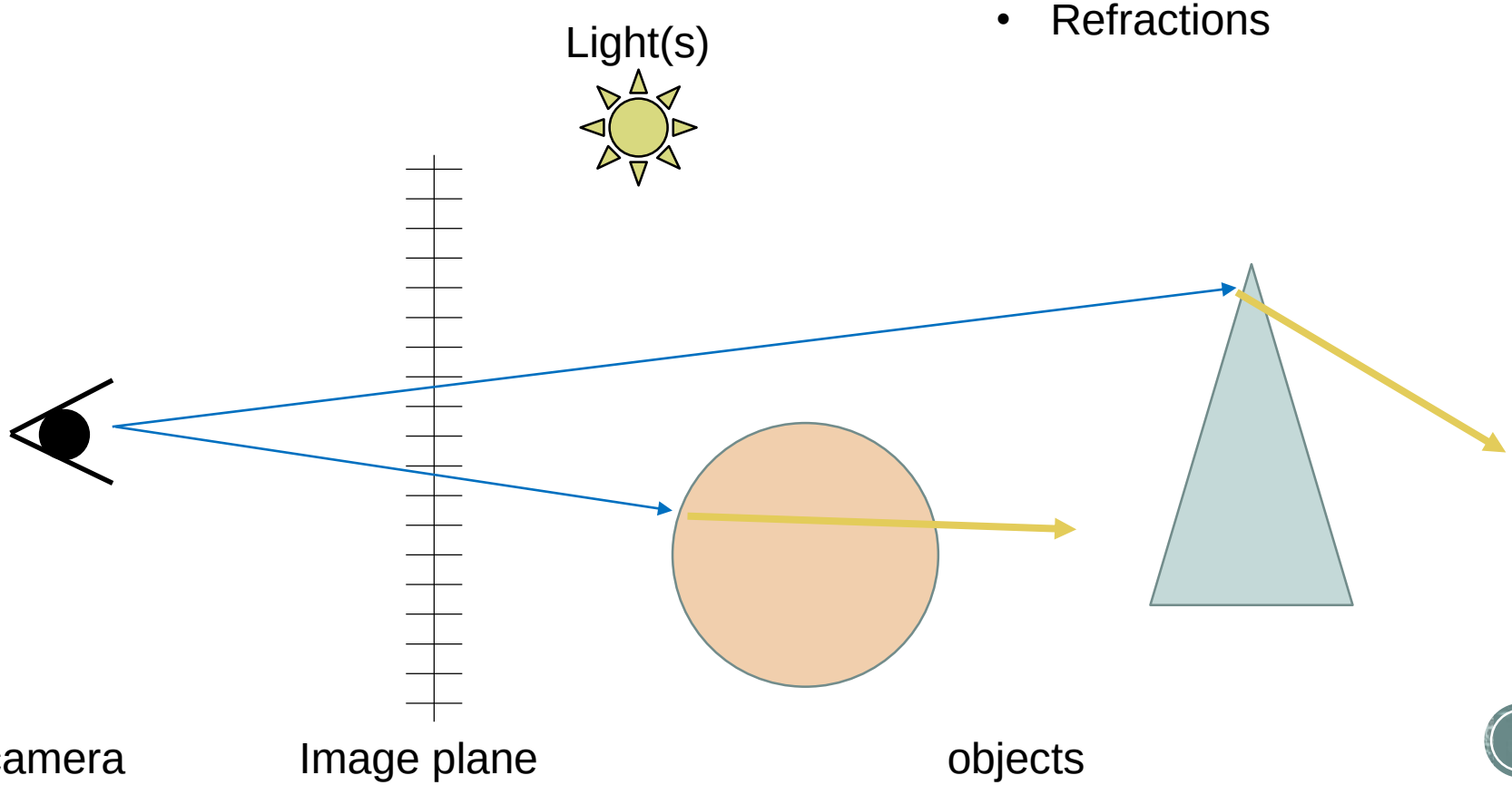
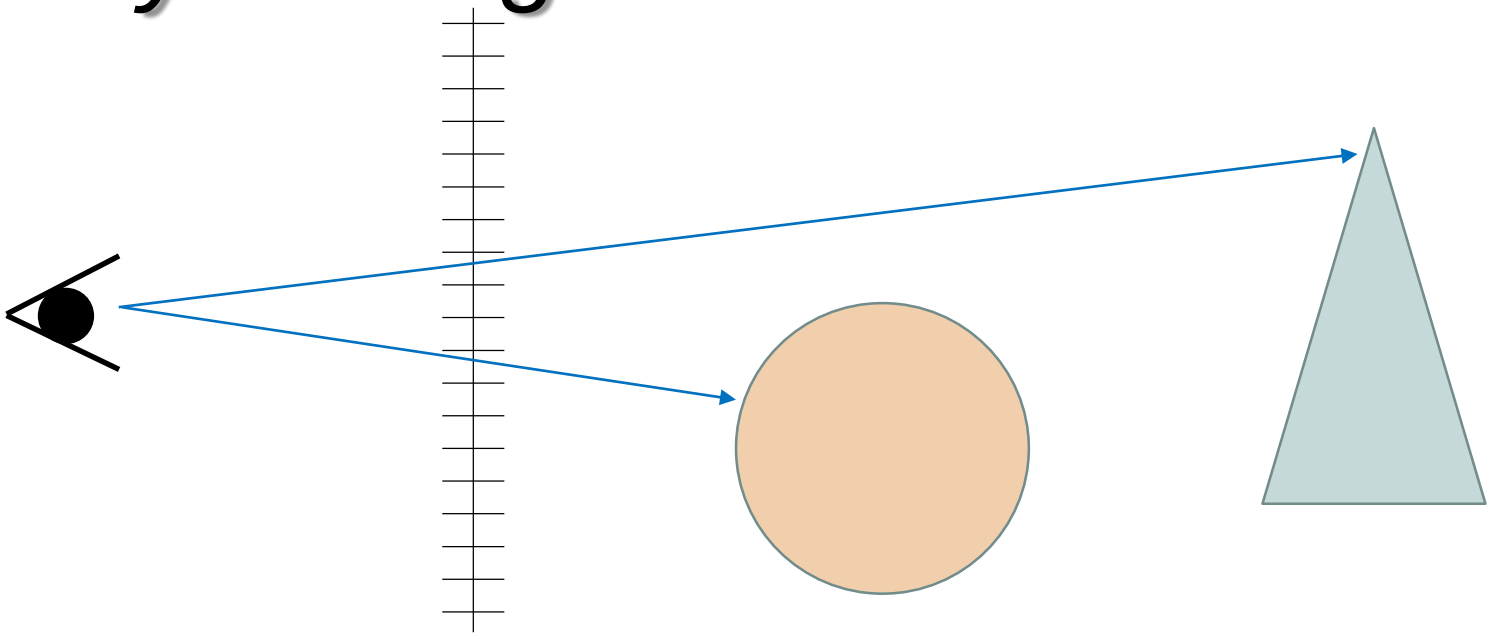


