

# A Novel Profit Maximizing Metric for Measuring Classification Performance of Customer Churn Prediction Models

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**Abstract**—The interest for data mining techniques has increased tremendously during the past decades, and numerous classification techniques have been applied in a wide range of business applications. Hence, the need for adequate performance measures has become more important than ever. In this paper, a cost-benefit analysis framework is formalized in order to define performance measures which are aligned with the main objectives of the end users, i.e., profit maximization. A new performance measure is defined, the expected maximum profit criterion. This general framework is then applied to the customer churn problem with its particular cost-benefit structure. The advantage of this approach is that it assists companies with selecting the classifier which maximizes the profit. Moreover, it aids with the practical implementation in the sense that it provides guidance about the fraction of the customer base to be included in the retention campaign.

**Index Terms**—Data mining, classification, performance measures



## 1 INTRODUCTION

As a result of the steep growth in computational power, the interest for data mining techniques has increased tremendously the past decades. A myriad of classification techniques has been developed and is being used in a wide range of business applications. As more and more methods are elaborated, the need for adequate performance measures has become more important than ever before. There has been a lot of attention for the receiver operating characteristic (ROC) curve, which is a graphical representation of the classification performance for varying thresholds [1]. However, rather than visually comparing curves, practitioners prefer to capture the performance of a classification method in a single number. A very popular and straightforward concept is the area under the ROC curve (AUC), which is closely related to the Gini coefficient and the Kolmogorov-Smirnov statistic. The problem with these measures is that they implicitly make unrealistic assumptions about misclassification costs. The H measure is a new approach to performance measurement, which overcomes this problem and focuses on misclassification costs [2].

In this paper, not only the misclassification costs, but also the benefits originating from a correct classification are explicitly taken into account. The main rationale is that the most important goal for practitioners is profit maximization. In Section 2, a cost-benefit analysis framework will be worked out, in which two types of performance measures will be defined. The first metric is the maximum profit (MP), whereas the second metric is the expected maximum profit (EMP). The difference between both measures is that MP is a deterministic approach, which assumes that all parameters related to the costs and benefits are accurately known. The EMP measure on the other hand defines a probability distribution for the cost and benefit parameters, and is a probabilistic approach. Analogously to the H measure, also EMP is related to the ROC curve of the classifier, as will be discussed in Section 3.

Due to the multitude of business situations in which classification methods are employed, it is difficult, if not impossible, to define one single profit driven performance measure. Section 4 will focus on the prediction of customer churn, which has become a very important business problem. During the last decade, the number of mobile phone users has increased drastically, with expectations of 5.6 billion mobile phone subscribers in 2011,<sup>1</sup> which is around 80 percent of the world population. Hence, telecommunication markets are getting saturated, particularly in developed countries, and the emphasis is shifting from attraction of new customers to retention of the existing customer base. In this context, customer churn prediction models play a crucial role and they are increasingly being researched (see, e.g., the extensive literature overview given by Verbeke et al. [3]) and new approaches such as the use of social network data are explored (see among others [4]). When investigating and comparing these data mining techniques for customer churn prediction, it is imperative

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to have an adequate performance measure. Therefore, with the guidance of the cost-benefit framework, a novel performance measure which consistently incorporates the losses and gains will be developed. The main advantage of this metric is that it not only unambiguously identifies the classifier which maximizes the profit for a given customer retention campaign, but also determines the fraction of the customer base which should be targeted to maximize the profit. This is a crucial help for practitioners, since deviating from the optimal fraction leads to suboptimal profits. Section 5 explores the link with the H measure and shows that the H measure can be used as an approximation for the EMP measure for customer churn. Finally, the developed performance measures will be tested in an extensive case study, of which the findings are reported in Section 6.

## 2 THE COST-BENEFIT ANALYSIS FRAMEWORK

Measuring the performance of classifiers is essential for identifying superior classification techniques [5]. This paper focusses on classification problems with a binary outcome, i.e., it deals with the two-class case, where instances belong either to class 0 or to class 1. Many classifiers produce a continuous score,  $s(\mathbf{x})$ , which is a function of the attribute vector  $\mathbf{x}$  and aims to discriminate between two classes. It is assumed that the instances from class 0 have a lower score than the instances from class 1; if this is not true, the score could be multiplied with minus one. To classify an instance, a cutoff  $t$  has to be chosen, where all instances with  $s$  smaller than  $t$  are classified as a zero, whereas instances for which  $s$  is larger than  $t$  are classified as ones.

Throughout this paper, the following notation will be adopted. The number of instances in the data set is denoted with  $N$ , whereas the prior probabilities of instances belonging to class 0 or 1 are denoted with  $\pi_0$  and  $\pi_1$ , respectively. Two types of instances are considered, those from class 0 and 1, and for both groups of observations, the probability distribution of the classification scores can be defined. The probability density functions are  $f_0(s)$  and  $f_1(s)$ , whereas the cumulative density functions are  $F_0(s)$  and  $F_1(s)$  for class 0 and 1, respectively. Usually, the outcome of a classification task is used as input to a business process leading to benefits for correct classifications and costs for misclassifications. The cost or benefit related to classifying an instance from class  $j$  to class  $i$  is denoted with  $c(i|j)$ . By convention, both costs and benefits will be positive or equal to zero. Hence, in the cost-benefit analysis, a minus sign will be applied for the misclassification costs.

In general, a classification exercise leads to a confusion matrix as shown in Table 1. For example, the upper right cell contains the instances belonging to class 0 which are incorrectly classified into class 1. The number of instances in this category is given by  $\pi_0(1 - F_0(t))N$ , whereas the cost of such a misclassification is  $c(1|0)$ . For notational convenience, the costs and benefits are put to  $b_0$ ,  $c_0$ ,  $b_1$ , and  $c_1$ , as indicated in Table 1. By multiplying the total number of observations in a certain cell with the classification cost or benefit (between square brackets), and summing this over all cells, one obtains the total classification profit, as will be discussed later.

In the literature, several performance measures have been proposed. An overview of performance measures for

TABLE 1  
Confusion Matrix Containing the Number of Instances Classified in Each Cell

		Classified into	
		Class 0	Class 1
Belongs to	Class 0	$\pi_0 F_0(t) N$ [ $c(0 0) = b_0$ ]	$\pi_0 (1 - F_0(t)) N$ [ $c(1 0) = c_0$ ]
	Class 1	$\pi_1 F_1(t) N$ [ $c(0 1) = c_1$ ]	$\pi_1 (1 - F_1(t)) N$ [ $c(1 1) = b_1$ ]

Between square brackets, the related classification costs and benefits are given.

classification techniques can be found in [6] and [7]. In the data mining community, the most well-known measures include:

$$\text{Accuracy} = \pi_0 F_0(t) + \pi_1 (1 - F_1(t)),$$

$$\text{Sensitivity} = F_0(t),$$

$$\text{Specificity} = 1 - F_1(t),$$

$$\text{AUC} = \int F_0(s) f_1(s) ds.$$

The accuracy of a classifier measures the percentage of correctly classified observations. The sensitivity represents the proportion of zeros which are correctly classified, whereas the specificity measures the proportion of ones correctly predicted. Most of these performance measures do not take into account the misclassification costs, and are only valid when the misclassification costs are equal.

There has been much attention for cost-sensitive learning. For example, Domingos [8] proposed a general method to produce cost-sensitive classifiers, [9] combined ROC curve analysis with cost distribution information, [10] developed an ontology-based approach for cost-sensitive classification, [11] used over- and undersampling and threshold moving (and an ensemble of these methods) for cost-sensitive learning with neural networks, and more recently, [2] introduced the H-measure, which takes into account misclassification costs. However, as pointed out by Elkan [12]:

“Although most recent research in machine learning has used the terminology of costs, doing accounting in terms of benefits is generally preferable, because avoiding mistakes is easier, since there is a natural baseline from which to measure all benefits, whether positive or negative.”

So even though a cost-only approach could be mathematically equivalent, in this study the benefits will be taken explicitly into account since this allows for a more straightforward interpretation by the practitioner.

