

Agenda

- ⇒ A new Business Case
- ⇒ Imbalanced Data
- ⇒ Problem with Accuracy
- ⇒ More Robust Metrics
 - ⇒ Confusion Matrix
 - ⇒ Precision Score
 - ⇒ Recall Score
 - ⇒ F1-Score

Business Case

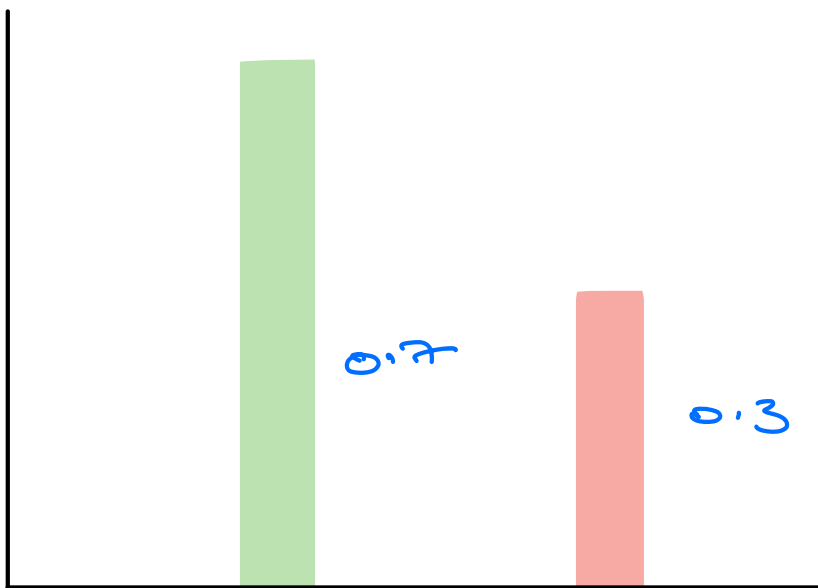
Text	Spam
Hi - - - - -	1
Join scales - - - -	0

0: Non Spam

1: Spam

A Objective : Build a ML model which can classify email as Spam or Not Spam.

Data Distribution

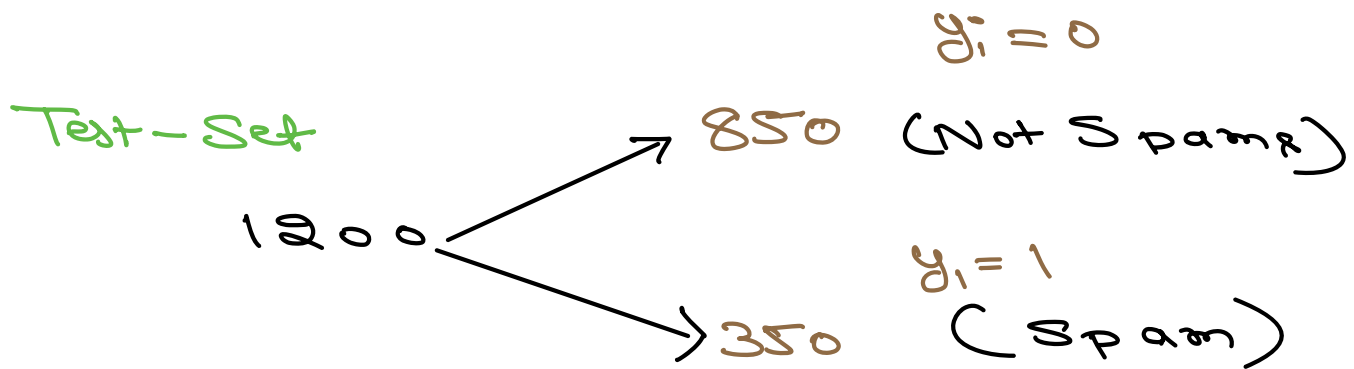


Accuracy 0.93
93%

20 : 100 D1 : Imbalance

80 : 100 D2 : Slightly imbalanced

Problem with Accuracy



Dumb Model: Predicts Every Email as Not-Spam

Accuracy $\hat{y} \geq 0$

$$\frac{850}{1200} \approx 70.8$$

Case 2:

Credit Card Transaction
 \swarrow Fraudulent
 \searrow Non F

NF 99.5 \approx 0.5 F

Extreme imbalance

Always Says $\hat{y} = NF$
 Acc. 99.5%

How to Handle imbalance:

① Data Augmentation

② Update Loss Function

③ Change the Metric ✓

Learn Alternative of Accuracy that give us fair Estimate of Performance irrespective of Distribution.