Ray-casting vs ray-tracing

Eye rays only
= Ray casting

- Shadow rays
- Reflections
- Refractions

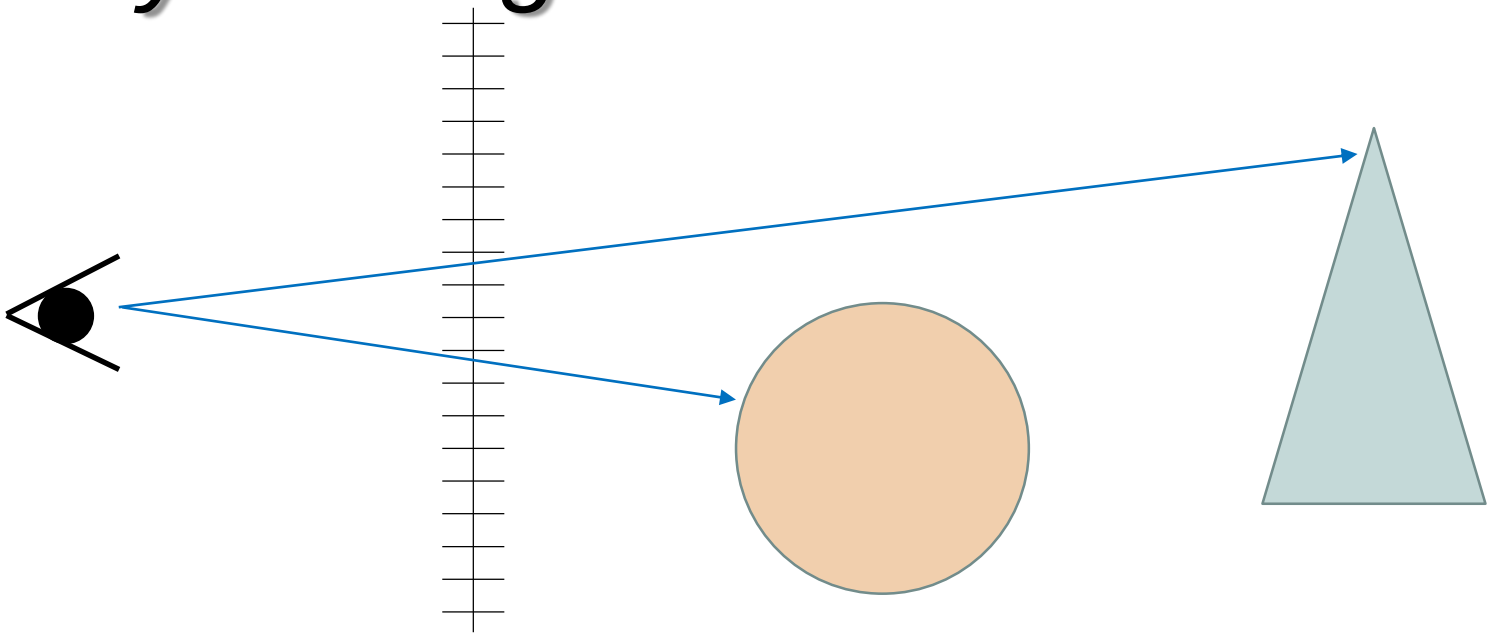


Ray-casting vs ray-tracing

Secondary rays
= Ray tracing

- Shadow rays
- Reflections
- Refractions

Eye rays only
= Ray casting



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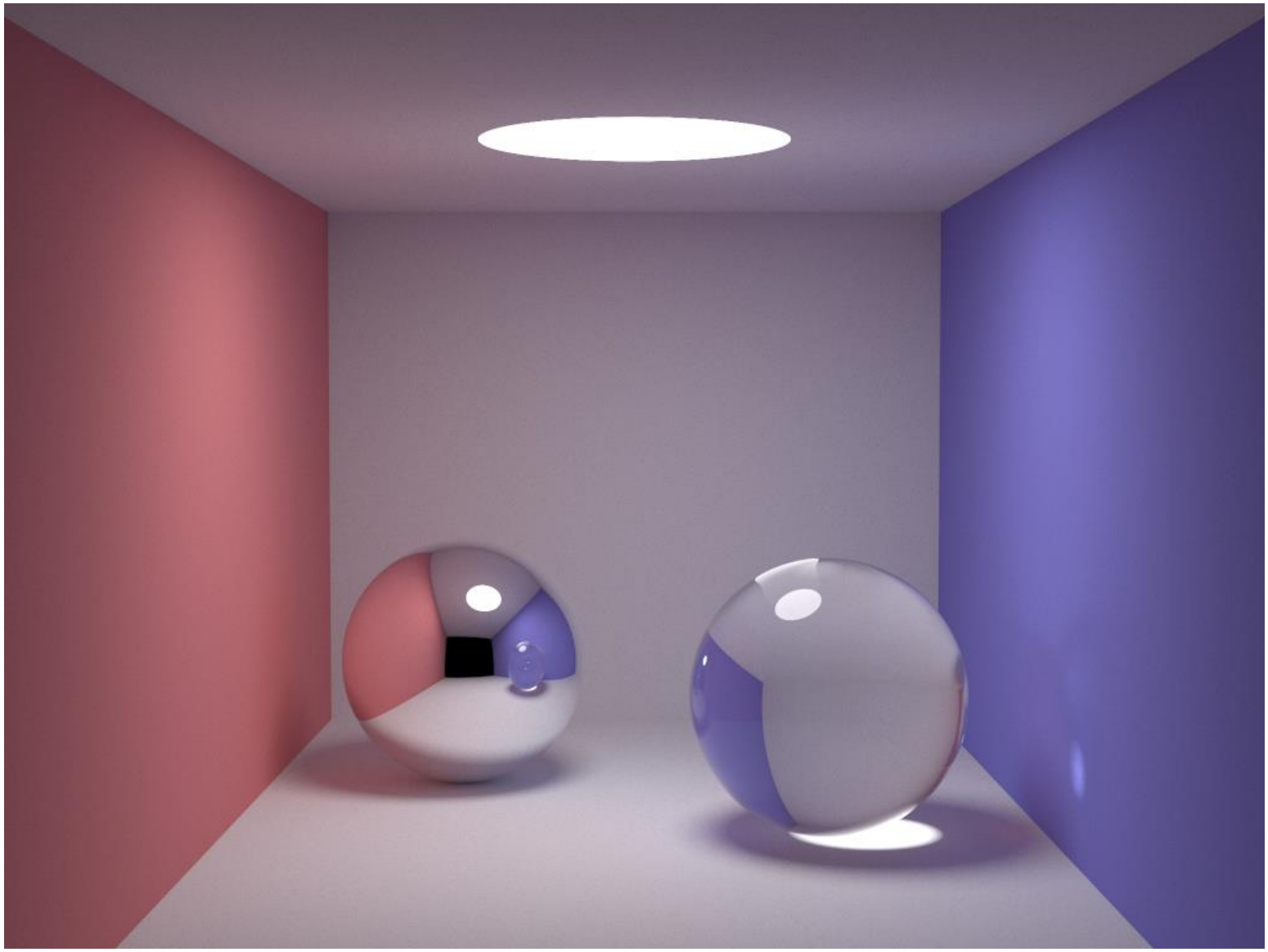

Ray-casting: summary

- For each pixel
  - Compute eye ray
  - For each object
    - Check ray-object intersection
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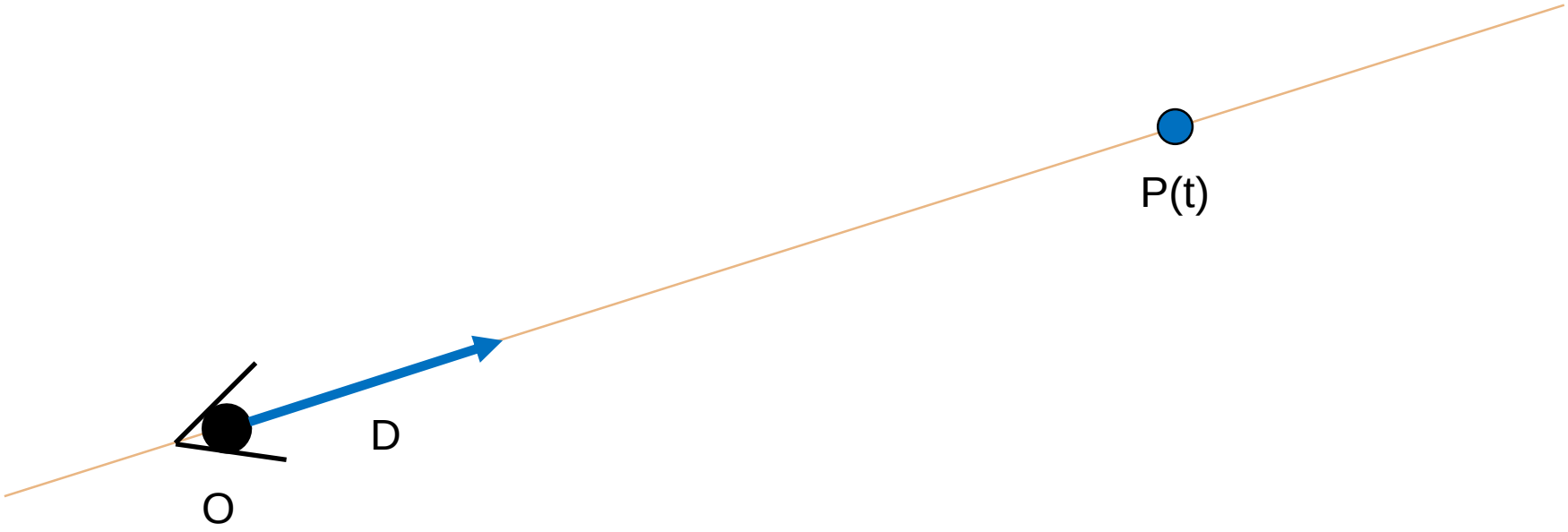
    - Shade depending on light and normal vector

Finding intersection point and normal is the central part of ray-casting!

Eye ray and camera

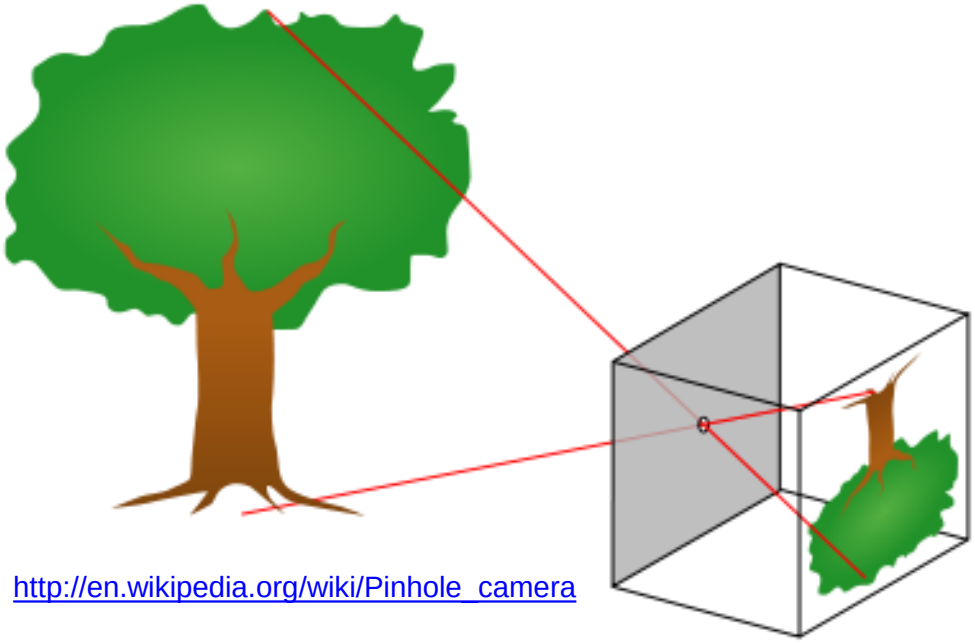
- Ray representation: parametric line
  - Origin O (3D point)
  - Direction D (normalized vector)
  - P(t) = O + t*D



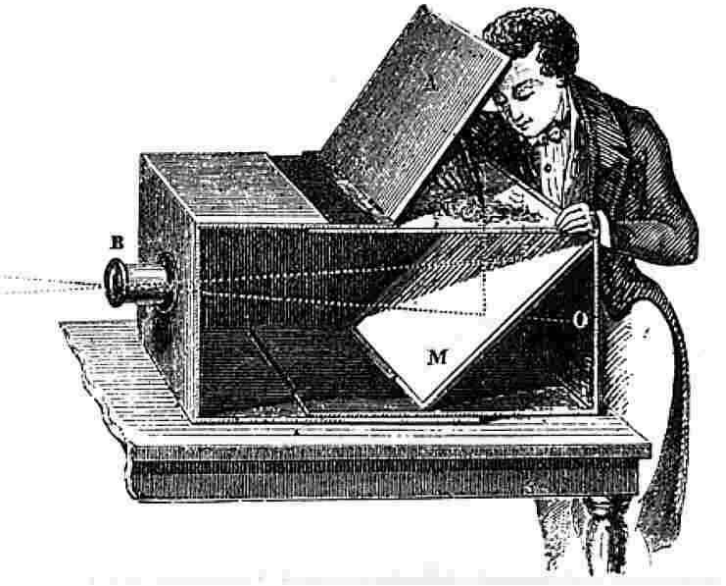
Goal: find smallest t>0 such that P(t) lies on a surface

Eye ray and camera

- Pinhole camera (or camera obscura)
  - Small aperture (perfect image if pinhole infinitivelly small)
  - Inverted image
  - Pure geometric optics



http://en.wikipedia.org/wiki/Pinhole_camera



A 19th-century artist using a camera obscura to outline his subject

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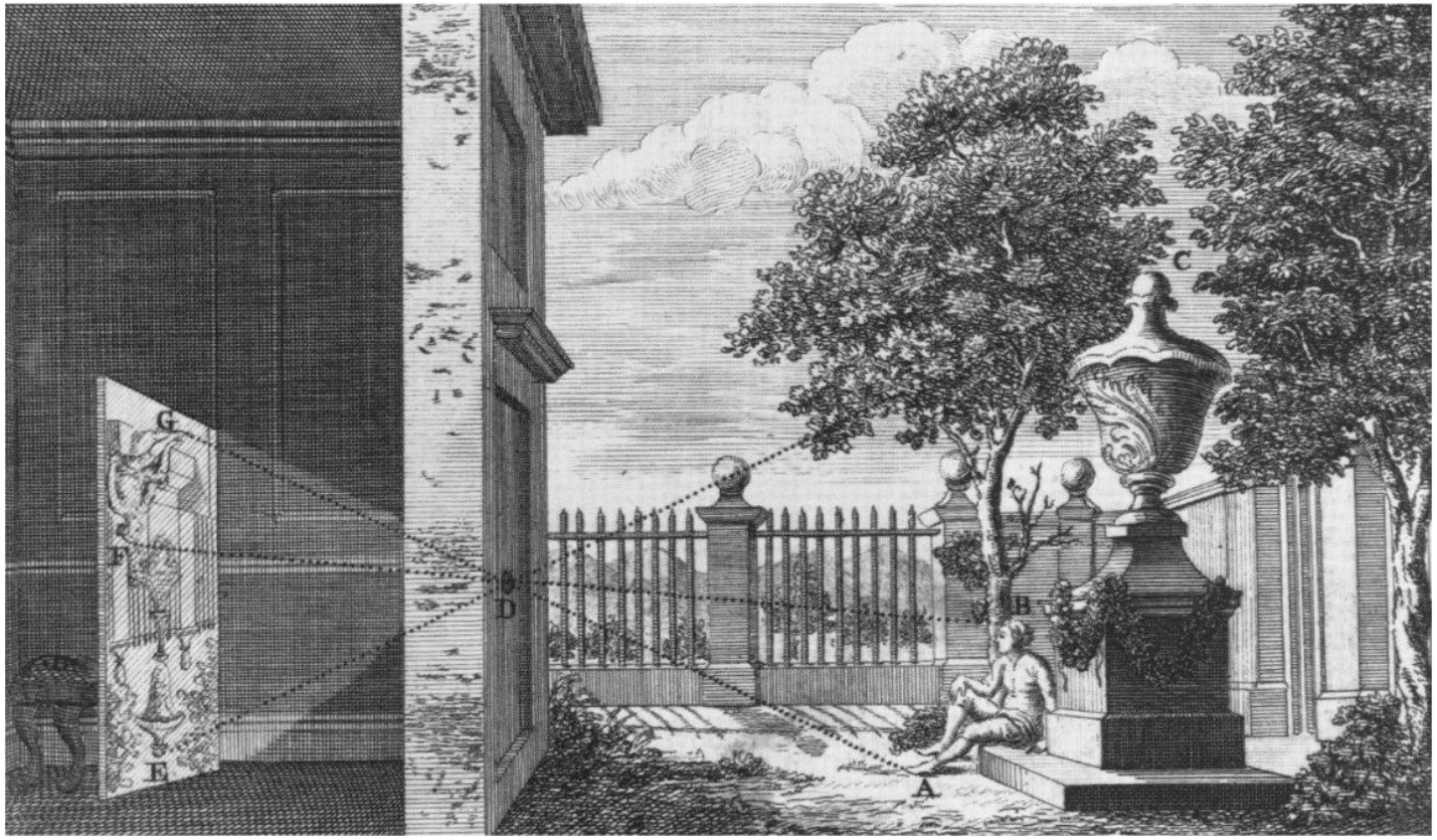
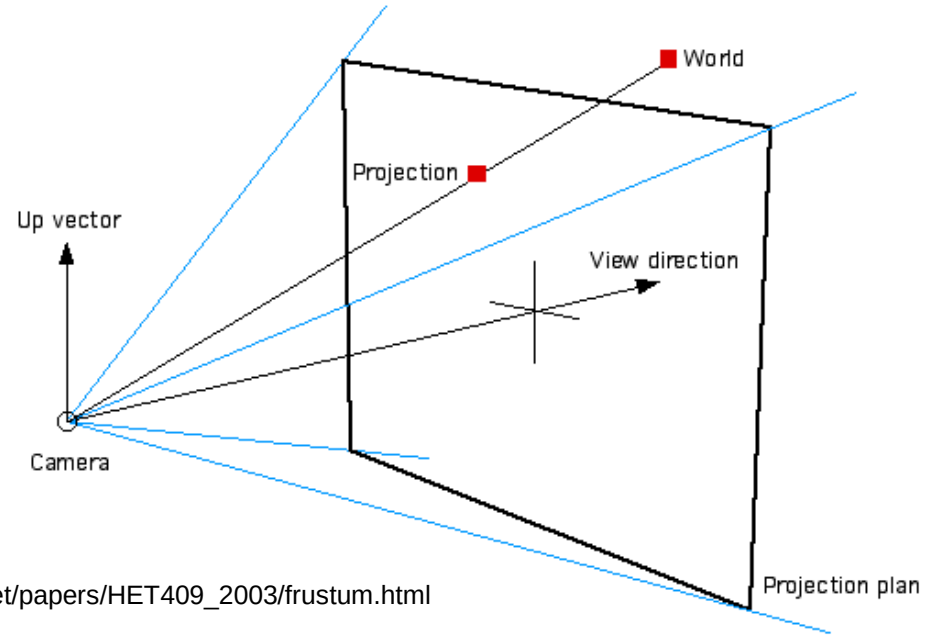