The central concept in this paper is the cost-benefit framework, i.e., the fact that a different benefit or cost is related to each entry in the confusion matrix. The main purpose is to work out a performance metric which selects the classifier with the highest profit. This metric is used to select the best performing technique, and thus can be used with all classification algorithms. The average classification profit of a classifier is defined as follows:

**Definition 1.** *The average classification profit of a classifier is the profit generated by the employment of this classifier. It is*

the sum of the classification benefits minus the classification costs, divided by the number of instances.

The average classification profit can be expressed as a function of the classification threshold,  $t$ :

$$P(t; b_0, c_0, b_1, c_1) = b_0\pi_0F_0(t) + b_1\pi_1(1 - F_1(t)) - c_0\pi_0(1 - F_0(t)) - c_1\pi_1F_1(t), \quad (1)$$

with  $b_0$ ,  $c_0$ ,  $b_1$ , and  $c_1$  parameters as defined by Table 1. These parameters are positive unless explicitly stated otherwise. Rearranging yields

$$P(t; b_0, c_0, b_1, c_1) = (b_0 + c_0)\pi_0F_0(t) - (b_1 + c_1)\pi_1F_1(t) + b_1\pi_1 - c_0\pi_0. \quad (2)$$

The average classification profit depends on the cutoff,  $t$ . For a perfect classifier at the optimal threshold, it holds that  $F_0 = 1$  and  $F_1 = 0$ , which results in an average classification profit equal to  $b_0\pi_0 + b_1\pi_1$ . For a fixed classifier and given costs and benefits, the threshold  $t$  is to be optimized, resulting in the maximum profit of a classifier.

**Definition 2.** The maximum profit, *MP*, of a classification technique is the profit resulting from the classification outcome when the optimal cutoff,  $T$ , is used.

The maximum profit is a measure for the effectiveness of the technique, since profit maximization is the ultimate aim. This approach to classification performance measurement has already been explored by Verbeke et al. [13]. MP is analytically expressed as:

$$MP = \max_{\forall t} P(t; b_0, c_0, b_1, c_1) = P(T; b_0, c_0, b_1, c_1), \quad (3)$$

with  $T$  the optimal threshold. The optimal threshold satisfies the first order condition for the maximization of the average profit  $P$ :

$$\frac{f_0(T)}{f_1(T)} = \frac{\pi_1(b_1 + c_1)}{\pi_0(b_0 + c_0)} = \frac{\pi_1\theta}{\pi_0}. \quad (4)$$

The parameter  $\theta = (b_1 + c_1)/(b_0 + c_0)$ , the *cost benefit ratio*, is introduced for notational convenience. It also indicates that the optimal threshold and profit depends on a ratio of costs and benefits, and thus is not dependent on the measurement scale. Since it is assumed that the cost-benefit parameters  $(b_0, c_0, b_1, c_1)$  are positive, the value of  $\theta$  ranges from zero to plus infinity. Equation (4) has an appealing graphical interpretation on the ROC-curve, as will be shown in Section 3.1.

The MP measure is a *deterministic* approach to cost-benefit analysis, since the costs and benefits are supposed to be known. In reality, however, it is not straightforward to estimate precise values for these parameters. Therefore, this paper proposes to adopt a probability distribution for the cost and benefit parameters, leading to a *probabilistic* cost-benefit-based performance measure, the *expected maximum profit* of a classifier.

**Definition 3.** The expected maximum profit, *EMP*, is the expectation of the maximal profit of a classifier with respect to the distribution of classification costs.

The expected maximum profit measures the effectiveness of a classification technique, taking into account the uncertainty of the classification costs and benefits and is a genuine contribution of this paper.

Let  $w(b_0, c_0, b_1, c_1)$  be the joint probability density of the classification costs, then the expected maximal profit is equal to

$$EMP = \int_{b_0} \int_{c_0} \int_{b_1} \int_{c_1} P(T(\theta); b_0, c_0, b_1, c_1) \cdot w(b_0, c_0, b_1, c_1) db_0 dc_0 db_1 dc_1. \quad (5)$$

Equation (5) is the most general expression for the expected maximum profit for a given classifier. Note that for *each* combination of  $(b_0, c_0, b_1, c_1)$ , the optimal threshold  $T$  is determined through (4). The profit is then calculated for the optimal threshold and weighed with the probability density for this particular combination of classification costs. Integrating over all possible benefits and costs leads to the expected maximum classification profit. When the costs are known with certainty, the function  $w(b_0, c_0, b_1, c_1)$  is a Dirac impulse at the known values, and EMP simplifies to MP. Although the previous discussion only focussed on the profit related to a classification outcome, there is a link to the ROC curve of the classifier, as will be explored in the next section.

### 3 THE RECEIVER OPERATING CHARACTERISTIC CURVE AND THE H-MEASURE

The receiver operating characteristic curve is a concept which has been extensively used in the machine learning community [1]. Section 3.1 discusses the ROC curve in the context of cost-benefit analysis, along with a derived performance measure, the Area under the ROC-curve, also known as AUC [14]. However, [2] showed recently that AUC is a flawed measure and proposed an alternative, the H-measure, which will be treated in Section 3.2.

#### 3.1 The ROC-Curve and the Area under the ROC-Curve

A ROC curve is a graphical representation of the classification performance with varying threshold  $t$ . It is a plot of the sensitivity versus one minus the specificity, i.e.,  $F_0(t)$  as a function of  $F_1(t)$ . The interested reader is referred to [1] or [15] for an extensive discussion on ROC-curves. Because ROC-curves are not convenient to compare classifiers, especially when their ROC-curves intersect, the area under the ROC-curve is often used to quantify the performance. A larger AUC would indicate superior performance. The area under the ROC curve, which is closely related to the Gini coefficient and the Kolmogorov-Smirnov statistic, has the following statistical interpretation: the AUC of a classification method is the probability that a randomly chosen positive instance will be ranked higher than a randomly chosen negative instance [1].

Also in the context of the cost-benefit analysis framework, the ROC-curve has its merit. Since each point on the ROC-curve corresponds to a threshold  $t$ , the optimal cutoff  $T$ , is located somewhere on the curve.

**Theorem 1.** *If the ROC-curve is convex<sup>2</sup> and continuously differentiable, the optimal cutoff, for given classification costs  $c_0$  and  $c_1$ , and benefits  $b_0$  and  $b_1$ , corresponds to the point on the ROC-curve for which the tangent slope equals  $\pi_1\theta/\pi_0 = [\pi_1(b_1 + c_1)]/[\pi_0(b_0 + c_0)]$ .*

This theorem is a direct result from the definition of the ROC curve and the first order condition as defined by (4). When the ROC-curve is not convex, and thus the slope is not monotonically decreasing, there may be multiple points on the ROC curve satisfying the first order condition. More specifically, points in the concave region are not optimal for any  $\theta$ , in which case the convex hull needs to be defined.

**Theorem 2.** *The convex hull of a (nonconvex) ROC-curve defines a set of points where each point corresponds to the optimal cutoff for a certain value of the cost benefit ratio  $\theta \in [0, +\infty)$ .*

This theorem is based on the second order condition for profit maximization and is discussed in detail by Fawcett [1]. The interesting implication of this fact is that an integration over a range of  $\theta$  values is equivalent to an integration over the corresponding part of the ROC curve. In fact, every value for  $\theta \in [0, +\infty)$ , has a corresponding isoperformance line with a slope equal to  $\pi_1\theta/\pi_0$ . The optimal cutoff for a given  $\theta$  value is then located where the isoperformance line is tangent to the ROC curve. Thus, by varying  $\theta$  from zero to infinity, each point on the ROC curve is traversed.

This interpretation of an integration over the ROC curve has another very important consequence, as was revealed by Hand [2]. He showed that the popular AUC is equivalent to an expected maximum profit measure. However, the probability density which is implicitly assumed when calculating the AUC depends on the empirical score distribution of the classifier itself. Therefore, AUC is seriously flawed as a performance measure, and Hand proposed an alternative, the H measure, which will be discussed in the next section.

