

Lista de exercícios

a)
$$\begin{vmatrix} 2 & 3 \\ 1 & 5 \end{vmatrix} \quad \det = 10 - 3 = 7 //$$

b)
$$\begin{vmatrix} -2 & -4 \\ 3 & 6 \end{vmatrix} \quad \det = -12 - (-12) = -12 + 12 = 0 //$$

c)
$$\begin{vmatrix} 3 & -1 & 1 \\ 2 & 1 & -1 \\ 1 & 4 & -2 \end{vmatrix} \quad \begin{matrix} 3 & -1 & 1 \\ 2 & 1 & 1 \\ 1 & 4 & 1 \end{matrix} \quad \begin{matrix} -12 & 4 \\ -6 & 1 & 8 \end{matrix} \quad \det = 3 - (-7) = 10 //$$

$$1 + (-12) + 4 = 1 - 12 + 4 = -7$$

$$-6 + 1 + 8 = 3$$

d)
$$\begin{vmatrix} 3 & 2 & -1 \\ 2 & 3 & 1 \\ -3 & 1 & 1 \end{vmatrix} \quad \det = 36 - 16 = 20 //$$

$$\begin{matrix} 3 & 3 & 2 & -1 & -2 \\ 2 & 3 & 1 & 1 & 2 \end{matrix} \quad 36 + (-2) + 2 = 36 - 2 + 2 = 36$$

$$-3 + 3 + 16 = 16$$

2. $A = (a_{ij})$ 3×3 $\text{det} \begin{cases} -3 & \text{se } i=j \\ 0 & \text{se } i \neq j \end{cases}$

$$\begin{vmatrix} -3 & 0 & 0 \\ 0 & -3 & 0 \\ 0 & 0 & 0 \end{vmatrix} \quad \text{det} = -27 - 0 = -27,$$

$$\begin{vmatrix} 0 & -3 & 0 & 0 & 0 \\ 0 & 0 & -3 & 0 & 0 \end{vmatrix}$$

$$\begin{array}{c|cc|c} 3 & x & 1 & x \\ \hline 3 & x & 4 & = -3 \\ x^2 & 1 & 3 & 3 \\ \hline 12x & x & 3 & x & 9x \\ 9 & 3 & x & 4 & 4 \end{array} \quad \begin{aligned} (3x^2 + 9x + 4) - x^2 + 3x + 9 \\ 2x^2 - 3x - 5 + 3 \\ 2x^2 - 3x_1 - 2 = 0 \\ 2x^2 + x - 4x - 2 = 0 \\ x(2x + 1) - 4x - 2 = 0 \\ (2x + 1)(x - 2) = 0 \end{aligned}$$

$$2x + 1 = 0 \quad x' = -1/2,$$

$$x - 2 = 0 \quad x'' = 2,$$

alternativa (E),

$$\begin{array}{c|cc|c} 4. & x-1 & -1 & 0 \\ \hline 0 & x+1 & -1 \\ 2 & -1 & x+1 \\ \hline x-1 & -1 & 0 \\ 0 & x+1 & -1 \end{array}$$

$$(x-1)(x+1) - (-1)(-1) = 2$$

$$x^2 - 1 - 1 = 2$$

$$5. A = (a_{ij})_{3 \times 2}$$

$$a_{ij} = 2i - 3j$$

$$B = (b_{jk})_{2 \times 3}$$

$$b_{jk} = k - j$$

$$B = \begin{bmatrix} 0 & 1 & -2 \\ -1 & 0 & -1 \end{bmatrix} \quad b_{11} = 1 - 1 = 0 \\ b_{12} = -2 - 1 = 1 \\ b_{13} = -1 - 1 = -2$$

$$A = \begin{vmatrix} -1 & -4 \\ 1 & -2 \\ 3 & 0 \end{vmatrix}$$

$$b_{23} = 3 - 2 = 1 \\ b_{21} = 3 - (-1) = 4 \\ b_{22} = 2 - 2 = 0 \\ b_{23} = 3 - 2 = -1$$

$$d_{11} = 2 \cdot 1 - 3 \cdot 1 = 2 - 3 = -1$$

$$d_{12} = 2 \cdot 1 - 3 \cdot 2 = 2 - 6 = -4$$

$$d_{13} = 2 \cdot 2 - 3 \cdot 1 = 4 - 3 = 1$$

$$d_{21} = 2 \cdot 2 - 3 \cdot 2 = 4 - 6 = -2$$

$$d_{22} = 2 \cdot 3 - 3 \cdot 2 = 6 - 6 = 0$$

$$d_{23} = 2 \cdot 3 - 3 \cdot 1 = 6 - 3 = 3$$

$$\begin{array}{l} (-1, 0)(-4, -1) \quad (-1, 1)(-4, 0) \quad (-1, 2)(-4, -1) \\ (1, 0)(2, -1) \quad (1, 1)(-2, 0) \quad (1, 2)(-2, -1) \\ (3, 0)(0, -1) \quad (3, 1)(0, 0) \quad (3, 2)(0, -1) \end{array}$$

$$\begin{bmatrix} -0+4 & -1-0 & -2-4 \\ 0+2 & 1-0 & 2-2 \\ 0+0 & 3+0 & 6-0 \end{bmatrix}$$

$$3. A_{3 \times 2} \cdot B_{2 \times 3} =$$

$$\begin{bmatrix} 4 & -1 & -6 \\ 2 & 1 & 0 \\ 0 & 3 & 6 \end{bmatrix}$$

$$\begin{array}{r|rrr} & 4 & -1 & -6 \\ \hline 2 & 1 & 0 & \\ 0 & 0 & 3 & 6 \\ \hline 0 & 1 & -1 & -6 \\ -12 & 2 & 1 & 0 \end{array}$$

$$\det A \cdot B = (24 + 0 - 36) - (0 - 12 + 0)$$

$$\det A \cdot B = -12 + 12$$

$$\det A \cdot B = 0,$$

alternativa (c), //

$$6. A = \begin{vmatrix} 2 & 0 & -1 \\ -1 & 1 & 0 \end{vmatrix}_{2 \times 3}$$

$$B = \begin{vmatrix} 1 & -1 \\ -1 & 1 \\ 0 & 2 \end{vmatrix}_{3 \times 2}$$

$$\begin{bmatrix} (2 \cdot 1)(0 \cdot -1)(-1 \cdot 0) & (2 \cdot -1)(0 \cdot 1)(-1 \cdot 2) \\ (-1 \cdot 1)(1 \cdot -1)(0 \cdot 0) & (-1 \cdot -1)(1 \cdot 1)(0 \cdot 2) \end{bmatrix}$$

$$\begin{bmatrix} 2+0-0 & -2+0-2 \\ -1-1-0 & 1+1-0 \end{bmatrix}$$

$$\begin{array}{|cc|} \hline 2 & -4 \\ -2 & 2 \\ \hline 8 & 4 \\ \hline \end{array}$$

$$A_{2 \times 3} \cdot B_{3 \times 2} = \begin{bmatrix} 2 & -4 \\ -2 & 2 \end{bmatrix}$$

$$\text{der } A \cdot B = 4 - 8 = -4,$$

alternativa (D),