Eye ray and camera

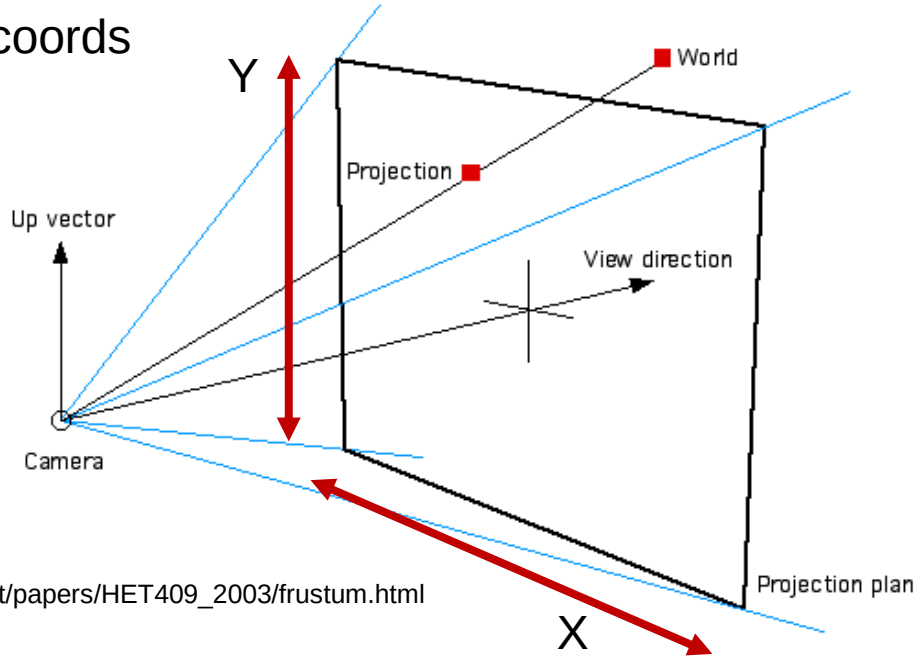
- Simplified Pinhole camera
  - Eye position: e
  - Orthogonal basis: u,v,w (right, up, view) directions
  - Field of view: alpha
  - Aspect ratio: w/h



http://paulbourke.net/papers/HET409_2003/frustum.html

Eye ray and camera

- Simplified Pinhole camera
  - Eye position: e
  - Orthogonal basis: u,v,w (right, up, view) directions
  - Field of view: alpha
  - Aspect ratio: w/h
- Image coordinates
  - Normalized image coords
  - X in [-1,1]
  - Y in [-1,1]



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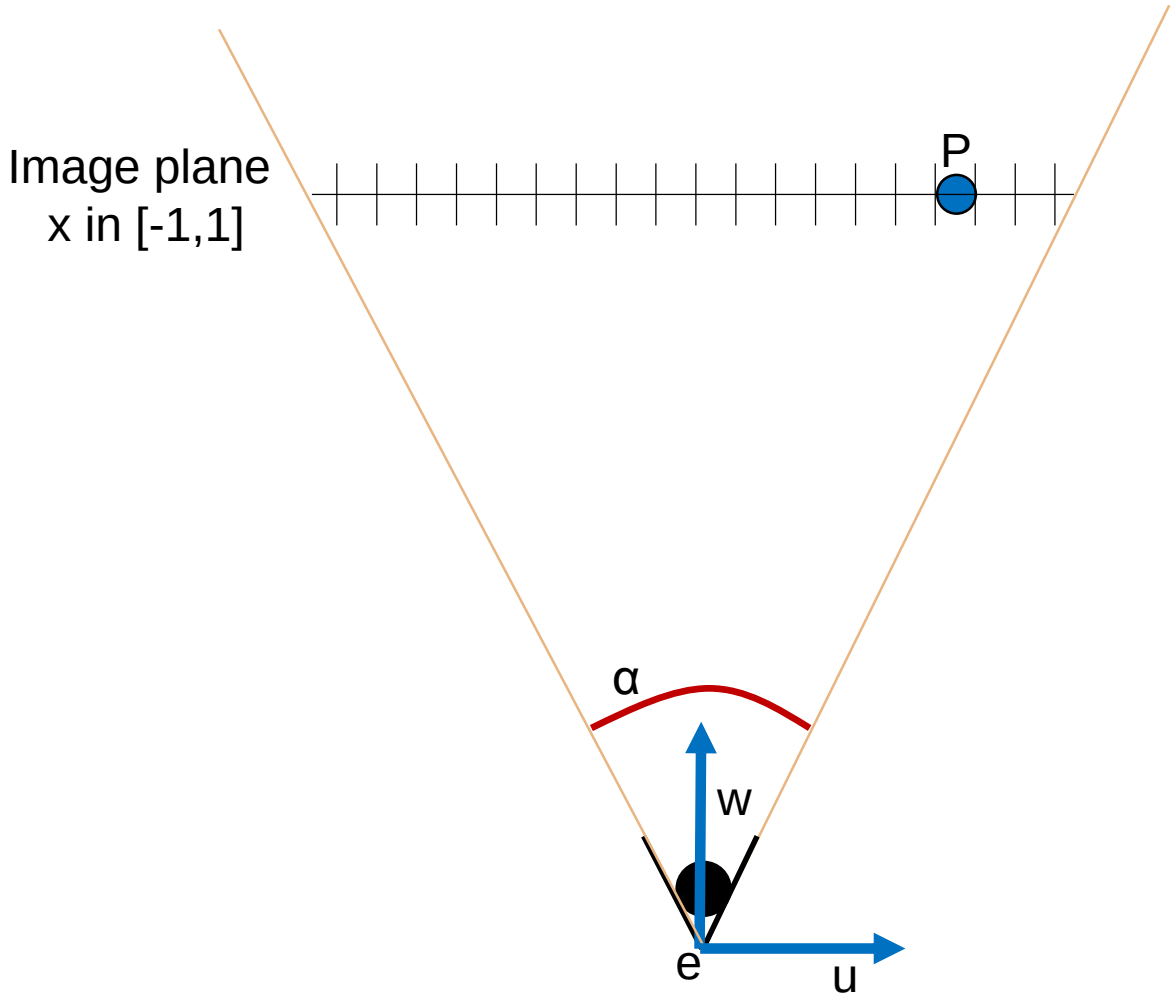
Ray generation