### 3.2 The H-Measure

Hand [2] proposed the H measure as a coherent alternative to the area under the ROC curve. This measure resembles an EMP measure, with the difference that the H measure only explicitly states the misclassification costs and not the benefits. The core of the H measure is the average classification loss,  $Q$ , which is equal to the negative of the average classification profit,  $P$ , with  $b_0 = b_1 = 0$ . Hence, the focus is not on the expected maximum profit, but on the expected minimum loss. Moreover, a variable substitution is carried out:

$$Q(t; c, b) = b \cdot [c\pi_0(1 - F_0(t)) + (1 - c)\pi_1 F_1(t)], \quad (6)$$

with  $c = c_0/(c_0 + c_1)$  and  $b = c_0 + c_1$ . In this case, the cost benefit ratio on which the optimal threshold  $T$  depends, is equal to  $\theta = (1 - c)/c$ .

2. It was already pointed out by Hand [2] that the machine learning community in the context of ROC-curves by convention considers a function  $g(x)$  convex if  $g(\lambda x + (1 - \lambda)y) \leq \lambda g(x) + (1 - \lambda)g(y)$  for  $0 < \lambda < 1$ . A twice differentiable function  $g(x)$  is convex if  $\partial^2 g(x)/\partial x^2 \geq 0$ . The mathematical community on the contrary adopts the definition of convexity with the inequality sign reversed.

To calculate a concrete value for the expected minimum loss, assumptions have to be made regarding the probability density of  $b$  and  $c$ . A first assumption is the independence of  $b$  and  $c$ , namely that  $w(b, c) = u(c)v(b)$  holds true, where  $w(b, c)$  is the joint probability density function of  $b$  and  $c$ , whereas  $u(c)$  and  $v(b)$  are the marginal probability density functions of  $c$  and  $b$ , respectively. The expected minimum loss ( $L$ ) is then equal to

$$L = E[b] \int_0^1 Q(T(c); b, c) \cdot u(c)dc, \quad (7)$$

with  $E[b] = 1$  for an appropriate choice for the unit in which  $b$  is measured. Furthermore, the probability density function of  $c$  is supposed to follow a beta distribution with parameters  $\alpha$  and  $\beta$ , which is characterized as follows:

$$u_{\alpha, \beta}(x) = \begin{cases} \frac{x^{\alpha-1} \cdot (1-x)^{\beta-1}}{B(1, \alpha, \beta)} & \text{if } x \in [0, 1], \\ 0 & \text{else,} \end{cases} \quad (8)$$

with  $\alpha$  and  $\beta$  greater than one, and

$$B(x, \alpha, \beta) = \int_0^x t^{\alpha-1} \cdot (1-t)^{\beta-1} dt. \quad (9)$$

Finally, to arrive at the H measure, a normalization is performed to obtain a performance measure bounded by zero and one:

$$H = 1 - \frac{\int_0^1 Q(T(c); b, c) \cdot u(c)dc}{\pi_0 \int_0^{\pi_1} c \cdot u(c)dc + \pi_1 \int_{\pi_1}^1 (1-c) \cdot u(c)dc}, \quad (10)$$

with  $u(c)$  shorthand notation for  $u_{\alpha, \beta}(c)$ . The denominator gives the misclassification loss for the worst classifier, i.e., a random classifier. Also, the integration over  $c = [0..1]$  corresponds to an integration over  $\theta = [0..+\infty)$ , and thus of a ROC curve tangent slope from plus infinity to zero. Thus, the H measure takes into account the entire ROC curve of a classifier. A close inspection of the H measure shows that only a part of the measure changes with varying classification techniques, holding the data set constant:

$$H = 1 + \frac{H_{var} - \pi_0 \int_0^1 c \cdot u(c)dc}{\pi_0 \int_0^{\pi_1} c \cdot u(c)dc + \pi_1 \int_{\pi_1}^1 (1-c) \cdot u(c)dc}, \quad (11)$$

with  $H_{var}$  defined as:

$$H_{var} = \int_0^1 [\pi_0 c F_0 - \pi_1 (1-c) F_1] \cdot u(c)dc. \quad (12)$$

This variable part of H,  $H_{var}$ , is an expression which will be useful in Section 5.

## 4 COST BENEFIT-BASED PERFORMANCE MEASUREMENT FOR CUSTOMER CHURN PREDICTION

Until now, the performance measures MP and EMP have been discussed in general terms, without any assumptions on the distribution of the cost and benefit parameters other than that their values are assumed to be positive. However, when the cost-benefit framework is to be applied, an

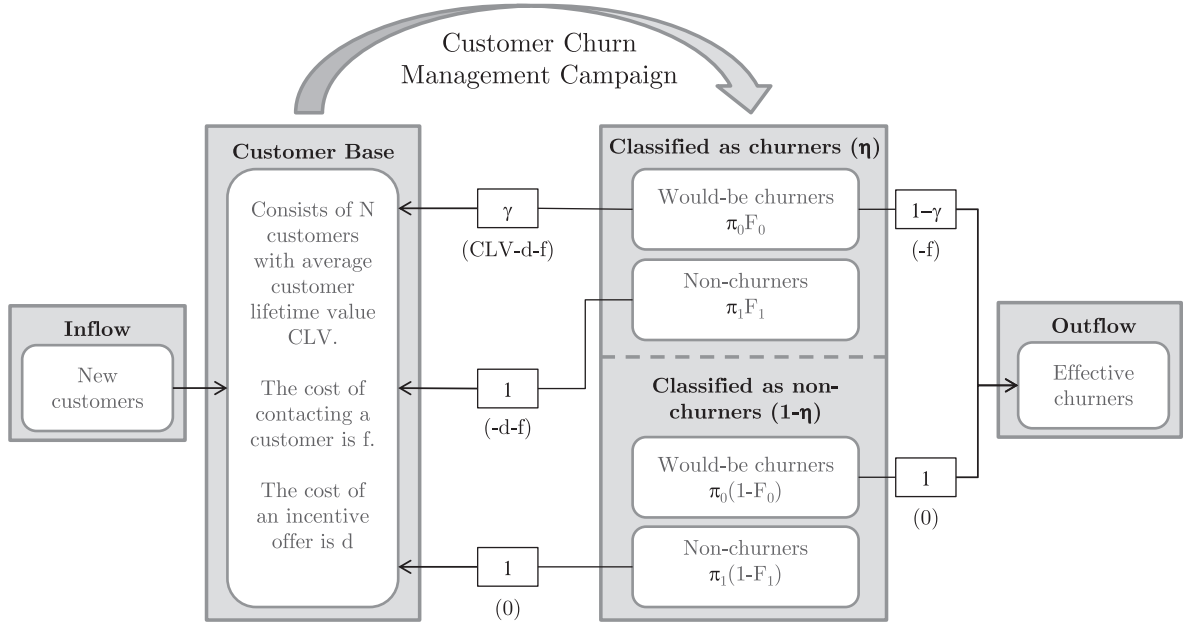


Fig. 1. Schematic representation of customer churn and retention dynamics within a customer base.

interpretation has to be given to the parameters, which requires domain specific knowledge. Section 4.1, will discuss the deterministic approach for performance measurement of customer churn prediction. The probabilistic approach will be treated in detail in Section 4.2.

