

Lista de exercícios

1.

$$B = \begin{bmatrix} -1 & 1 & 0 \\ 1 & -3 & 4 \end{bmatrix} \quad 2 \times 3$$

A =

$$\begin{bmatrix} 3 & -1 \\ 0 & 2 \end{bmatrix} \quad 2 \times 2$$

$$(3 \cdot -1)(-1 \cdot 1) \quad (3 \cdot 0)(-1 \cdot -3) \quad (3 \cdot 0)(-1 \cdot 4) \\ (0 \cdot 1)(2 \cdot 1) \quad (0 \cdot 0)(2 \cdot -3) \quad (0 \cdot 0)(2 \cdot 4)$$

$$B_{2 \times 3} \cdot A_{2 \times 2} = \cancel{A}_{2 \times 2}$$

$$\begin{bmatrix} -3-1 & 6+3 & 0-4 \\ 0+2 & 0-6 & 0+8 \end{bmatrix}$$

$$3 \quad A_{2 \times 2} \cdot B_{2 \times 3} = \begin{bmatrix} -4 & 9 & -4 \\ 2 & -6 & 8 \end{bmatrix} \quad 2 \times 3 \cancel{A}_{2 \times 2}$$

2.

$$B = \begin{bmatrix} 3 & -2 \\ 1 & -3 \end{bmatrix}$$

A =

$$\begin{bmatrix} 5 & 2 & -1 \\ 7 & 4 & 3 \end{bmatrix} \quad 3 \times 3$$

$$(5 \cdot 3)(2 \cdot 1)(-1 \cdot -4) \quad (5 \cdot -2)(2 \cdot -3)(-1 \cdot 0) \\ (7 \cdot 3)(4 \cdot 1)(3 \cdot -4) \quad (7 \cdot -2)(4 \cdot -3)(3 \cdot 0)$$

$$\begin{bmatrix} 15+2+4 & -10-6-0 \\ 21+4-12 & -14-12+0 \end{bmatrix}$$

$$3 \quad A_{2 \times 3} \cdot B_{3 \times 2} = \cancel{A}_{2 \times 2}$$

$$\begin{bmatrix} 25 & -36 \\ 23 & -26 \end{bmatrix} \quad 2 \times 2 \cancel{A}_{2 \times 2}$$

$$A = \begin{vmatrix} 5 & 2 & -1 \\ 7 & 4 & 3 \end{vmatrix} \quad 2 \times 3$$

$$B = \begin{vmatrix} 3 & -2 \\ 1 & -3 \\ -4 & 0 \end{vmatrix} \quad 3 \times 2$$

(3,5)(-2,7)	(3,2)(-2,4)	(3,-1)(-2,3)
(1,5)(-3,7)	(1,2)(-3,4)	(1,-1)(-3,3)
(-4,5)(0,7)	(-4,2)(0,4)	(-4,-1)(0,3)

$$\begin{vmatrix} 15-14 & 6-8 & -3-6 \\ 5-21 & 2-12 & -1-9 \\ -20+0 & -8+0 & 4+0 \end{vmatrix}$$

$$\exists B_{3 \times 2} \cdot A_{2 \times 3} = \begin{vmatrix} 1 & -2 & -9 \\ -16 & -10 & -10 \\ -20 & -8 & 4 \end{vmatrix} \quad 3 \times 3 //$$

$$3. \quad A = \begin{vmatrix} -1 & 0 \\ 1 & 2 \end{vmatrix} \quad 2 \times 2 \quad A^T = \begin{vmatrix} -1 & 1 \\ 0 & 2 \end{vmatrix} \quad 2 \times 2$$

$$\begin{bmatrix} (-1,-1)(0,0) & (-1,1)(0,-2) \\ (1,-1)(2,0) & (1,1)(2,2) \end{bmatrix}$$

$$\begin{vmatrix} 1+0 & -1+0 \\ -1+0 & 1+4 \end{vmatrix}$$

$$A_{2 \times 2} \cdot A_{2 \times 2}^T = \begin{vmatrix} 1 & -1 \\ -1 & 5 \end{vmatrix} \quad 2 \times 2 //$$

alternativa (B) //

$$4 \quad A = \begin{vmatrix} 1 & 2 & 5 \\ 3 & 4 & 6 \end{vmatrix}_{2 \times 3} \quad B = \begin{vmatrix} 1 \\ 2 \\ 3 \end{vmatrix}_{3 \times 1}$$