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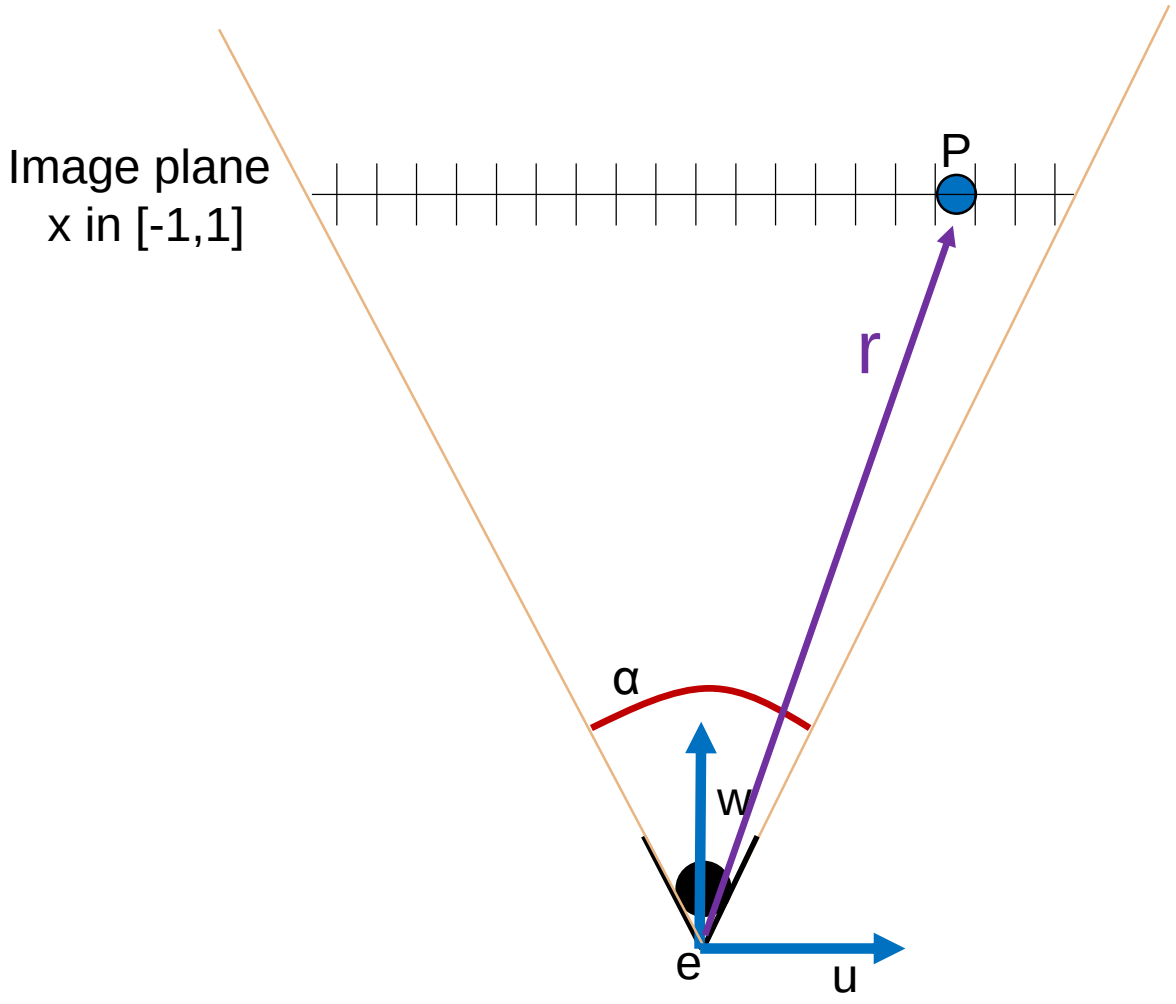
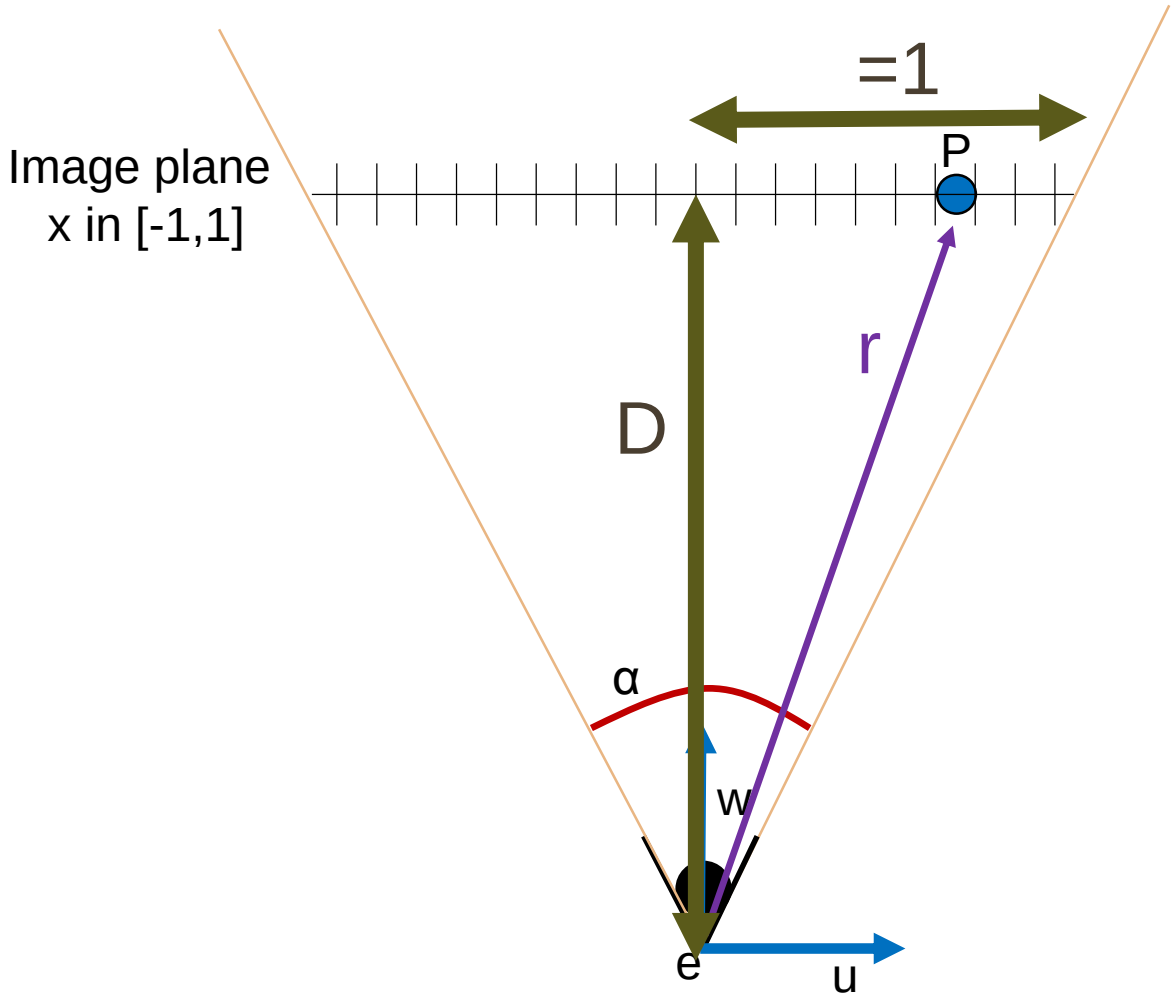


Goal: find r

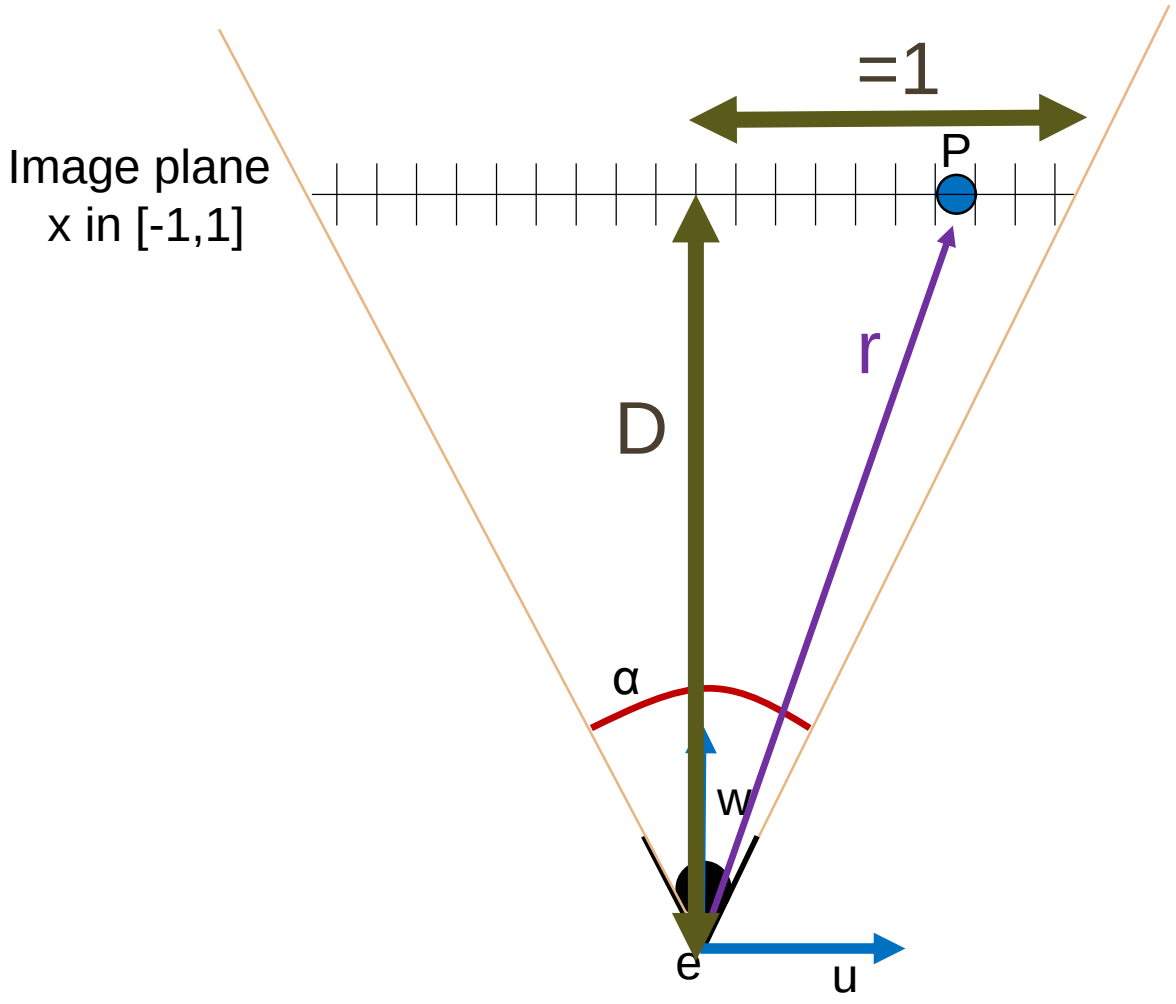
Ray generation



Goal: find r

D = ?

Ray generation

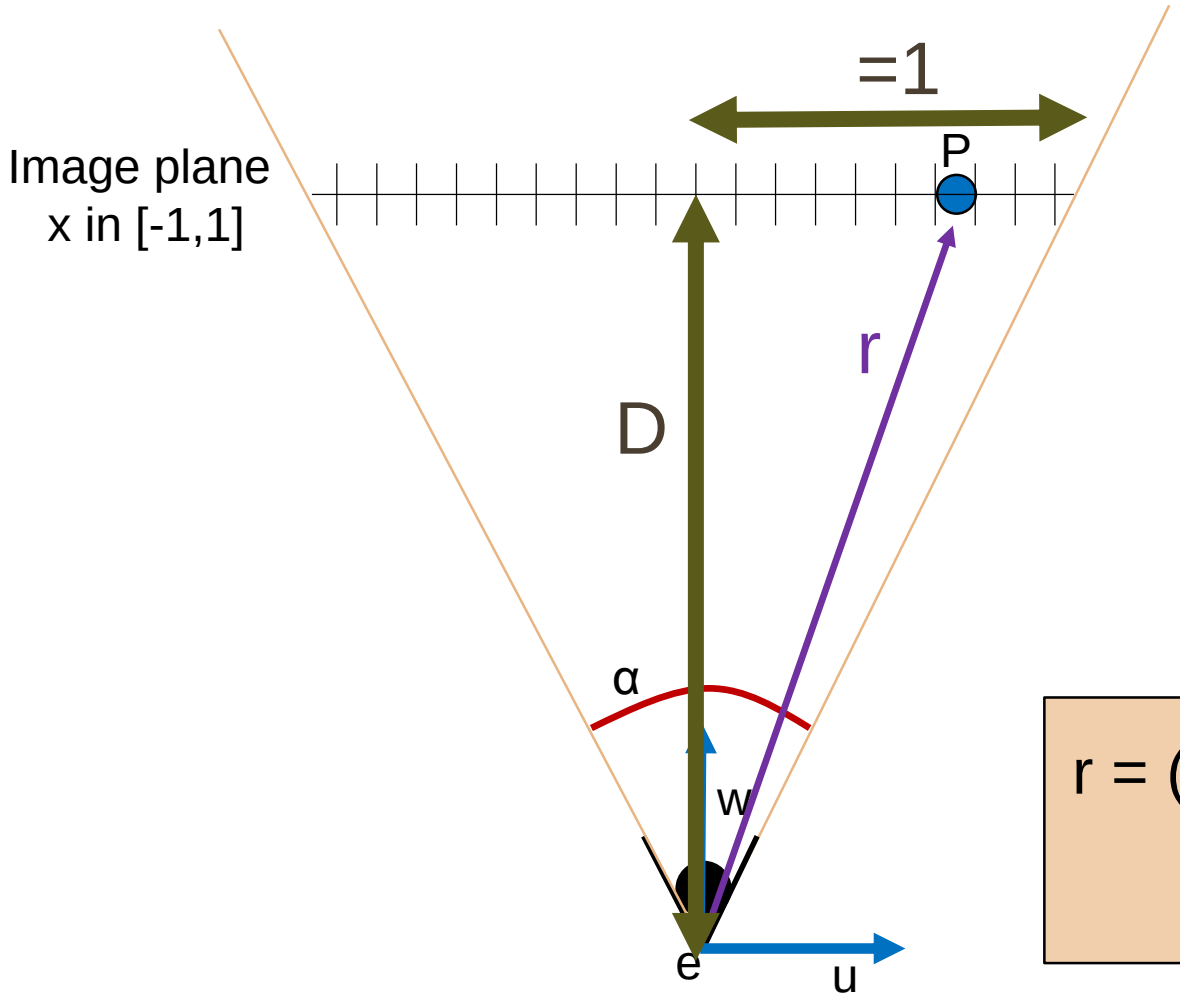


Goal: find r

$$\tan\frac{\alpha}{2} = \frac{1}{D}$$

$$D = \frac{1}{\tan(\alpha/2)}$$

Ray generation



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$$\tan\frac{\alpha}{2} = \frac{1}{D}$$