#### 4.1 The Maximum Profit Criterion for Customer Churn

Fig. 1 schematically represents the dynamical process of customer churn and retention within a customer base. New customers flow into the customer base by subscribing to a service of an operator, and existing customers flow out of the customer base by churning. When setting up a churn management campaign, the fraction  $\eta$  of the customer base with the highest propensity to churn is contacted at a cost  $f$  per person and is offered an incentive with cost  $d$ . In this fraction, there are true would-be churners and false would-be churners. In the latter group everyone accepts the incentive and does not churn, as they never had the intention. From the former group, a fraction  $\gamma$  accepts the offer and thus results in gained customer lifetime value ( $CLV$ ), whereas the fraction  $(1 - \gamma)$  effectively churns. In the fraction  $(1 - \eta)$ , which is not targeted, all would-be churners effectively churn, and all nonchurners remain with the company. The benefits per customer related to each flow are shown between brackets in Fig. 1. These are *incremental* benefits, as compared to not undertaking the customer churn management campaign. This process was described

by Neslin et al. [16], who established the following expression for the total profit of a retention campaign:

$$\text{Profit} = N\eta[(\gamma CLV + d(1 - \gamma))\pi_0\lambda - d - f] - A, \quad (13)$$

with  $\eta$  the fraction of the customer base that is targeted,  $CLV$  the customer lifetime value,  $d$  the cost of the incentive,  $f$  the cost of contacting the customer, and  $A$  the fixed administrative costs. The lift coefficient,  $\lambda$ , is the percentage of churners within the targeted fraction  $\eta$  of customers, divided by the base churn rate,  $\pi_0$ . Lastly,  $\gamma$  is the fraction of the would-be churners accepting the offer, or alternatively it is interpreted as the probability of a targeted churner accepting the offer and thus not churning. It is assumed that  $CLV$ ,  $A$ ,  $f$ , and  $d$  are positive, and that  $CLV > d$ . Note that  $\eta$  depends on the choice for the threshold  $t$ , and thus the company has influence on the size of the targeted fraction.

Equation (13) can be expressed in terms of the score distributions. Moreover, if the average rather than the total profit is considered, and the fixed cost  $A$ , irrelevant for classifier selection, is discarded, it is possible to obtain a functional form equivalent to the expression for  $P$  in (1). To work out the conversion, note that:

$$\begin{aligned} \eta(t) &= \pi_0 F_0(t) + \pi_1 F_1(t), \\ \lambda(t) &= \frac{F_0(t)}{\pi_0 F_0(t) + \pi_1 F_1(t)}. \end{aligned}$$

Moreover, two dimensionless parameters are introduced, being  $\delta = d/CLV$  and  $\phi = f/CLV$ .

**Definition 4.** *The average classification profit of a classifier for customer churn,  $P_C$ , is the interpretation of Definition 1 specifically for customer churn:*

$$P_C(t; \gamma, CLV, \delta, \phi) = CLV(\gamma(1 - \delta) - \phi) \cdot \pi_0 F_0(t) - CLV(\delta + \phi) \cdot \pi_1 F_1(t). \quad (14)$$

Comparison with (1) shows that  $b_0 = CLV(\gamma(1 - \delta) - \phi)$  and  $c_1 = CLV(\delta + \phi)$ . When all parameter values in (14) are assumed to be known, the deterministic performance measure, the maximum profit defined in Definition 2, can be worked out for a customer churn context.

**Definition 5.** *The maximum profit measure for customer churn, MPC, is the interpretation of Definition 2 in a customer churn setting:*

$$MPC = \max_{\forall t} P_C(t; \gamma, CLV, \delta, \phi). \quad (15)$$

As pointed out by Verbeke et al. [13], the MPC criterion is preferred over the commonly used top-decile lift. Setting the targeted fraction of customers to, e.g., 10 percent is a purely arbitrary choice and most likely leads to suboptimal profits and model selection. Since the ultimate goal of a company setting up a customer retention campaign is to minimize the costs associated with customer churn, it is logical to evaluate and select a customer churn prediction model by using the maximum obtainable profit as the performance measure. Moreover, it has another advantage, which is very appealing to practitioners, in the sense that it is possible to determine the optimal MPC fraction. This quantity represents how many customers should be targeted for profit maximization.

**Definition 6.** *The profit maximizing fraction for customer churn,  $\bar{\eta}_{mpc}$ , is the fraction of the customer base which should be targeted to maximize the profit generated by the retention campaign:*

$$\bar{\eta}_{mpc} = \pi_0 F_0(T) + \pi_1 F_1(T), \quad (16)$$

with:

$$T = \arg \max_{\forall t} P_C(t; \gamma, CLV, \delta, \phi). \quad (17)$$

The combination of the maximum profit MPC and the optimal fraction  $\eta_{mpc}$  provides telecom operators with a rigorous framework for making operational decisions with profit maximization as main goal.

## 4.2 The Expected Maximum Profit Measure for Customer Churn

In the previous section, it was assumed that accurate estimates for the parameters in the expression for  $P_C$  are available, in which case a deterministic performance measure can be employed. Often, however, there is significant uncertainty involved. Specifically for the problem of customer churn, there are four parameters, of which customer lifetime value, the cost of the incentive and the contacting cost can be estimated with sufficient reliability. However, about the probability of a churning accepting the

retention offer much less is known. Therefore, this probability,  $\gamma$ , is considered to introduce uncertainty in the estimation of the maximum profit, and thus, a probabilistic performance measure is proposed.

**Definition 7.** *The expected maximum profit measure for customer churn, EMPC, is the interpretation of Definition 3 in a customer churn setting:*

$$EMPC = \int_{\gamma} P_C(T(\gamma); \gamma, CLV, \delta, \phi) \cdot h(\gamma) d\gamma, \quad (18)$$

with  $T$ , the optimal cutoff for a given  $\gamma$ , and  $h(\gamma)$  the probability density function for  $\gamma$ .

Analogously to the H measure, a beta distribution is proposed, because of its flexibility. The parameters are named  $\alpha'$  and  $\beta'$ , where the prime aims to distinguish these parameters from those of the H measure. A procedure for the estimation of EMPC is given in the mathematical appendix, which can be found on the Computer Society Digital Library at <http://doi.ieeecomputersociety.org/10.1109/TKDE.2012.50>. The cost benefit ratio for customer churn,  $\theta_C$ , is equal to

$$\theta_C = \frac{b_1 + c_1}{b_0 + c_0} = \frac{\delta + \phi}{\gamma(1 - \delta) - \phi}, \quad (19)$$

where  $\gamma$  is the parameter introducing the uncertainty.

At this point, an important remark has to be made regarding the relation between the ROC curve of a classifier and its EMPC. In Section 3.1, it was stated that, theoretically, calculating the EMP considers all points of the convex hull of a ROC curve. With EMPC, the cost and benefit parameters obey certain assumptions, specific for a customer churn context. The value of  $\theta_C$  now ranges from  $-(\delta + \phi)/\phi$  to  $-\infty$  for  $\gamma \in [0, \phi/(1 - \delta))$ , and from  $+\infty$  to  $(\delta + \phi)/(1 - \delta - \phi)$  for  $\gamma \in (\phi/(1 - \delta), 1]$ . Hence, for a certain interval of  $\gamma$ ,  $\theta_C$  (and also  $b_0$ ) is negative. This corresponds to the situation when the probability of a churning accepting the retention offer is so low that the expected net gained customer lifetime value, i.e.,  $\gamma(CL - d)$ , does not offset the cost of contacting the customers,  $f$ . In this case, the optimal decision is not to contact any customer, which corresponds to the origin of the ROC curve.

A second observation concerns the fact that  $\theta_C$  does not extend over the entire positive set of real numbers,  $\mathbb{R}^+$ , since it only spans  $[(\delta + \phi)/(\gamma - \gamma\delta - \phi), +\infty)$ . Therefore, points on the convex hull of a ROC curve with a slope smaller than  $(\pi_1/\pi_0) \cdot (\delta + \phi)/(1 - \delta - \phi)$  are not optimal for any value of  $\gamma \in [0, 1]$ . Consequently, when calculating EMPC, not all points of the convex hull are taken into account. Moreover, the more skewed the data set toward nonchurners, the smaller the portion of the convex hull which is taken into account. Intuitively this makes sense since, for very low churn rates, the percentage of churners in a large targeted fraction will quickly become insignificant and hence jeopardize the profitability. The optimal targeted fraction can also be determined when dealing with the expected maximal profit.

**Definition 8.** *The expected profit maximizing fraction for customer churn,  $\bar{\eta}_{empc}$ , is the fraction of the customer base*

which is targeted when taking into account the uncertainty about  $\gamma$ :

$$\bar{\eta}_{\text{empc}} = \int_{\gamma} [\pi_0 F_0(T(\gamma)) + \pi_1 F_1(T(\gamma))] \cdot h(\gamma) d\gamma, \quad (20)$$

with  $T(\gamma)$  being the optimal cutoff, as defined in (16).

