

Basics of R software.

- ① R is a software for statistical analysis and data computing.
- ② It is an effective data handling software and outcome storage is possible.
- ③ It is capable of graphical display.
- ④ It is a free software.

problem 1 :- solve the following

- ① $4 + 6 + 8 \div 2 - 5$
- ② $2^2 + | -3 | + \sqrt{45}$
- ③ $5^3 + 7 \times 5 \times 8 + 46/5$
- ④ $\sqrt{4^2 + 5 \times 3 + 7/16}$
- ⑤ round off
 ~~$4.687 + 9 \times 8$~~

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one

(1) $24 + 6 + 8 / 2 - 5$

[1] 9

(2) $2^2 + \text{abs}(-3) + \sqrt{45}$

[1] 13.7082

(3) $5\sqrt{3} + 7 * 5 * 8 + 46 / 5$

[1] 414.2

(4) $\sqrt{4 \cdot 2 + 5 \cdot 3 + 7 \cdot 6}$

[1] 5.671567

(5) round ($46.17 + 9 \cdot 8$)

[1] 79.

of problem (2)

(2)

(i) $C(2, 3, 5, 7) * 2$

(ii) $C(2, 3, 5, 7) * (2 \cdot 3)$

(iii) $C(2, 3, 5, 7) * C(2, 3, 6, 2)$

(iv) $C(1, 6, 2, 3) * C(-2, -3, -4, -1)$

(v) $C(2, 3, 5, 7) \wedge 2$

(vi) $C(4, 6, 8, 9, 4, 5) \wedge C(1, 2, 3)$

(vii) $C(6, 2, 7, 5) \wedge C(4, 5)$

$$\text{(ii)} \quad C(2, 3, 5, 2) * 2 \\ \text{C1)} \quad 4 \quad 6 \quad 10 \quad 14$$

$$\text{(iii)} \quad C(2, 3, 5, 7) * C(2, 3) \\ \text{C1)} \quad 4 \quad 9 \quad 10 \quad * 21$$

$$\text{(iv)} \quad C(2, 3, 5, 7) * C(-2, -3, 6, 2) \\ \text{C1)} \quad 4 \quad 9 \quad 30 \quad 14$$

$$\text{(v)} \quad C(1, 6, 2, 3) * C(-2, -3, -4, -1) \\ \text{C1)} \quad -2 \quad -18 \quad -8 \quad -3$$

$$C(2, 3, 5, 7) \wedge 2.$$

$$\text{C1)} \quad 4 \quad 9 \quad \cancel{25} \quad \cancel{49}.$$

$$\text{(vi)} \quad C(4, 6, 8, 9, 4, 5) \wedge C(1, 2, 3).$$

$$\text{C1)} \quad 4 \quad 36 \quad 512 \quad 9 \quad 16 \quad 125$$

$$\text{(vii)} \quad C(6, 2, 7, 5) [5 (4, 5)]$$

$$\text{C1)} \quad 1.50 \quad 0.40 \quad 1.75 \quad 1.00$$

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problem 3 :-

$$\text{Q/ } x = 20$$

$$y = 30$$

$$z = 2.$$

$$\text{find i) } x^2 + y^3 + z$$

$$\text{ii) } \sqrt{x^2+y}$$

$$\text{iii) } x^2 + y^2$$

Ans.

$$\therefore x = 20$$

$$\therefore y = 30$$

$$\therefore z = 2$$

$$\therefore x^2 + y^3 + z$$

$$[1] 27402$$

$$\therefore \sqrt{x^2+y}$$

$$[1] 20.73644$$

$$\therefore x^2 + y^2$$

$$[1] 1300.$$

problem 4 :-

create matrix

$$x = \begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$$



my $\gamma \times \zeta$ - matrix [n row = 4, n col = 2, data = 55
 $\{1, 2, 3, 4, 5, 6, 7, 8\}$]

