

Advanced Monetary Economics

Lecture 9

Malte Rieth

Martin-Luther-Universität Halle-Wittenberg

Money in a model

- Agents in a DSGE model face the question: Why hold money?
- Not an interest-bearing asset
- Bonds as investment opportunity more attractive
- Need to introduce a feature or friction for money demand

Questions we want to answer

- How to model money demand in a model?
- How does it matter for the transmission mechanism of monetary policy?

1 Money in the utility

- Holding money is positively valued – it yields direct utility.
- This assumption is rationalized by assuming: money gives utility because it provides transaction services.
- Instantaneous utility $U = U(C_t, M_t/P_t, L_t)$ depends on
 - consumption C_t ,
 - the flow of services yielded by real money holdings $\frac{M_t}{P_t}$
 - leisure L_t
- Properties of the utility function: $U_c \geq 0, U_{cc} \leq 0, U_{mm} \leq 0, U_l \geq 0, U_{ll} \leq 0$

- Further assets in the model are bonds.
- Bond B pays a nominal interest rate of $1 + i_{t-1}$.

- Households' budget constraint

$$\frac{(1 + i_{t-1})B_{t-1}}{P_t} + \frac{M_{t-1}}{P_t} = C_t + \frac{B_t}{P_t} + \frac{M_t}{P_t}$$

- For the sake of time we exclude non-negativity constraints and no Ponzi-schemes conditions.
- The intertemporal first-order condition for bonds is

$$\lambda_t = \frac{\beta \lambda_{t+1} (1 + i_t)}{\pi_{t+1}}.$$

- Marginal costs of investment in bonds is to forego consumption today
- The marginal benefit of the investment is
 1. discounted utility of the additional resource next period
 2. plus the expected real interest rate earned on the investment
- Optimality condition for money demand: the intertemporal first-order condition w.r.t. money implies

$$\lambda_t = U_m(C_t, M_t/P_t, L_t) + \frac{\beta \lambda_{t+1}}{\pi_{t+1}}.$$

- Marginal costs of holding money is to forego investment in bonds or the marginal utility from consumption

- The marginal benefit of holding money has two parts:
 1. direct utility
 2. discounted utility of the additional resource next period
- Cost and benefits of holding money: investing in bonds yields nominal interest rate

$$\lambda_t = \frac{\beta \lambda_{t+1} i_t}{\pi_{t+1}} + \frac{\beta \lambda_{t+1}}{\pi_{t+1}}.$$

- Holding money foregoes the nominal interest rate.
- Utility from money is the compensation

$$\lambda_t = U_m(c_t, m_t, l_t) + \frac{\beta \lambda_{t+1}}{\pi_{t+1}}.$$

- How to model money demand in a model? One way is to introduce money on the utility function.
- Agents are willing to hold money because they receive utility from it.
- The costs of holding money is the foregone nominal interest rate.
- An increase in the nominal interest rate increases the cost of holding money.
- Monetary policy in the MIU model: supplies money and follows a money supply rule

$$M_t - M_{t-1} = \theta_t M_{t-1}$$

- A monetary policy shock is an unexpected temporary increase in the money growth rate

$$\theta_t = \theta + \varepsilon_t$$

- **Separability of money:** In case the marginal utility of consumption and leisure are not affected by real money holdings money is modeled separable in the utility function (see tutorial).
- A change in money supply and expected inflation only affect real money holdings
- monetary policy does not have an effect on the economy.
- Important side note: prices are flexible in the model

- **Non-separability of money:** assume marginal utility of consumption depends on money holdings and both are complements (see Gali, Ch. 2.5.2)
- an increase in money supply increases inflation
- a decrease in real money holdings decreases consumption
- the intratemporal first-order condition then requires an increase in leisure
- households work less and output declines
- How does it matter for the transmission mechanism of monetary policy?
- Monetary policy in the MIU model:

- depends on the specification of the utility function
- has an effect on the economy only if the real money balances affect the marginal utility of consumption or leisure

2 Cash in advance (CIA)

- Money does not yield utility.
- Instead it is modeled as a medium of exchange - it is used to purchase goods.
- The household faces an additional constraint: it needs as much money as it wants to consume goods.

