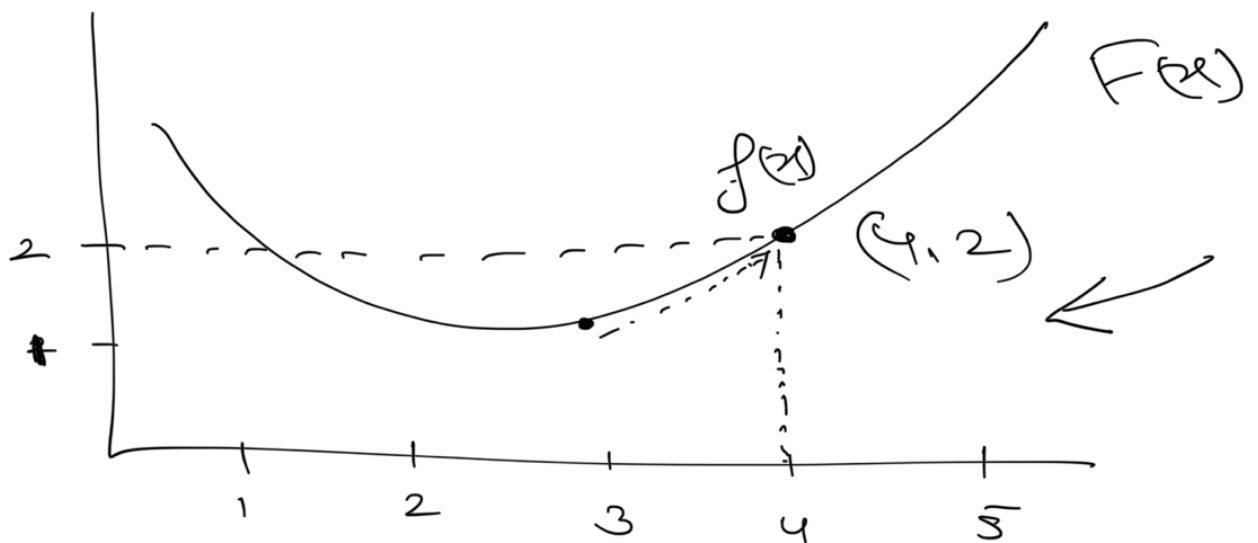


Basic Calculus Part 2

→ Limit at a point



L.H.L

$$\lim_{x \rightarrow 4^-} f(x) \Rightarrow 2$$

3.1, 3.2, ..., 3.9
3.99, 3.999

R.H.L

$$\lim_{x \rightarrow 4^+} f(x) \Rightarrow 2$$

5.1, 5.01, 5.001, 5.000

$\downarrow f(x)$

$$\lim_{x \rightarrow 3^-} (x^2) \Rightarrow 9$$

L.H.L

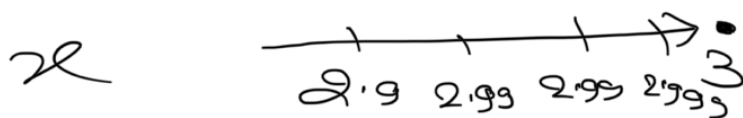
$$x \geq 2.9 \Rightarrow f(x) \geq 8.41$$

$$x \geq 2.99 \Rightarrow f(x) \geq 8.94$$

$$x \geq 2.999 \Rightarrow f(x) \geq 8.994$$

$$x \geq 2.9999 \Rightarrow f(x) \geq 8.9994$$

$$y \geq 9$$



$$y = (x^2) < 2.9$$

R.H.L

$$\lim_{x \rightarrow 3^-} f(x) = 9$$

$$\lim_{x \rightarrow 3^+}$$

$$4.1 \rightarrow 16.81$$

$$3.9 \rightarrow 15.21$$

$$3.7 \rightarrow 13.69$$

$$3.10 \rightarrow 9.61$$

$$3.001 \rightarrow 9.006$$

$$3.0001 \rightarrow 9.000601$$

$$\Rightarrow 9$$

To check continuity

you have to evaluate if

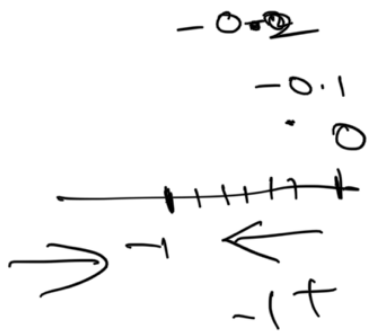
$$L.H.L = R.H.L$$

$$\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$$

$$-0.99$$

$$-0.9$$

$$-0.3$$



$$f(x) \begin{cases} 1 & : x > 0 \\ 0 & : x \leq 0 \end{cases}$$

$$\lim_{x \rightarrow -1^-} f(x) = 0$$

$$\lim_{x \rightarrow -1^+} f(x) = 0$$



$$L.H.L = R.H.L$$

$$\text{at } x = -1$$

$f(x)$ is continuous at $x = -1$

0.7
0.8
0.9