Confusion Matrix

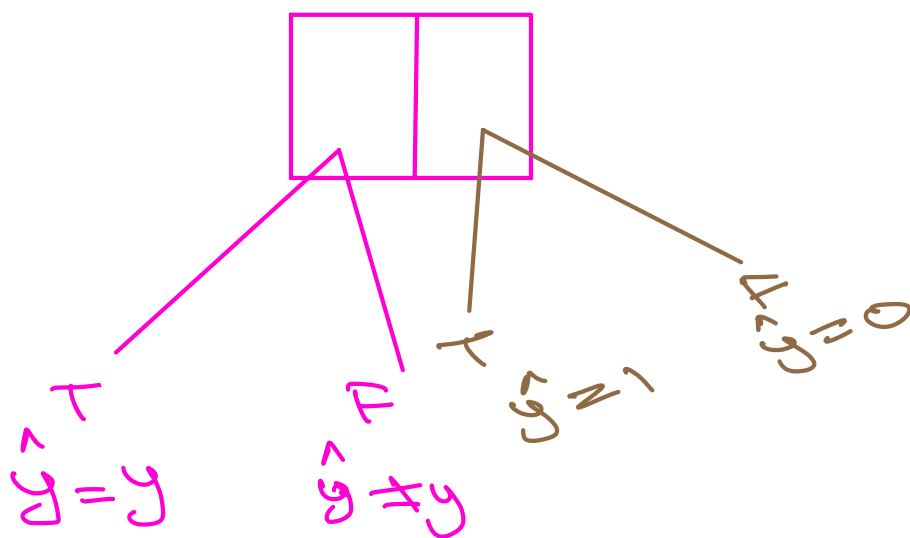
Predicted (\hat{y})

Not Spam (0) Spam (1)

actual (y)	Not Spam (0)	Count y 1 Case 1 $\hat{y}=0$ $y=0$	2 Case 2 $\hat{y}=1$ $y=0$
	Spam (1)	3 Case 3 $\hat{y}=0$ $y=1$	4 Case 4 $\hat{y}=1$ $y=1$

$\hat{y}=0$	$y=0$
$\hat{y}=1$	$y=0$
$\hat{y}=0$	$y=1$
$\hat{y}=1$	$y=1$

①	$\hat{y} = 0$	$y = 0$	True Negative (TN)
②	$\hat{y} = 1$	$y = 0$	False Positive (FP)
③	$\hat{y} = 0$	$y = 1$	False Negative
④	$\hat{y} = 1$	$y = 1$	True Positive



- * First term tells us if model pred is correct/incorrect
- * Second Term tell us pred

Not Spam (0) Spam (1)

Not Spam (0)	TN	FP
Spam (1)	FN	TP

actual (y)

Questions

$$Acc \Rightarrow \frac{TP + TN}{TN + FN + TP + FP}$$

How about multi-class Classification

$K \times K$

1 2 3 4 5 ... K

1						
2						
3						
4						
...						
K						

Predict (\hat{y})

Understanding Confusion Matrix

Test data $\begin{cases} 360 \text{ Not Spam} \\ 40 \text{ Spam} \end{cases}$
 400 DP

Actual \nearrow Predict

Dumb Model

	Not Spam (0)	Spam (1)
Not Spam (0)	360 TP	0 Type-1
Spam (1)	40 Type-2	0 TN

$\hat{y} = \text{majority}$

$$\text{Acc: } \frac{360+0}{400}$$

$\Rightarrow 90\%$

Ideal Model

	Not Spam (0)	Spam (1)
Not Spam (0)	360	0
Spam (1)	0	40

$$\frac{400}{400} = 100\% \text{ Acc}$$

For Ideal Model, which of the following is true?

4 options

Active Duration (Most preferred: 30 seconds)

Appears for 60 Secs

A FP and FN \downarrow , while TP and TN \uparrow

B TP and TN \downarrow , while FP and FN \uparrow

C TP and FN \downarrow , while FP and TN \uparrow

D FP and TN \downarrow , while TP and FN \uparrow

Type of Errors:

FP

FN

Precision

Scenario

$y = 1$

$\hat{y} = 0 \Rightarrow FN$

1) Receiving a Spam in Normal Mailbox

2) Other letter sent to Spam



Actual $\Rightarrow 0$

Spam-folder

Pred $\Rightarrow 1$

FP

FP is Dangerous

Goal should be to minimize FP

$$\text{Precision} \Rightarrow \frac{TP}{TP + FP}$$

$$\hat{y} = 1$$

Among all $y\text{-pred} = 1$, How much was $\text{actual} = 1$

Dumb Model

	Not Spam (0)	Spam (1)
Not Spam (0)	360	0
Spam (1)	40	0

$$\frac{TP}{TP + FP}$$

$$\frac{0}{0 + 0 + 100}$$

\Rightarrow Precision $\Rightarrow 0$

Ideal Model

	Not Spam (0)	Spam (1)
Not Spam (0)	360	0
Spam (1)	0	40

$$\frac{TP}{TP + FP}$$

$$\Rightarrow \frac{40}{40 + 0}$$

Range of Precision $\in [0, 1]$

Recall

Cancer Diagnostic Negative

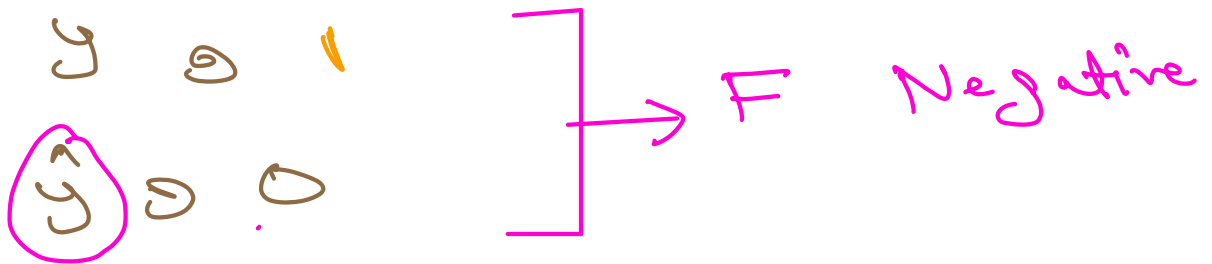
Class 0 : No Cancer

Class 1 : Cancer

① Healthy patient diagnosed as Cancer



② Cancer patient Diagnosed as Healthy



FN is dangerous

$$\text{Recall} = \frac{TP}{TP + FN}$$

Ideal Model

	Not Spam (0) Spam (1)	
actual (y)	Not Spam (0)	360
	Spam (1)	0
actual (y)	Not Spam (0)	0
	Spam (1)	40

$$= \frac{40}{40+0} = 1$$

Dumb Model

	Not Spam (0)	Spam (1)
actual (0) Not Spam (0)	360	0
actual (1) Spam (1)	40	0

$$\text{Recall} = \frac{0}{0+0} = 0$$

range of Recall $\in (0, 1)$

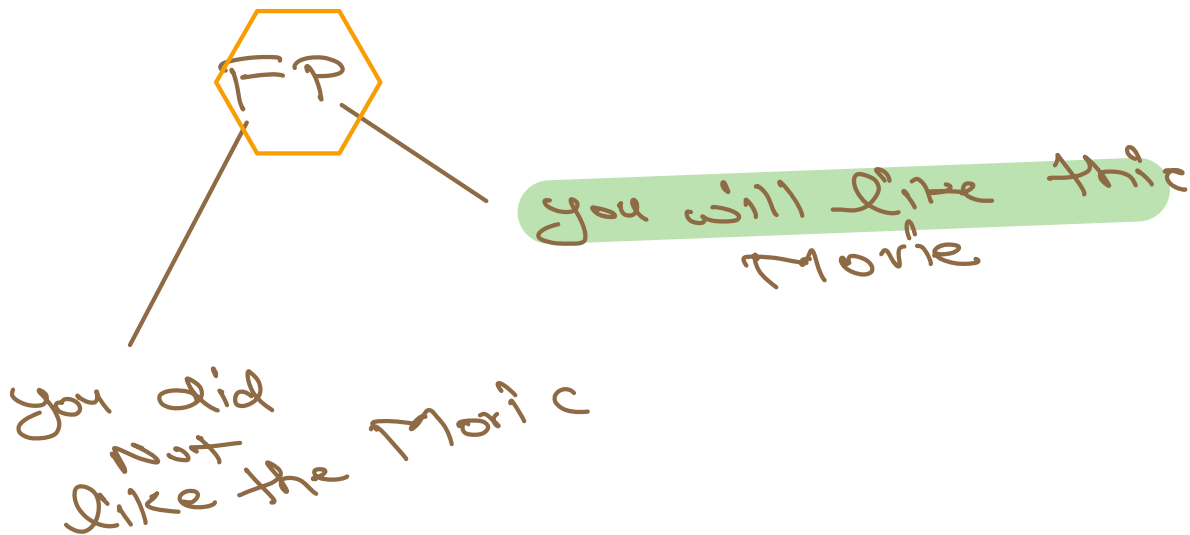
Confusion Matrix

	Not Spam (0)	Spam (1)
actual (0) Not Spam (0)	TN	FP
actual (1) Spam (1)	FN	TP

Numerator is always TP

Precision \Rightarrow Denom is Last Col

Recall \Rightarrow Denom is Last Row



min FP & Precision
Max

* min FP & Precision Max

if Both FP and FN
are great Mistakes

F1 - Score : $\frac{1}{\frac{1}{P} + \frac{1}{R}}$ & $\frac{2PR}{P+R}$

$$\frac{P+R}{2}$$

	P	R	Avg (P+R)/2
M1	0.3	0.8	0.55
M2	0.9	0.3	0.55
M3	0.7	0.40	0.55

	P	R	F-Score	$\frac{2PR}{P+R}$
M1	0.3	0.88	0.43	
M2	0.9	0.2	0.33	
M3	0.7	0.40	0.51	Best Model

F1 - Score adds penalty

if either of P and R is Low

Why does the F-1 score use Harmonic Mean (HM) instead of Arithmetic Mean (AM) ?

4 options

Active Duration (Most preferred: 30 seconds)

Appears for

60 Secs

A

AM penalizes models the most when even Precision and Recall are low.

B

HM penalizes models the most when even Precision and Recall are low.

C

HM penalizes models the most when even Precision and Recall are high.

P is Low 3 P
R is High

R is Low 3 R
P is High

CC \swarrow NP
 \searrow P