$$D = \frac{1}{\tan(\alpha/2)}$$

r = (x*u,D*w), normalized

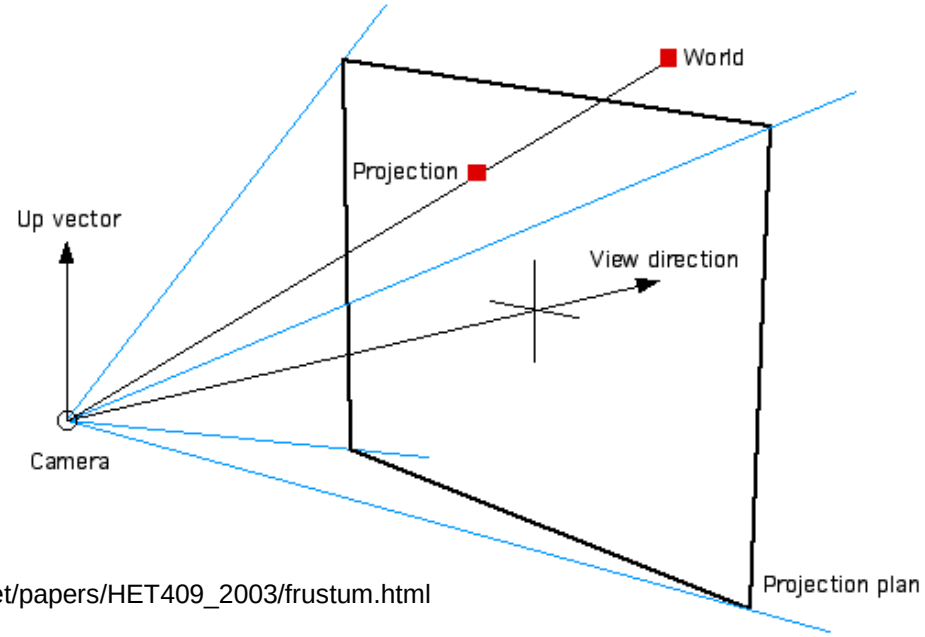
P(t) = e + t*r

Eye ray and camera

- In 3D

$$r = (x*u, aspect*y*v, D*w), \text{ normalized}$$

$$P(t) = e + t*r$$



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Eye ray and camera

- Persective

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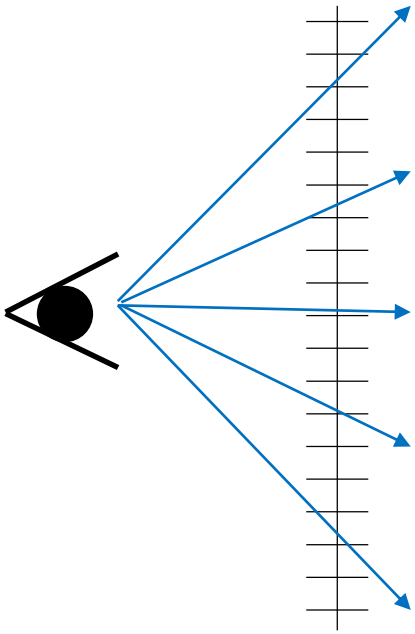

camera Image plane

Eye ray and camera

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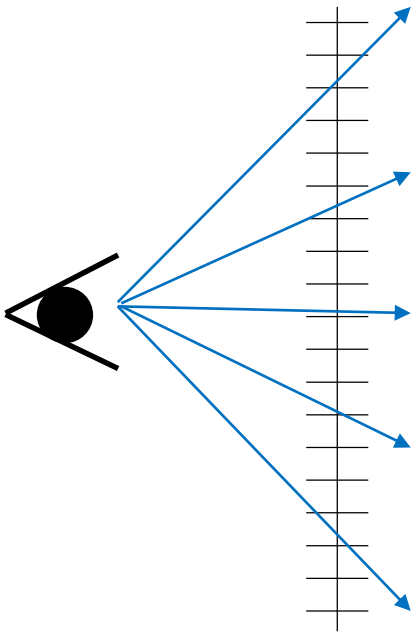
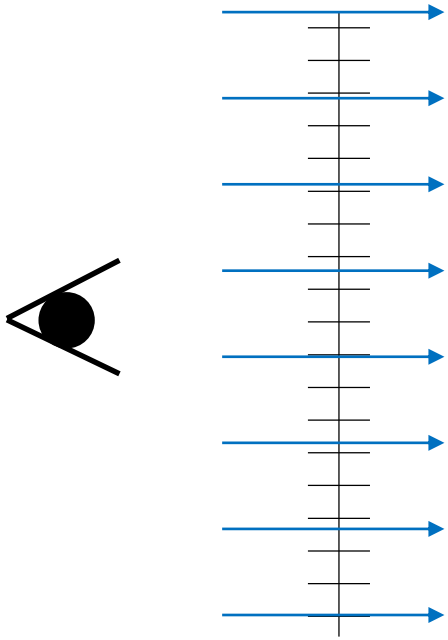


camera Image plane

- Orthographic



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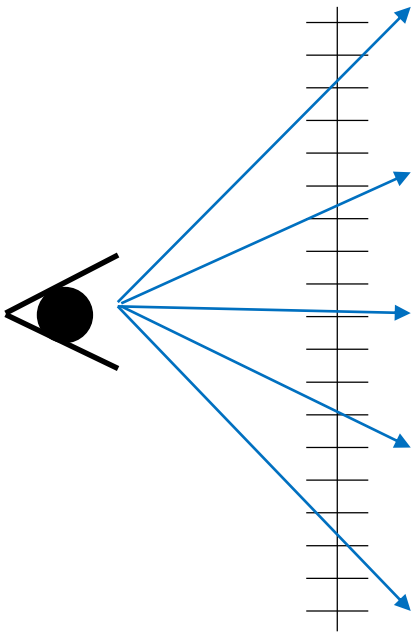
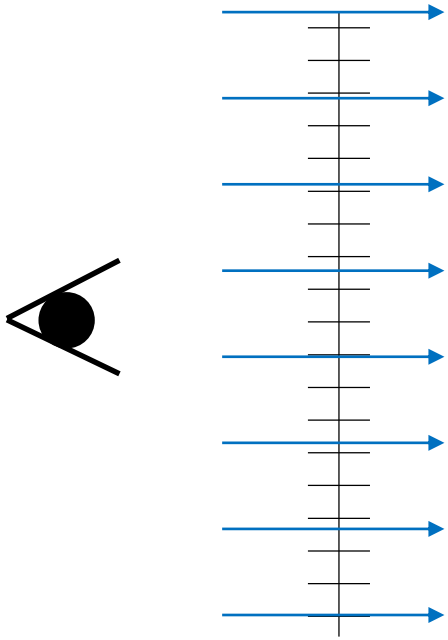


camera Image plane

- Orthographic

P(t) = o + t*w
o = e + x*size*u + y*size*v



camera Image plane

Ray-casting: summary

- For ~~each pixel~~
  - Compute eye ray
  - ~~For each object~~
    - Check ray-object intersection
    - Get closest intersection
    - Shade depending on light and normal vector

OK!

Finding intersection point and normal is the central part of ray-casting!

Ray-casting: summary

- For each pixel
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    - Check ray-object intersection ?
    - Get closest intersection
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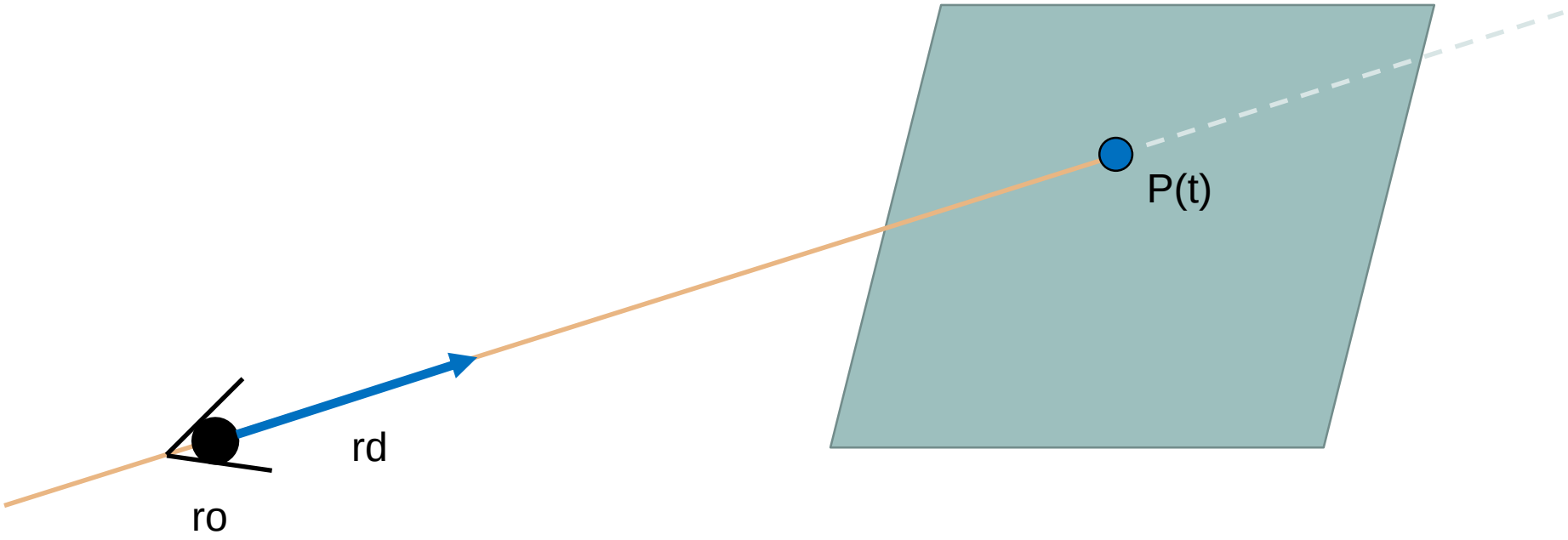
Finding intersection point and normal is the central part of ray-casting!

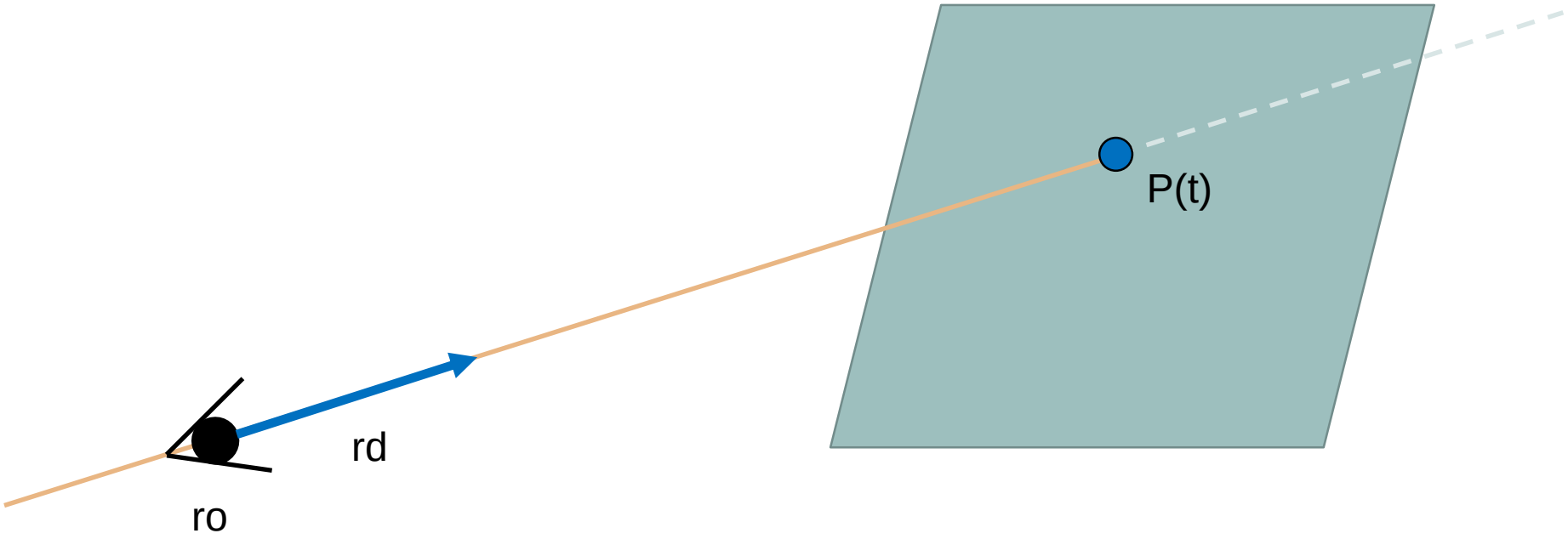
Ray-plane intersection

- Parametric ray equation: $P(t) = r_o + r_d * t$



Ray-plane intersection

- Parametric ray equation: $P(t) = r_o + r_d * t$
- Implicit plane equation: $Ax + By + Cz + D = 0$