- This constraint is called the cash-in-advance constraint.
- **Assumption 1:** What exactly denotes “goods” ?
- Consumption goods only or investment goods too?
- Mostly, only consumption will be cash-in-advance constrained.
- Are all consumption goods constrained or only a part of them?
- The possibility of credit goods exist.
- Today, all consumption will be constrained.

- **Assumption 2:** The timing

- Lucas - timing: Agents can allocate their resources after the shocks have been observed. Asset markets open first - followed by the goods market (see tutorial).
- Svensson - timing: Goods market opens first - followed by the asset market:

$$P_t C_t \leq M_{t-1}.$$

- **Simple CIA model setup:** utility function $u(C_t)$.
- Endowment: M_{t-1}, T_t, B_{t-1}
- T_t are transfers in form of money (helicopter money)

- Svensson - timing. Cash-in-advance constraint in nominal terms given by:

$$P_t C_t \leq M_{t-1} + T_t.$$

- CIA in real terms

$$C_t \leq \frac{m_{t-1}}{\pi_t} + \tau_t.$$

- Maximization problem (no uncertainty)

$$\begin{aligned} \mathcal{L} = & \sum_{t=0}^{\infty} \beta^t \left\{ u(C_t) + \lambda_t \left[(1 + i_{t-1}) \frac{b_{t-1}}{\pi_t} + \frac{m_{t-1}}{\pi_t} - C_t - m_t - b_t \right] \right. \\ & \left. + \mu_t \left[\frac{m_{t-1}}{\pi_t} + \tau_t - C_t \right] \right\} \end{aligned}$$

plus non-negativity constraints and a no-Ponzi condition.

- First-order condition in the CIA model

$$\lambda_t = \beta \frac{\lambda_{t+1} + \mu_{t+1}}{\pi_{t+1}}$$

- Marginal costs of holding money is to forego investment in bonds or consumption
- The marginal benefit of holding money has two parts:
 1. discounted utility of the additional resource next period
 2. discounted easing of the CIA-constraint next period
- Comparison CIA and MIU:
 - CIA

$$\lambda_t = \beta \frac{\mu_{t+1}}{\pi_{t+1}} + \beta \frac{\lambda_{t+1}}{\pi_{t+1}}$$

– MIU

$$\lambda_t = U_m(C_t, m_t, L_t) + \beta \frac{\lambda_{t+1}}{\pi_{t+1}}.$$

- The cost of holding money is in both cases the foregone nominal interest rate:

$$\lambda_t = \beta \frac{\lambda_{t+1} i_t}{\pi_{t+1}} + \beta \frac{\lambda_{t+1}}{\pi_{t+1}}.$$

- Both models add a feature that motivates the agent to hold money.
- How to introduce money demand in a model?
- One way is to introduce money in the utility function.
- Another one is to model money necessary to obtain consumption goods. Agents are willing to hold money because they need it to obtain consumption goods.

- **Interest rates as a tax:** in a standard CIA model: $i_t = \frac{\mu_{t+1}}{\lambda_{t+1}}$.

- First-order condition w.r.t. consumption can be re-written as

$$U_c = \lambda_t (1 + i_{t-1})$$

- Marginal utility exceeds marginal utility of income
- Nominal interest rates, and therefore expected inflation, can be thought of as a tax on consumption.
- What about the effects of monetary policy in the CIA model?
 1. A persistent increase the money supply increases expected inflation and thus nominal interest rates

2. Marginal utility of consumption increases
 3. Agents substitute towards leisure
 4. Labor and output fall
- How does it matter for the transmission mechanism of monetary policy?
 - Monetary policy in the CIA model works through nominal interest rates as a tax on the constrained good
 - depends on the definition of the constrained good
 - depends on the availability of credit
 - Questions we have answered
 1. How to model money demand in a model?

2. How does it matter for the transmission mechanism of monetary policy?