Hence, there are two frameworks available to telecom operators. One framework, based on MPC, takes a deterministic approach and considers all parameters in the profit equation to be known. The second framework is based on EMPC and provides practitioners with a probabilistic method to evaluate profits and losses, reflecting the uncertainty about the response rate  $\gamma$ . Due to its specific costs and benefits, performance measurement in a customer churn setting cannot simply be done by applying the H measure. However, it is possible to approximate the EMPC measure to a certain degree, as will be shown in Section 5.

### 4.3 Sensitivity of the EMPC Measure to Variations in the Fixed Parameters

The EMPC measure incorporates uncertainty about the acceptance rate  $\gamma$ , but for the parameters CLV,  $\delta$ , and  $\phi$ , fixed values are assumed. In this paragraph, the sensitivity of the EMPC measure to small variations in these fixed parameters will be assessed. Therefore, the first derivative of (18) with respect to CLV is calculated:

$$\frac{\partial \text{EMPC}}{\partial \text{CLV}} = \int_{\gamma} \frac{\partial P_C(T(\gamma); \gamma, \text{CLV}, \delta, \phi)}{\partial \text{CLV}} h(\gamma) d\gamma.$$

Note that the optimal cutoff,  $T(\gamma)$ , depends on the value of CLV. In what follows, the partial derivative within the integration is elaborated. Using (14) yields

$$\begin{aligned} \frac{\partial P_C(T)}{\partial \text{CLV}} &= (\gamma(1 - \delta) - \phi) \cdot \pi_0 F_0(T) - (\delta + \phi) \cdot \pi_1 F_1(T) \\ &\quad + \text{CLV}(\gamma(1 - \delta) - \phi) \cdot \pi_0 f_0(T) \frac{\partial T}{\partial \text{CLV}} \\ &\quad - \text{CLV}(\delta + \phi) \cdot \pi_1 f_1(T) \frac{\partial T}{\partial \text{CLV}}, \end{aligned}$$

which, by using (14) and (19), can be rewritten as follows:

$$\begin{aligned} \frac{\partial P_C(T)}{\partial \text{CLV}} &= \frac{P_C(T)}{\text{CLV}} + \text{CLV} \frac{\partial T}{\partial \text{CLV}} (\gamma(1 - \delta) - \phi) \\ &\quad \pi_1 f_1(T) \cdot \left( \frac{\pi_0 f_0(T)}{\pi_1 f_1(T)} - \theta_C \right). \end{aligned}$$

Now, (4) can be applied, which leads to the last term between brackets being equal to zero, and thus:

$$\frac{\partial \text{EMPC}}{\partial \text{CLV}} = \int_{\gamma} \frac{P_C(T)}{\text{CLV}} h(\gamma) d\gamma = \frac{\text{EMPC}}{\text{CLV}}. \quad (21)$$

In other words, this means that when CLV is changed, holding  $\delta$  and  $\phi$  constant, EMPC changes proportionally. Note that holding  $\delta$  and  $\phi$  constant in fact means that the cost of the retention offer as a percentage of CLV, and the cost of contacting a customer as a percentage of CLV remain constant.

Analogously, for variations in  $\phi$  the following equation can be derived:

$$\begin{aligned} \frac{\partial \text{EMPC}}{\partial \phi} &= -\text{CLV} \int_{\gamma} [\pi_0 F_0(T) + \pi_1 F_1(T)] h(\gamma) d\gamma \\ &= -\text{CLV} \cdot \bar{\eta}_{\text{empc}}, \end{aligned} \quad (22)$$

where  $\bar{\eta}_{\text{empc}}$  is the expected profit maximizing fraction. For changes in  $\delta$ , the following holds true:

$$\begin{aligned} \frac{\partial \text{EMPC}}{\partial \phi} &= -\text{CLV} \int_{\gamma} [\gamma \pi_0 F_0(T) + \pi_1 F_1(T)] h(\gamma) d\gamma \\ &= -\text{CLV} \cdot \bar{\rho}_{\text{empc}}, \end{aligned} \quad (23)$$

with  $\bar{\rho}_{\text{empc}}$ , the expected fraction of the customer base which accepts the retention offer. In fact, this implies that the larger the optimal targeted fraction (or the fraction accepting the offer), the more sensitive the expected maximum profit for variations in  $\phi$  (or  $\delta$ ). Also note that an increase in CLV, while holding  $d$  and  $f$  constant instead of  $\delta$  and  $\phi$ , corresponds to a parallel decrease in  $\delta$  and  $\phi$ . In Section 6, the sensitivity of the rankings will be analyzed in a real-life case study.

### 4.4 Parameter Values of the Profit Function and Response Rate Distribution

To employ the MPC and EMPC measures, it is necessary to obtain values for the parameters in the profit function. The values for these parameters, such as CLV, are industry specific and may even vary from company to company. This paper focuses on customer churn prediction in the telecom industry and estimates for the parameters are based on values reported in the literature ([16] and [17]) and information from telecom operators. When a specific company uses MPC or EMPC for selecting the optimal model, they can plug in their own estimates for the parameters. In this study, the values of the parameters CLV,  $d$ , and  $f$  are taken as €200, €10, and €1, respectively.

The parameter  $\gamma$ , representing the response rate, is much more difficult to estimate. For the MPC criterion, a single point estimate would be required, which corresponds to one degree of freedom. For the EMPC criterion, however, there are two degrees of freedom, i.e.,  $\alpha$  and  $\beta$ . This enables the practitioner to define an expected value and a standard deviation, where the latter accounts for the uncertainty in the practitioner's estimation. The  $\alpha$  and  $\beta$  parameters can be obtained by solving the following system of equations:

$$\begin{cases} E[\gamma] = \mu = \alpha / (\alpha + \beta) \\ \text{Var}[\gamma] = \sigma^2 = \alpha \beta / [(\alpha + \beta)^2 (\alpha + \beta + 1)], \end{cases}$$

which yields

$$\begin{cases} \alpha = \mu((1 - \mu)/\sigma^2 - 1) \\ \beta = (1 - \mu)((1 - \mu)/\sigma^2 - 1). \end{cases}$$

There is only one restriction, namely that  $\alpha$  and  $\beta$  need to be strictly greater than one in order to obtain a unimodal beta distribution.

Neslin et al. [16] assumed values ranging from 10 to 50 percent, therefore this paper proposes the expected value and standard deviation of the acceptance rate to be equal to 30 percent and 10 percent respectively. This leads to the parameters  $\alpha'$  and  $\beta'$  being 6 and 14, respectively, which corresponds to the probability density function plotted in Fig. 2 (solid line). When MPC is calculated, a point estimate



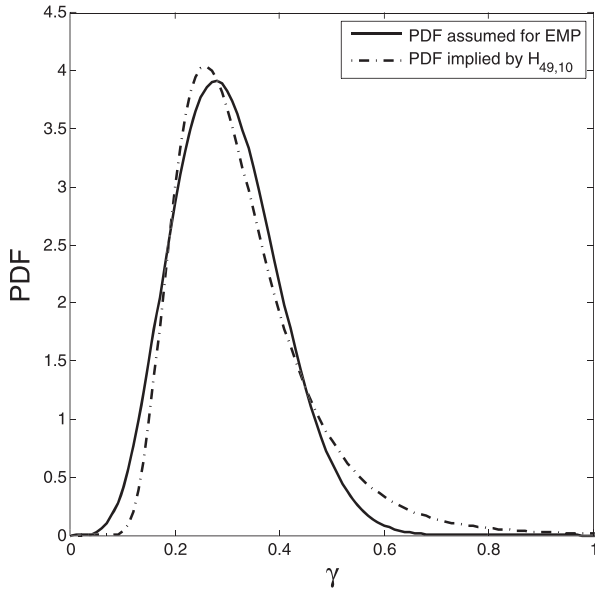


Fig. 2. The graph shows the proposed density function for the response rate in the EMPC measure, and the density function implied by the H-measure with optimized parameters.

for  $\gamma$  is required, in which case the expected value, equal to 30 percent, is taken.