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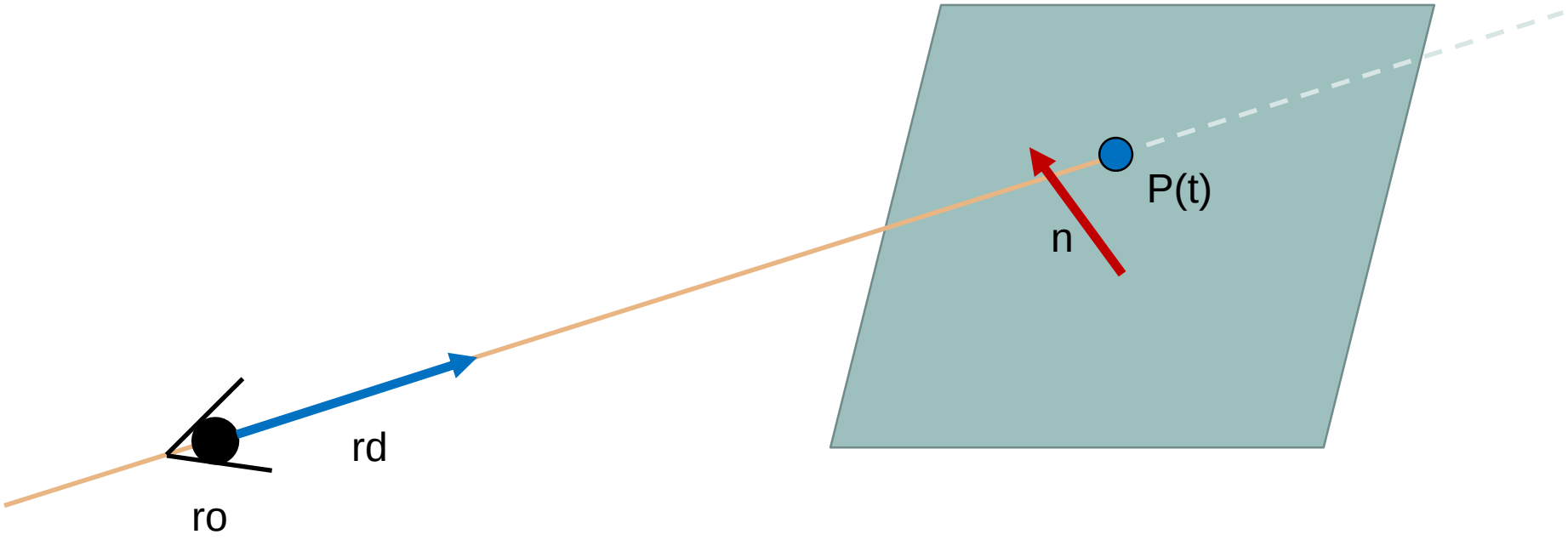

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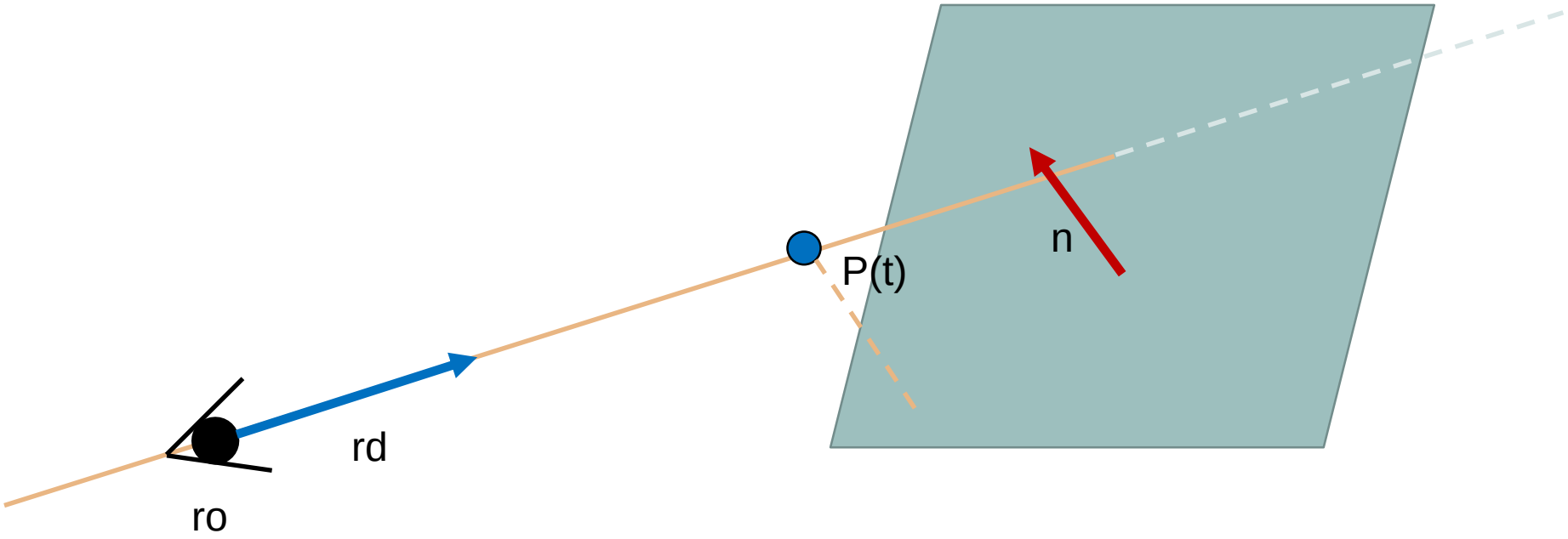
$$n \cdot P + D > 0$$



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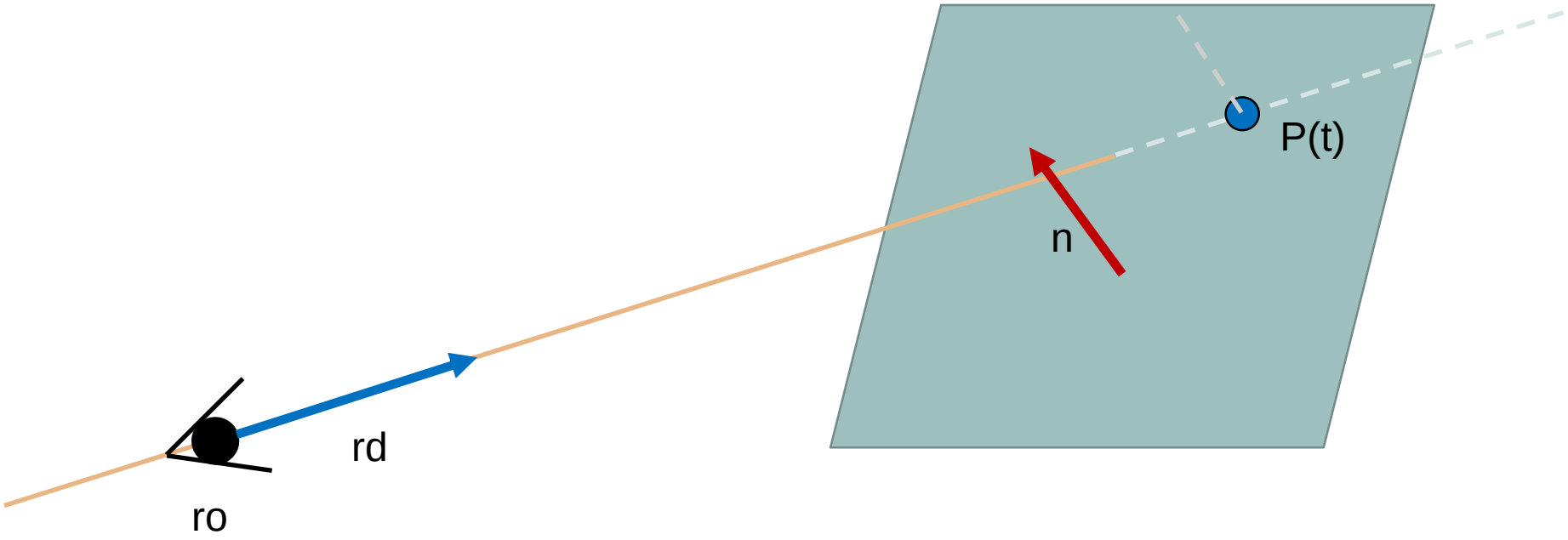

Ray-plane intersection

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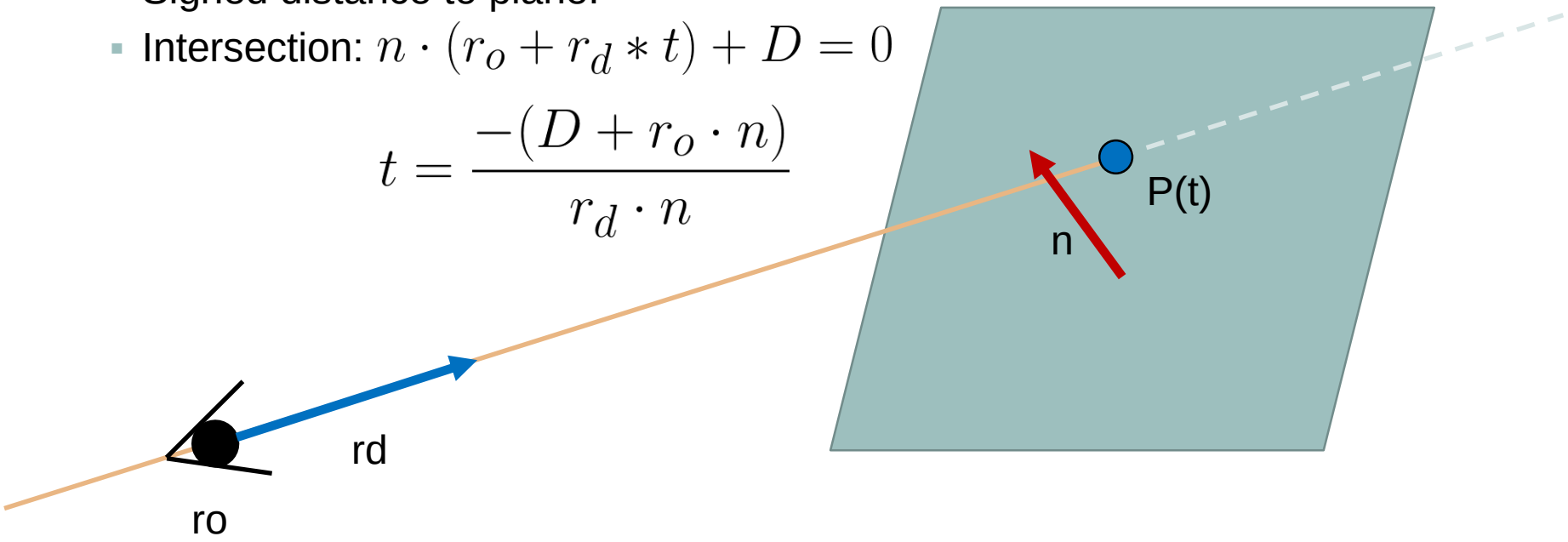
- Implicit plane equation: $Ax + By + Cz + D = 0$