C21

$$\begin{bmatrix} (1,1)(2,2)(5,3) \\ (3,1)(4,2)(6,3) \end{bmatrix}$$

$$\begin{bmatrix} 1+4+15 \\ 3+8+18 \end{bmatrix}$$

$$C_{21} = 29 //$$

$$C = \begin{bmatrix} 20 \\ 29 \end{bmatrix}$$

alternativa (A) 29 //

$$5 \text{ a)} \quad \begin{array}{c|cccc} & 25 & 50 & 200 & 20 \\ \hline & 28 & 60 & 150 & 22 \end{array} \quad 2 \times 4 \quad \begin{bmatrix} 1 & 1 \\ 8 & 10 \\ 0,9 & 0,8 \\ 1,5 & 1 \end{bmatrix} \quad 4 \times 2$$

$$\text{b)} \quad \begin{array}{l} (25,1)(50,8)(200,0,9)(20,1,5) \quad (25,1)(50,10)(200,0,8)(20,1) \\ (28,1)(60,8)(150,0,9)(22,1,5) \quad (28,1)(60,10)(150,0,8)(22,1) \end{array}$$

$$\begin{array}{ll} 25 + 400 + 180 + 30 & 25 + 500 + 160 + 20 \\ 28 + 480 + 135 + 33 & 28 + 600 + 120 + 22 \end{array}$$

$$\text{produto} = \begin{bmatrix} 635 & 705 \\ 676 & 770 \end{bmatrix}$$

$$705 - 635 = 70$$

$$770 - 676 = 94$$

$$70 + 94 = 164$$

R\$ 164,00 //

6

$$\begin{bmatrix} 0 & -1 \\ a & 1 \end{bmatrix}$$

$$\begin{bmatrix} a & 1 \\ -1 & 0 \end{bmatrix}$$

$$\begin{array}{ll} (0 \cdot a)(-1, -1) & (0, 1)(-1, 0) \\ (a \cdot a)(1, -1) & (a, 1)(1, 0) \end{array}$$

$$\begin{bmatrix} 0+1 & 0+0 \\ a^2-1 & a+1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ a^2-1 & a \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad a=1 \text{ ou } -1$$

alternativa (E) $\cancel{\rightarrow}$

lista de exercícios

1. $A = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \quad (A^T)^T = \begin{bmatrix} A & B \\ C & D \end{bmatrix}$

$$B = \begin{bmatrix} E & F \\ G & H \end{bmatrix} \quad (B^T)^T = \begin{bmatrix} E & F \\ G & H \end{bmatrix}$$

portanto $(A^T)^T = A$ e $(B^T)^T = B$

alternativa (A) $(A^T)^T = A$ e $(B^T)^T = B$ $\cancel{\rightarrow}$

2. De acordo com as particularidades $(A) AB = BA \rightarrow$ falso

sobre o produto matricial, podemos $(B) se AB = AC, ent\circ B = C \rightarrow$ falso
ver que:

alternativa (D) $(AB)C = A(BC)$ é

verdadeira $\cancel{\rightarrow}$

$A = O_n \rightarrow$ falso

$(D) (AB)C = A(BC) \rightarrow$ verdadeira

$(E) (A+B)^2 = A^2 + 2AB + B^2 \rightarrow$ falso



$$3 \begin{bmatrix} 5 & 8 & 10 \\ x & y & z \end{bmatrix} + \begin{bmatrix} 5 & 8 & 10 \\ 9 & 6 & 4 \end{bmatrix} - \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} 10 & 16 & 20 \\ 9 & 6 & 4 \end{bmatrix} - \begin{bmatrix} 9 \\ 6 \\ 4 \end{bmatrix}$$

$$\begin{bmatrix} 90 & 96 & 80 \\ 81 & 36 & 16 \end{bmatrix}$$

$$x = 9$$

$$y = 6$$

$$z = 4$$

alternativa (B), //

$$4. A = \begin{bmatrix} -1 \\ 4 \\ 2 \end{bmatrix} \quad A^T = \begin{bmatrix} -1 & 4 & 2 \end{bmatrix}$$

alternativa (C) primeira linha da
transposta de A //