## 5 EXPECTED MAXIMUM PROFIT AND THE H MEASURE

As mentioned in Section 3.2, the H measure is an expected minimum loss measure, with certain assumptions about the distribution of the cost and benefit parameters. These assumptions imply that the H measure takes into account all points on the convex hull. The EMPC measure, however, only takes into account a part of the convex hull. In this section, it will be investigated whether it is possible to approximate the EMPC measure with the H measure. After all, it would be convenient if the EMPC measure fits in an existing performance measurement framework.

The discussion will focus on the variable part of the H measure, defined in (12). Only this part of the H measure changes with varying classifiers, holding the data set constant, and thus, the ranking of techniques for a data set only depends on  $H_{var}$ . At this point, it is assumed that the variable  $c$  in  $H_{var}$  is a function of  $\gamma$ ,  $\delta$ , and  $\phi$ :

$$c = \frac{\gamma(1-\delta) - \phi}{\gamma(1-\delta) + \delta} = \frac{K\gamma - \phi}{K\gamma + \delta},$$

where  $K = 1 - \delta$  for notational convenience. In what follows, a variable transformation from  $c$  to  $\gamma$  will be carried out in the expression for  $H_{var}$ . Expressions for  $dc$  and  $u_{\alpha,\beta}(c)$  as a function of  $\gamma$  are derived:

$$\begin{aligned} dc &= \frac{K(\delta + \phi)}{(K\gamma + \delta)^2} d\gamma, u_{\alpha,\beta}(c(\gamma)) \\ &= \frac{1}{B(1, \alpha, \beta)} \left( \frac{K\gamma - \phi}{K\gamma + \delta} \right)^{\alpha-1} \left( \frac{\delta + \phi}{K\gamma + \delta} \right)^{\beta-1}. \end{aligned}$$

Hence, the variable substitution in the expression for  $H_{var}$  leads to

$$\begin{aligned} H_{var} &= \int_0^1 [\pi_0 c F_0 - \pi_1 (1-c) F_1] \cdot u_{\alpha,\beta}(c) dc \\ &= \int_{\phi/K}^{+\infty} [(K\gamma - \phi)\pi_0 F_0 - (\delta + \phi)\pi_1 F_1] \\ &\quad \cdot \underbrace{\frac{K(\phi + \delta)^\beta}{B(1, \alpha, \beta)} \cdot \frac{(K\gamma - \phi)^{\alpha-1}}{(K\gamma + \delta)^{\alpha+\beta+1}}}_{g(\gamma)} d\gamma \\ &= \frac{1}{CLV} \int_{\phi/K}^{+\infty} P_C(T(\gamma); CLV, \gamma, \delta, \phi) \cdot g(\gamma) d\gamma. \end{aligned}$$

For  $\gamma < \phi/K$ , the benefit associated with a targeted churner is negative. Since the maximal profit,  $P(T(\gamma))$ , for this range of  $\gamma$  is equal to zero,  $H_{var}$  can be expressed as:

$$H_{var} = \frac{1}{CLV} \int_0^{+\infty} P(T(\gamma); CLV, \delta, \phi) \cdot g(\gamma) d\gamma. \quad (24)$$

Equation (24) shows that  $H_{var}$  essentially is an EMPC measure scaled by  $CLV$ , for which the distribution  $h(\gamma)$  is replaced with the weight function  $g(\gamma)$ , and where  $\gamma \in \mathbb{R}^+$ . It is to be noted that the function  $g(\gamma)$  is not a probability density in the strict sense, since generally, the area under  $g$  will not be equal to one. However, by simply multiplying  $H_{var}$  with a normalization constant, this is resolved. Let the proper density function  $\tilde{h}(\gamma)$  be the normalized function  $g(\gamma)$ , then  $H_{var}$  equals

$$\begin{aligned} H_{var} &= \frac{\int_0^{+\infty} g(\gamma) d\gamma}{CLV} \\ &\quad \cdot \int_0^{+\infty} P(T(\gamma); CLV, \delta, \phi) \cdot \tilde{h}(\gamma) d\gamma. \end{aligned} \quad (25)$$

Because the H measure takes into account all points of the convex hull, this corresponds to integrating over  $\gamma \in [0, +\infty)$ .

As illustrated by (25), the H measure will rank classifiers according to their expected maximum profit, implicitly assuming the distribution  $\tilde{h}(\gamma)$ , which is specified by the parameters  $\alpha$  and  $\beta$ . The previously proposed distribution for  $\gamma$ ,  $h(\gamma)$ , is specified by the parameters  $\alpha'$  and  $\beta'$ . It is not possible to analytically find values for  $\alpha$  and  $\beta$  so that  $\tilde{h}(\gamma)$  equals  $h(\gamma)$ . Therefore, a distance measure between the two distributions is numerically minimized. Several distance measures have been experimented with, but the *Hellinger distance* leads to the best results. The Hellinger distance between two probability measures,  $D_h$ , is defined as the  $L_2$  distance between the square root of their densities [23]. Hence, the optimal parameters for the approximating H measure can be found by solving the following minimization problem:

$$\begin{aligned} \min_{\forall \alpha, \beta} D_h(h(\gamma), \tilde{h}(\gamma)) \\ = \min_{\forall \alpha, \beta} \int_0^{+\infty} \left( \sqrt{h(\gamma)} - \sqrt{\tilde{h}(\gamma)} \right)^2 d\gamma. \end{aligned} \quad (26)$$

Note that  $h(\gamma)$  is parameterized by  $\alpha'$  and  $\beta'$ , which are considered to be known, whereas  $\tilde{h}(\gamma)$  is parameterized by  $\alpha$  and  $\beta$ , which are to be optimized.

In order to find the optimal parameters for the approximating H measure, the minimization problem in (26) has been numerically solved, yielding  $\alpha \approx 49$  and  $\beta \approx 10$  as best



TABLE 2

Summary of Data Set Characteristics: ID, Source, Region, Number of Observations, Number of Attributes, Percentage Churners, and References to Previous Studies Using the Data Set

ID	Source	Region	# Obs.	# Att.	%Churn	Reference
O1	Operator	North America	47,761	53	3.69	[18], [13], [19]
O2	Operator	East Asia	11,317	21	1.56	[20], [13]
O3	Operator	East Asia	2,904	15	3.20	[20], [13]
O5	Operator	East Asia	2,180	15	3.21	[20], [13]
O6	Operator	Europe	338,874	727	1.80	[13]
D1	Duke	North America	93,893	197	1.78	[21], [22], [16], [13], [19]
D2	Duke	North America	38,924	77	1.99	[13], [19]
D3	Duke	North America	7,788	19	3.30	[13], [19]
UCI	UCI	-	5,000	23	14.14	[22], [13], [19]
KDD	KDD Cup 2009	Europe	46,933	242	6.98	[13]

values. This density function is plotted as the dashed line in Fig. 2, and has an expected value of 28.9 percent and a standard deviation of 10.4 percent. Although the density theoretically is nonzero for  $\gamma > 1$ , the accumulated probability for this region is smaller than  $10^{-3}$ . In Section 6, a case study will be carried out and it will be investigated how well the H measure approximates the EMPC measure in terms of ranking several classification techniques.

6 CASE STUDY

In this section, a case study will be presented to illustrate the use of the EMPC and H measure for measuring classification performance in a customer churn prediction context. A selection of 21 techniques has been tested on 10 different customer churn data sets. The data sets have been preprocessed to prepare them for the analysis. Table 2 summarizes the main characteristics of the data sets. The classification techniques used in the benchmarking study are listed in Table 3 and include many commonly applied data mining methods. A more extensive discussion regarding the data sets, the preprocessing and the employed techniques can be found in the original benchmarking study, carried out by Verbeke et al. [13].

