

Basics of Time and Space Complexity

Algorithm Analysis

memory (RAM)
(Space Complexity)

Computation
Time Complexity

Fun1 \downarrow
2 sec

Fun2 \downarrow
6 sec

Clock Speed 3 GHz

\downarrow
 $\frac{1}{t}$

\Rightarrow

3.5 GHz
 $3 \times 1024 \times 1024 \times 1024$

Big O [$O(n)$]

↑
Polynomial
with Highest
Power

⇒

$$3x^2 + 2x^2 + x$$

Big O ? $5x^2 + x$

↓
 $O(n^2)$

$$\in x^{-2} \Rightarrow cx + x^{1/2} + x^{1/3}$$

↓
 $O(n)$

$$\in x^{-3} \Rightarrow x^{1/2} + 10x$$

$$\Rightarrow x^{1/2} + 10x^0$$

$$O(n^{0.5})$$

$n = 10$
 for i in range(n): $\Rightarrow n$
 Print(i) $\rightarrow n$
 \Rightarrow for y in range(n): $\Rightarrow n$
 for k in range(n):
 Print($y \times k$)

$$2n^2 + 3n + C$$

$$\downarrow$$

$$O(n^2)$$

n

Loop

$$n = n // 2$$

\Rightarrow

$$n \geq n // 3$$

$$\downarrow$$

- ① $n/2 +$
- ② $n/2^2 +$
- ③ $n/2^3 +$
- ...
- $n/2^k +$

$$\log_3 n$$

$$\textcircled{k} \Rightarrow \boxed{n/2^k \leq 1}$$

$$n \leq 2^k$$

$$\log_2 n \geq k \log_2 2$$

$$\boxed{k \geq \log_2 n}$$

Def fact(n) # TC $\Theta(n)$

if $n == 1$:
 return 1

else:

 return n * fact(n-1)