$$n \cdot P + D = 0$$

  - Signed distance to plane!
  - Intersection: $n \cdot (r_o + r_d * t) + D = 0$

$$t = \frac{-(D + r_o \cdot n)}{r_d \cdot n}$$



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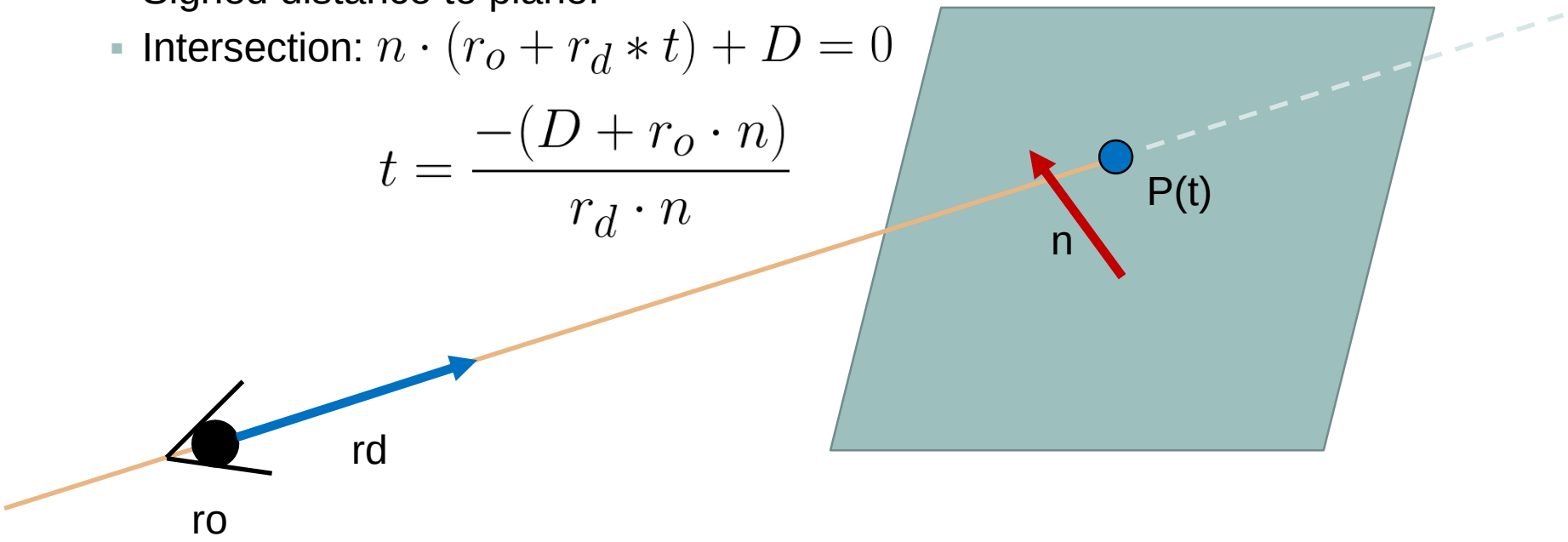
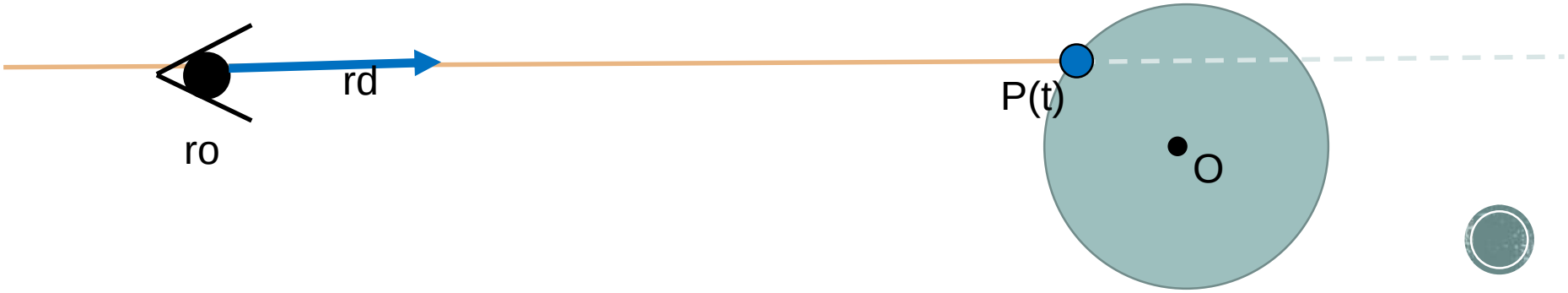


  - Normal: constant (n)

Ray-sphere intersection

- Parametric ray equation: $P(t) = r_o + r_d * t$
- Implicit sphere equation: $||P - O|| - r^2 = 0$



Ray-sphere intersection

- Parametric ray equation: $P(t) = r_o + r_d * t$
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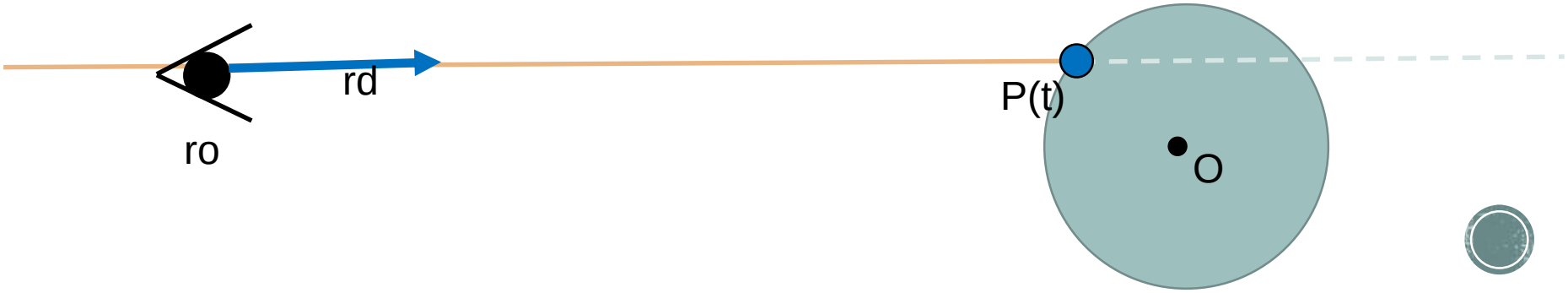

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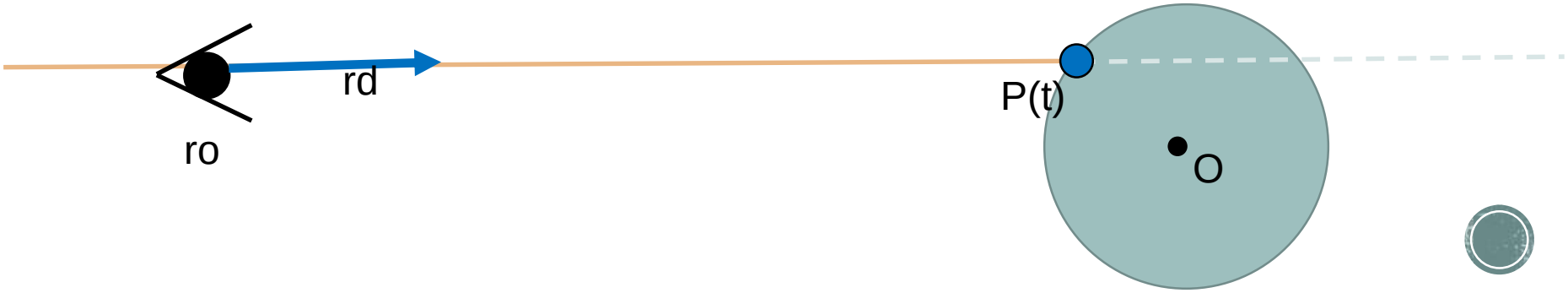
- Parametric ray equation: $P(t) = r_o + r_d * t$
- Implicit sphere equation: $||P - O|| - r^2 = 0$
  - $||r_o + r_d * t - O|| - r^2 = 0$
  - $(r_o + r_d * t - O) \cdot (r_o + r_d * t - O) - r^2 = 0$



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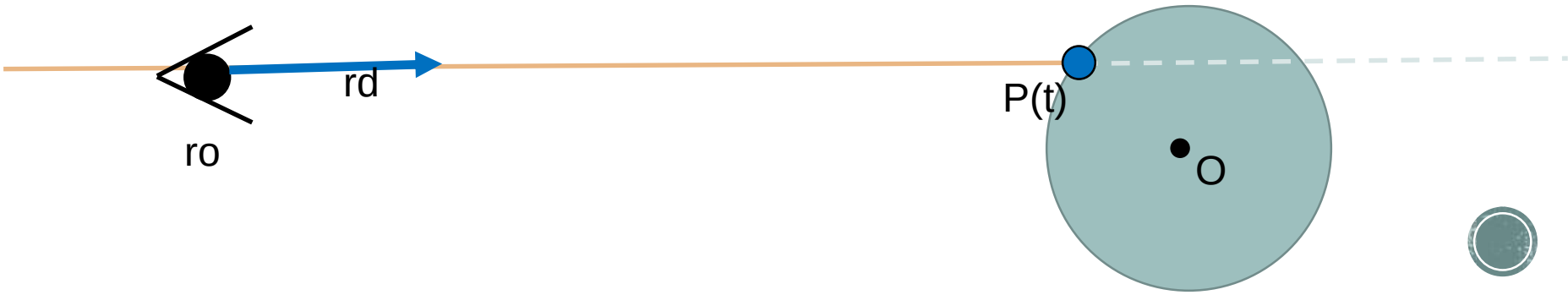
  - $||r_o + r_d * t - O|| - r^2 = 0$
  - $(r_o + r_d * t - O) \cdot (r_o + r_d * t - O) - r^2 = 0$
  - $(r_d \cdot r_d)t^2 + (2r_o \cdot r_d - 2r_d \cdot O)t + (r_o \cdot r_o - 2r_o \cdot O + O \cdot O - r^2) = 0$



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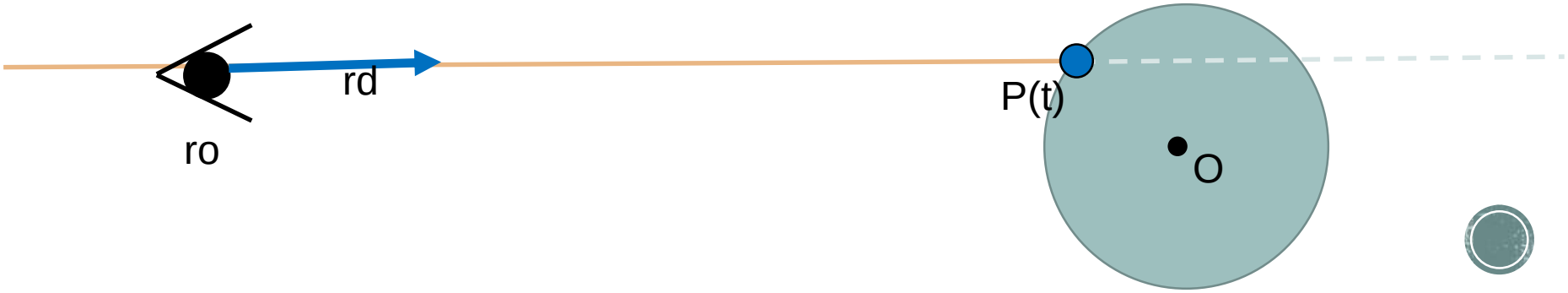
  - $(r_o + r_d * t - O) \cdot (r_o + r_d * t - O) - r^2 = 0$
  - $\boxed{(r_d \cdot r_d)}t^2 + \boxed{(2r_o \cdot r_d - 2r_d \cdot O)}t + \boxed{(r_o \cdot r_o - 2r_o \cdot O + O \cdot O - r^2)} = 0$
  - $\rightarrow at^2 + bt + c = 0, \; a = 1$