Each data set has been split into a training set and a test set, where the former was used to train the classifiers, and the latter to perform an out-of-sample test. Thus, each instance in the test set is assigned a score  $s$ , on which classification is based by setting a cutoff value. Through the empirical score distributions, the AUC, H measure, MPC measure, and EMPC measure are then calculated. Per data set, each measure leads to a ranking of the 21 techniques. Since the ranking is the most important output of the classification performance measurement process, the rankings from the different measures will be compared to one another. As the 10 data sets involved in this study are independent, the 10 resulting rankings of techniques are considered independent observations.

6.1 Comparison of EMPC with Other Performance Measures

Thus, each performance measure results in a ranking for every data set. For each single data set, Kendall’s  $\tau_b$  is used as a measure of dependence between the rankings based on different performance measures, yielding 10 values for each correlation. The box plot in Fig. 3 shows the distribution of the values of the correlation between EMPC and the four displayed performance metrics. It is clear that the agreement between AUC and EMPC-based rankings is lowest,

TABLE 3

Overview of the Classification Techniques

Overview of Classification Techniques	
<b>Decision Tree Approaches</b> C4.5 Decision Tree (C4.5) Classification and Regression Tree (CART) Alternating Decision Tree (ADT)	<b>Rule Induction Techniques</b> RIPPER (RIPPER) PART (PART)
<b>Ensemble Methods</b> Random Forests (RF) Logistic Model Tree (LMT) Bagging (Bag) Boosting (Boost)	<b>Statistical Classifiers</b> Logistic Regression (Logit) Naive Bayes (NB) Bayesian Networks (BN)
<b>SVM Based Techniques</b> SVM with linear kernel (linSVM) SVM with radial basis function kernel (rbfSVM) LSSVM with linear kernel (linLSSVM) LSSVM with radial basis function (rbfLSSVM) Voted Perceptron (VP)	<b>Nearest Neighbors</b> k-Nearest neighbors $k = 10$ (KNN10) k-Nearest neighbors $k = 100$ (KNN100)  <b>Neural Networks</b> Multilayer Perceptron (NN) Radial Basis Function Network (RBFN)

More information regarding these data mining techniques can be found in the original benchmarking study [13] or in a standard data mining handbook (e.g., [24], [25]).

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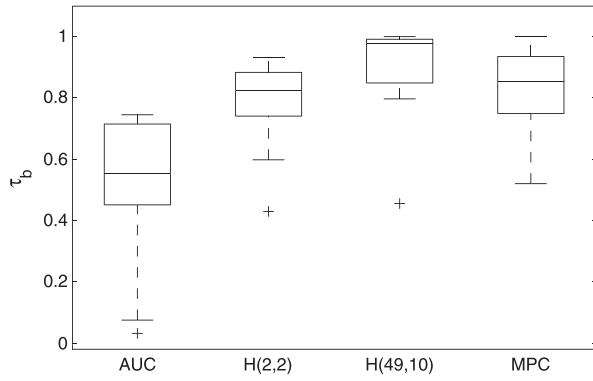


Fig. 3. Box plot indicating the distribution of correlations between EMPC and  $H_{2,2}$ ,  $H_{49,10}$ , and MPC, respectively.

and it has the largest variability. The H measure with default parameters ( $\alpha = 2$  and  $\beta = 2$ ) shows a higher level of correlation, but still significant variability. The H measure with optimized parameter values, however, shows very high correlation and lowest variability, indicating that both rankings agree to a large extent and that this is a reasonable approximation to the EMPC measure. Finally, the correlation between MPC and EMPC is again lower, which can be attributed to the fact that the underlying cost and benefit assumptions are different, i.e., it is a deterministic versus a probabilistic approach. This also suggests that when the operator has accurate estimates of the response rate  $\gamma$ , it is preferable to use MPC as criterion. When there is more uncertainty involved with the estimation of  $\gamma$ , a probabilistic approach, and thus EMPC, is recommended. Furthermore, the box plot shows an outlier for the correlation between EMPC and AUC,  $H_{2,2}$ , and  $H_{49,10}$ . These outliers correspond to the data set D2, where the expected maximum profit is zero for all techniques. As a result, EMPC and MPC consider all techniques to be unprofitable, and they all receive the same rank. AUC,  $H_{2,2}$ , and  $H_{49,10}$  on the other hand will rank techniques differently. Therefore, the correlation is low for this data set.

A further indication of the agreement in ranking is given in Fig. 4, which shows the rank of each technique, averaged over the 10 data sets. The full line represents the ranking according to the EMPC measure, whereas the other points represent other performance metrics. Hence, a point plotted far from the full line shows strong disagreement with the

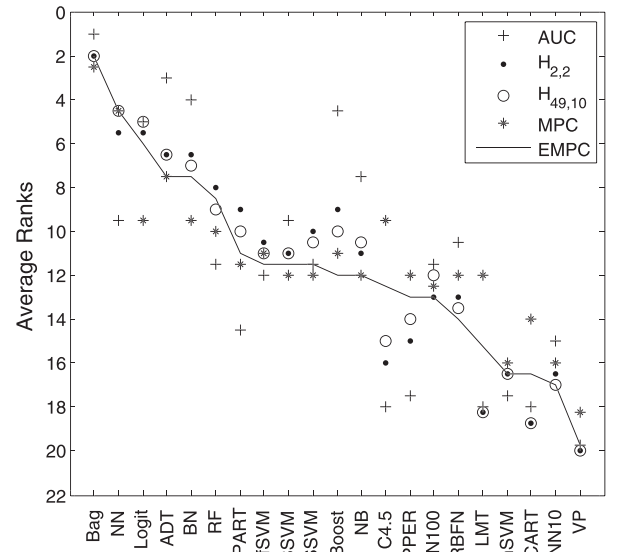


Fig. 4. The average rank over 10 data sets for each technique based on several performance measures (i.e., AUC,  $H_{2,2}$ ,  $H_{49,10}$ , MPC, EMPC).

EMPC-based ranking. One can immediately see that the disagreement of AUC with EMPC is larger than any other performance measure. The H measure with optimized parameters follows the EMPC ranking much closer, again indicating that it is a reasonable approximation.

A second point of view is the profitability of a retention campaign. As explained before, EMPC ranks classifiers according to the expected profit based on assumptions about the classification costs and benefits. AUC, as shown by Hand [2], is also a measure of profit, but with invalid assumptions for the distribution of costs and benefits. Therefore, choosing a classifier based on AUC may lead to suboptimal model selection from a profit point of view, which is illustrated in Table 4. For each data set, the optimal technique is selected based on EMPC and on AUC, and the expected profit for that particular choice of classifier is given. As indicated in the last column, selection based on AUC leads in some cases to suboptimal model selection, with losses up to €0.137 per customer, a substantial amount for telecom operators with millions of customers. Moreover, for selection based on EMPC, it is possible to calculate the fraction of the vast customer base which needs to be

TABLE 4  
Model Selection Based on EMPC and on AUC, with the Expected Profit for Each Method

Data Set	Selection based on EMPC			Selection based on AUC			Difference in EMPC (€)
	Technique	EMPC (€)	$\eta_{empc}(\%)$	Technique	AUC	EMPC (€)	
O1	ADT	0.129	2.10	Logit	0.747	0.120	0.009
O2	NN	0.051	0.09	Bag	0.644	0.017	0.034
O3	Boost	0.646	3.77	Bag	0.903	0.521	0.125
O5	Bag	1.652	3.44	Bag	0.964	1.652	0
O6	Bag	0.047	0.32	Bag	0.902	0.047	0
D1	KNN10	0.001	0.03	Boost	0.599	0	0.001
D2	PART	0	0	Bag	0.618	0	0
D3	BN	0.351	2.83	NB	0.809	0.214	0.137
UCI	RF	5.734	13.65	Bag	0.915	5.640	0.093
KDD	ADT	0.379	7.82	Bag	0.713	0.375	0.004

For model selection with EMPC, also the optimal fraction of customers to target is given.

targeted to realize the maximal profit, which is also displayed in Table 4. This is one of the major advantages of the EMPC (and also the MPC) measure, as it gives guidance to practitioners about how many customers to include in a retention campaign. When selecting a model with AUC or the H measure, there is no such guidance, and deviating from the optimal fraction may again lead to suboptimal profits.

