

# Agenda

- Recsys data prep for Content-based
- Regression using Content Based Data
- Collaborative Filtering
  - MF from Scratch
  - Using Library
- Metric for Evaluating Recommendations

mid	Animation	Fantasy	Comedy - - -
①	1	1	0
②	0	1	1
⋮			
1000			

## Optimization Equation

Loss  $\Rightarrow$

Optimize

$$\min_{U_i, I_j} \sum_{i,j} (A_{ij} - U_i I_j)^2$$

S.t.  $A_{ij} \neq \text{Null}$

SGD to find value of  $U_i$  and  $I_j$

Step 1: Initialize matrix  $U$  and Matrix  $I$  randomly  $\text{Dim} = K$

Step 2: Take derivative of loss and update  $U$  and  $I$

$$L = (A_{ij} - U_i I_j)^2$$

$$\frac{\partial L}{\partial u} = (A_{ij} - u_i I_j)^2$$

$$\frac{\partial L}{\partial u_i} = 2(A_{ij} - u_i I_j) \times \left( \frac{\partial A_{ij}}{\partial u_i} - \frac{\partial (u_i I_j)}{\partial u_i} \right)$$

$$= 2(x) \times (0 - 1 \times I_j)$$

$$\frac{\partial L}{\partial u_i} = -2(x) I_j$$

$$\frac{\partial L}{\partial I_j} = -2(x) u_i$$

Learning rate  $\alpha$

$$\Theta \Leftarrow \Theta - \alpha \frac{\partial L}{\partial \Theta}$$

$$u_i = u_i - \alpha 2(x) I_j$$

$$u_i = u_i - \alpha(x) I_j$$

# Metric for Evaluating Recommendations

User : Nina



Overlap  $\Rightarrow$   $\frac{\text{Intersection (recs, positive)}}{\text{Total +ve interaction}}$

$\Rightarrow \frac{3}{4} \Rightarrow 75\%$

Precision @ K

What is K-precision?

- K-Precision is a metric used to evaluate the quality of recommendations provided by recommendation systems.
- It assesses how many of the top-K recommended items are relevant to the user's preferences.
- A higher K-Precision value indicates better recommendation quality.

$$P@K = \frac{\sum \text{Relevant items in top K recommendations}}{\sum \text{Items in top K recommendations}}$$

$$K=10$$

relevant items in 10 sec.

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total item in  $K$