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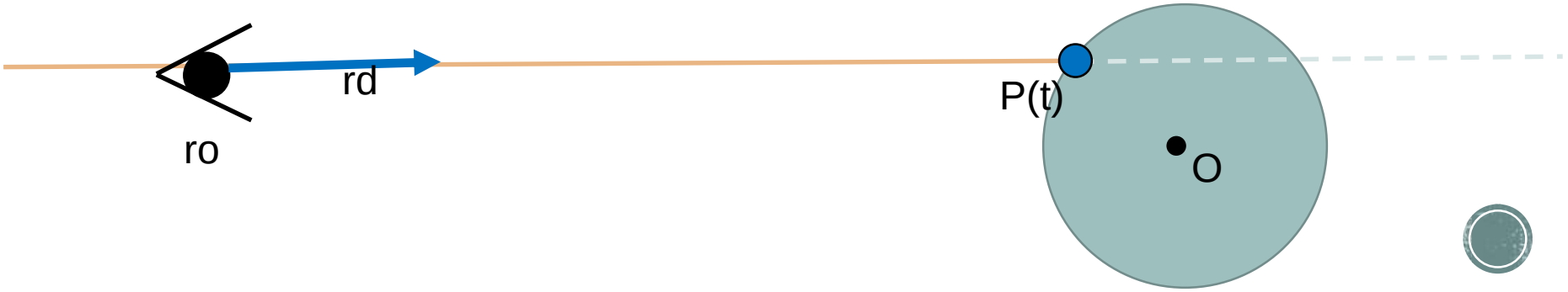
$$d = \sqrt{(b^2 - 4ac)}$$

$$t = \frac{-b \pm d}{2a}$$



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  - $(r_d \cdot r_d)t^2 + (2r_o \cdot r_d - 2r_d \cdot O)t + (r_o \cdot r_o - 2r_o \cdot O + O \cdot O - r^2) = 0$
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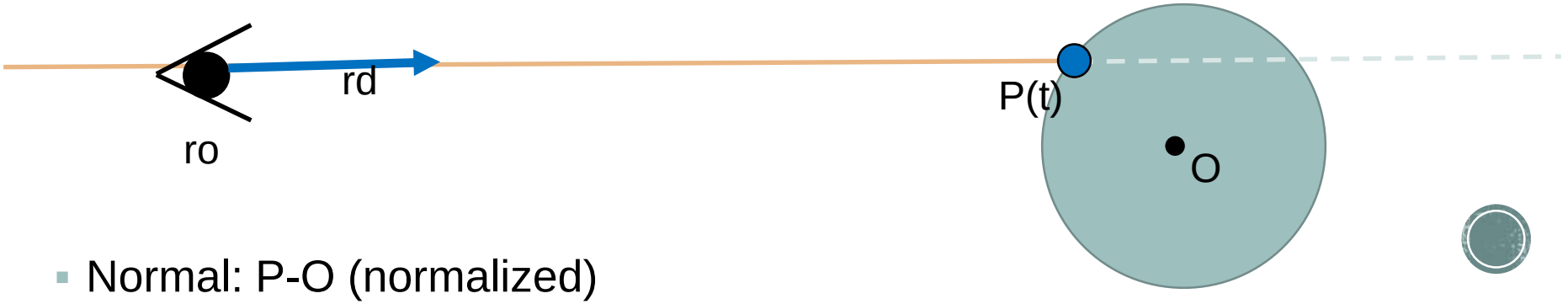
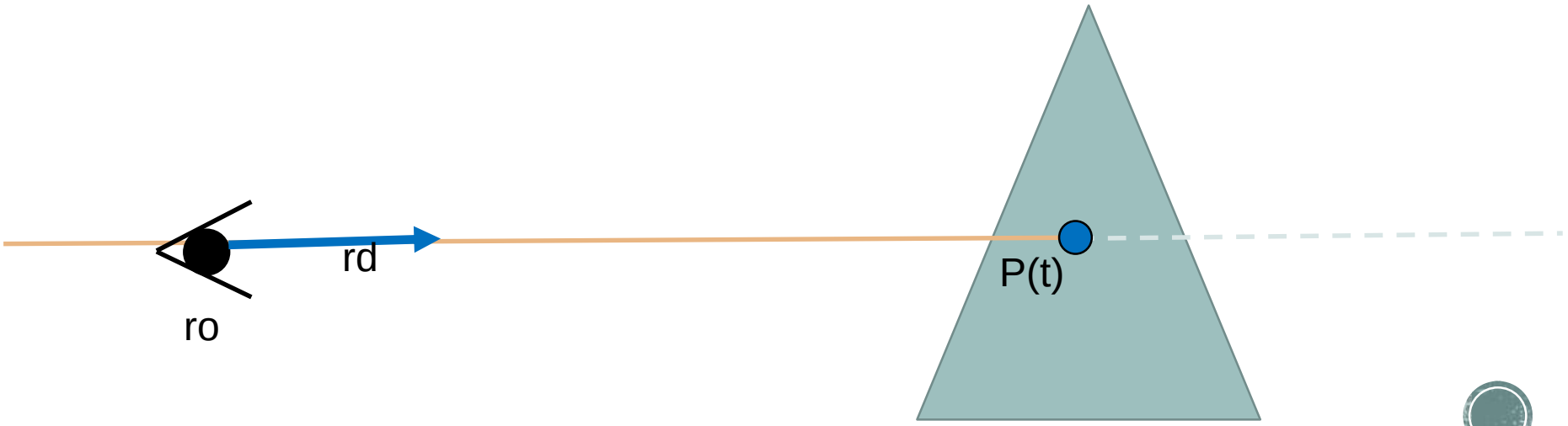


- Normal: P-O (normalized)

Ray-triangle intersection

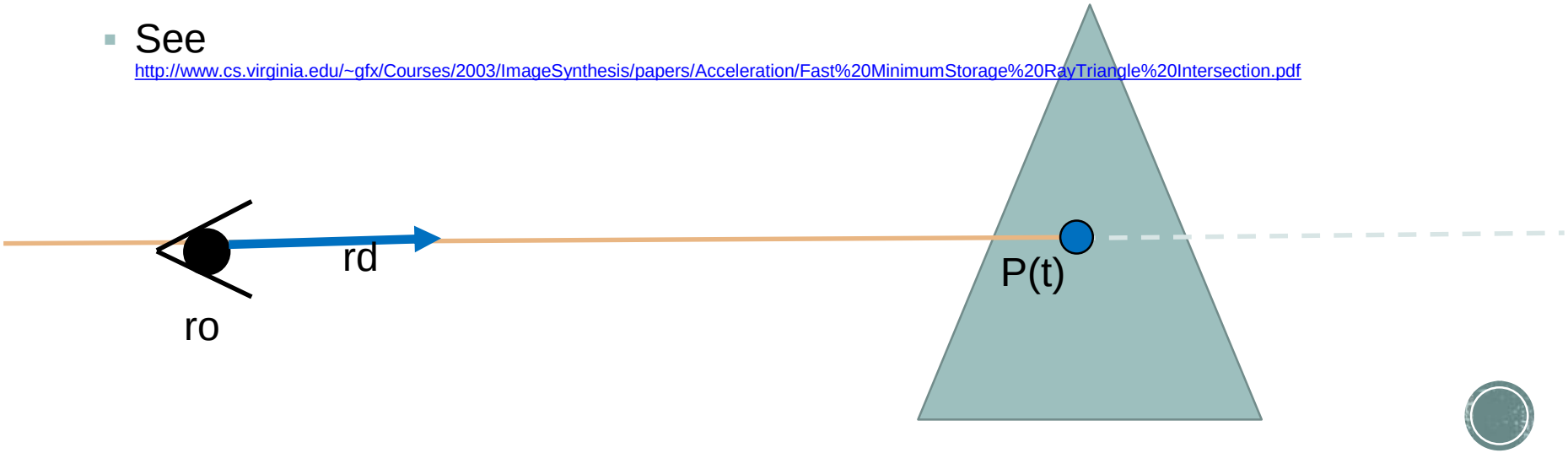
- Ray-plane intersection
- Then test each edge…



Ray-triangle intersection

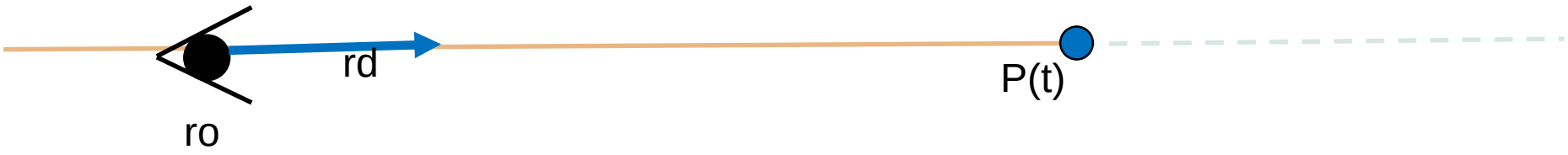
- Ray-plane intersection
- Then test each edge…

- Better: parametric solution [Moller & Trumbore 97]
  - $T(u,v) = (1-u-v)V_0 + uV_1 + vV_2, \qquad u \geq 0,\ v \geq 0 \qquad \text{and } u+v \leq 1.$
  - $O + tD = (1-u-v)V_0 + uV_1 + vV_2$
  - $\begin{bmatrix} -D, & V_1 - V_0, & V_2 - V_0 \end{bmatrix} \begin{bmatrix} t \\ u \\ v \end{bmatrix} = O - V_0$
  - See http://www.cs.virginia.edu/~gfx/Courses/2003/ImageSynthesis/papers/Acceleration/Fast%20MinimumStorage%20RayTriangle%20Intersection.pdf



Other intersections

- Cone, cylinder, elipsoid
  - Similar to sphere
- Box
  - 3 front facing planes
- Convex polygon
  - Similar to triangles
- Concav polygon
  - More complex point-in-polygon test



Ray-casting: summary

- For each pixel
  - Compute eye ray
  - For each object
    - Check ray-object intersection **OK**
    - Get closest intersection
    - Shade depending on light and normal vector

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- For each pixel
  - Compute eye ray
  - For each object
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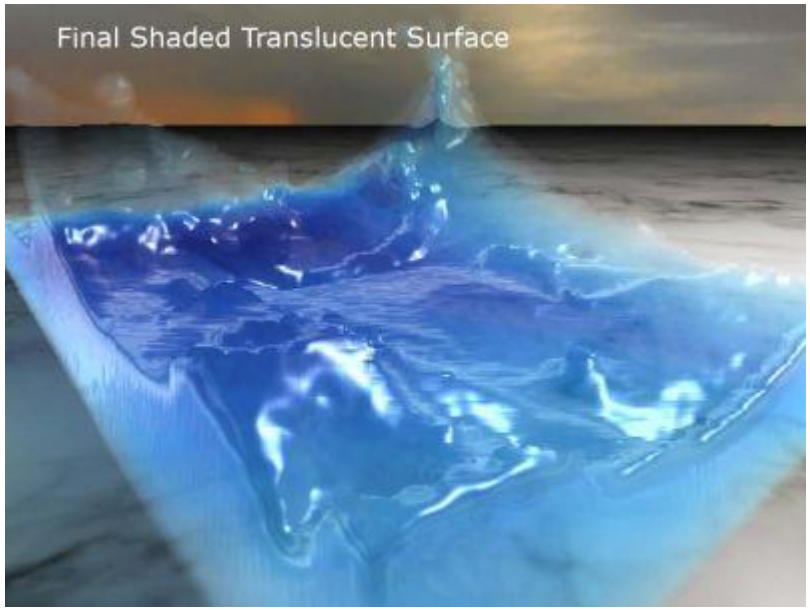
What if intersection cannot be computed analytically?



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