## 6.2 Sensitivity of the EMPC Measure and the Ranking to Variations in the Fixed Parameters

Section 4.3 discusses the impact of variations in CLV,  $\delta$ , and  $\phi$  on the estimated expected profit and analytically derives first order approximations for this sensitivity. This yields some straightforward rules of thumb for the sensitivity, such as, e.g., the higher the targeted fraction, the more sensitive the profit to changes in  $\phi$ . However, the question arises how the ranking between classification algorithms is affected. Therefore, the results of the case study are used to analyze this impact. First, the techniques have been ranked with the proposed values for CLV,  $\delta$ , and  $\phi$ . Then, each parameter has been multiplied with a constant (while holding the others equal), and the techniques have been ranked again with this new parameter value. The correlations between the ranking in the base scenario and the ranking in the new scenario have been plotted for varying values of the multiplier, ranging from  $1/2$  to 2. Fig. 5 shows these results for all three fixed parameters. The median and the first and third quartile (over the 10 data sets) have been plotted. Note that the plot for CLV assumes that CLV is changed while  $d$  and  $f$  are held constant (not  $\delta$  and  $\phi$ ). It can be seen that variations in both CLV and  $\delta$  have a similar impact, with median correlations decreasing until 0.8. The impact of  $\phi$  is virtually nonexistent.

Furthermore, when the ranking changes, also the best performing technique (with the highest expected profit) may change. Therefore, Fig. 5 also displays the impact of suboptimal classifier selection due to incorrect parameter values on the profitability. The percentage loss is plotted on the right axis. Again, the impact is most significant for CLV and  $\delta$ , whereas variations in  $\phi$  do not impact the profitability. But even though there is an impact, it is relatively limited to losses of maximal 20 percent, and this for substantial variations in the parameters (doubling or halving the CLV or  $\delta$ ). These results, both in terms of correlation between rankings and percentage loss due to incorrect classifier selection, indicate that the EMPC measure and corresponding rankings are robust to changes in the fixed parameters. The impact only becomes noticeable for multipliers smaller than 0.75 or larger than 1.5.

## 7 CONCLUSION

The implications of the findings presented in this paper are straightforward but essential. Companies rely more than ever on data mining techniques to support their decision making processes. When evaluating a classification technique which is to be used in a business context, it is imperative to base any evaluation criterion on the goal of the end user. Since companies strive for profit maximization, a performance measure evidently should take this into

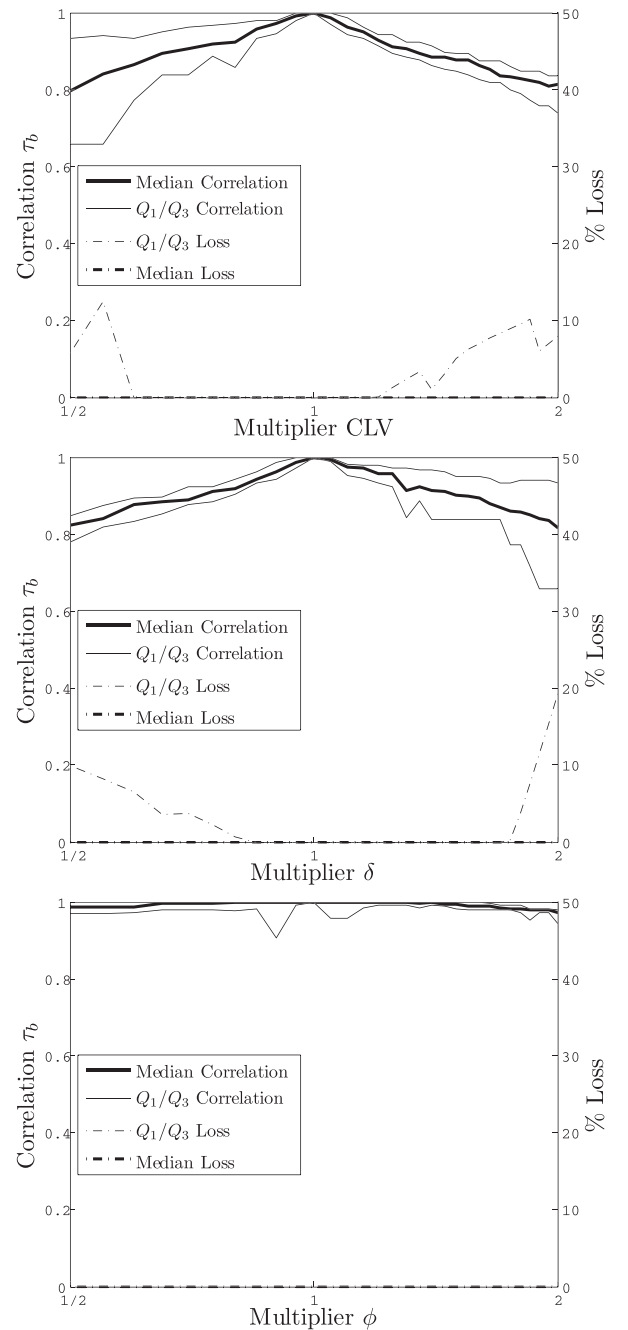


Fig. 5. Sensitivity of the EMPC measure to variations in CLV,  $\delta$ , and  $\phi$ , respectively. The left axis and full lines indicate the correlation between the ranking of the base scenario and the ranking with the changed parameter. The right axis and dashed lines show the percentage loss due to incorrect classifier selection. For both correlation and percentage loss, the median, first quartile ( $Q_1$ ) and third quartile ( $Q_3$ ) have been plotted. The  $x$ -axis is plotted on a logarithmic scale with base 2, with the multiplier ranging from  $1/2$  to 2.

account. The very commonly used area under the ROC curve does have its merits and an interesting interpretation in the sense that the AUC of a classification method is the probability that a randomly chosen positive instance will be ranked higher than a randomly chosen negative instance. However, as [2] has shown, AUC makes incorrect implicit assumptions about the misclassification costs, and the use of this performance metric in a business environment leads to suboptimal profits. This paper outlines a

theoretical framework which incorporates all gains and losses related to the employment of a data mining technique, and defines a probabilistic performance measure, the expected maximum profit.

As each corporate environment has its own specificities, the framework is defined on a general level. To be applicable to a certain business problem, the particularities of its cost and benefit structure need to be incorporated. This process is worked out in detail for the problem of customer churn and an EMP measure for customer churn, EMPC, is derived. Also the link between EMPC and the H measure was investigated and it appears that the latter with appropriately chosen distribution parameters is a good approximation of the former. The performance measure for customer churn is validated in an extensive case study. The results clearly indicate that the use of AUC as a performance metric leads to suboptimal profits. The case study also points to one of the major advantages of the EMPC measure. It does not only select the classifier which maximizes the profit, but it also provides the practitioner with an estimate of the fraction of the customer base which needs to be targeted in the retention campaign. This optimal fraction varies from case to case, and deviating from this fraction again leads to suboptimal profits. Note that the H measure, although it is able to select the most profitable classifier, does not provide guidance on the optimal fraction of the customer base to be included in the retention campaign. Finally, a sensitivity analysis was carried out, to analyze how vulnerable the EMPC measure is to incorrect estimation of the fixed parameters CLV,  $\delta$ , and  $\phi$ . The outcome shows that the EMPC measure and its resulting ranking is relatively robust with regard to changes in these parameter values.

An obvious though not straightforward direction for further research entails the extension of the framework to multiclass problems. Furthermore, besides the application of the cost-benefit analysis framework to the customer churn problem, there remain many business problems where a profit driven performance measure would add value. Among others, data mining techniques are employed for financial credit scoring [26], direct marketing response models [27], fraud detection [28], and viral marketing in social networks [29]. With the explosive growth of data, and the increasing popularity of social network sites, companies will rely more than ever on data mining techniques to support their decision making process. In such cases, the cost-benefit analysis framework presented in this paper provides directions on how to develop performance measures tailored to specific business problems.

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