$$\begin{bmatrix} C_{1,1} & 1 \\ C_{2,1} & 2 \\ C_{3,1} & 3 \\ C_{4,1} & 4 \end{bmatrix} \quad \begin{bmatrix} C_{1,2} \\ C_{2,2} \\ C_{3,2} \\ C_{4,2} \end{bmatrix} = \begin{bmatrix} 5 \\ 6 \\ 7 \\ 8 \end{bmatrix}$$

problem 5 :-

find $x+y$ and $2x+3y$ where

$$x = \begin{bmatrix} 4 & 7 & 9 \\ -2 & 0 & -5 \\ 6 & 7 & 3 \end{bmatrix}$$

$$y = \begin{bmatrix} 10 & 12 & 15 \\ -5 & -4 & -6 \\ 7 & 9 & 5 \end{bmatrix}$$

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix} \quad y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

~~Ans.~~
 > x<-matrix(c(4, 7, 9, -2, 0, -5, 6, 7, 3), nrow=3, ncol=3, data=rnorm(9))
 > y<-matrix(c(10, 12, 15, -5, -4, -6, 2, 9, 1), nrow=3, ncol=3, data=rnorm(9))

> x+y

	[C, 1]	[C, 2]	[C, 3]
[1,]	14	-7	13
[2,]	19	-4	16
[3,]	24	-4	8

> 2 * x + 3 * y

	[C, 1]	[C, 2]	[C, 3]
[1,]	38	-19	33
[2,]	50	-12	41
[3,]	63	-28	21

Q/ Problem 6 : Create table.

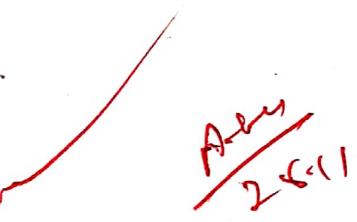
(a) marks of statistic of 18 students

59, 20, 35, 24, 46, 56, 55, 45, 29,
22, 47, 58, 54, 40, 50, 32, 36, 29, 35,
39

x = c(59, 20, 25, 24, 46, 56, 55, 45, 27,
22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)
length (in)

c, 20
> breaks = seq(20, 60, 5)
> a = cut(x, breaks, right = FALSE).
> b = table(a)
> c = transform(b)
> L.
>

op	a	freq
1	[20, 25)	3
2	(25, 30)	2
3	[30, 35)	1
4	(35, 40)	4
5	[40, 45)	1
6	(45, 50)	3
7	[50, 55)	2
8	(55, 60)	4



PRATICAL - 2 (PROBABILITY DISTRIBUTION)

Check whether the followings are pmf or not.

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x	$P(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

x	1	2	3	4	5
$P(x)$	0.2	0.2	0.3	0.2	0.2
	0.2	0.2	0.3	0.2	0.2
	0.2	0.2	0.3	0.2	0.2
	0.2	0.2	0.3	0.2	0.2

x	10	20	30	40	50
$P(x)$	0.2	0.2	0.35	0.15	0.1
	0.2	0.2	0.35	0.15	0.1
	0.2	0.2	0.35	0.15	0.1
	0.2	0.2	0.35	0.15	0.1

(i) Since $P(2) = -0.5$, it can't be a pmf
since pmf $P(x) \geq 0 \forall x \in \mathbb{N}$

(ii) It cannot be a pmf as in pmf
 $\sum P(x) \neq 1$

\Rightarrow Prob = $C(0.2, 0.2, 0.3, 0.2, 0.2)$
 \Rightarrow sum (Prob)

(1) 1.0.

Ans iii)

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Since $\sum P(x) = 1$ if it is a pmf
 $\rightarrow \text{Prob} = C(0.2, 0.2, 0.35, 0.15, 0.1)$
 $\rightarrow \text{sum(Prob)}$
 $\rightarrow [1] 1$

Q 2

(i) Find c.d.f for the following p.m.f and sketch the graph.

x	10	20	30	40	50
$P(x)$	0.2	0.2	0.35	0.15	0.1

Ans

$\rightarrow \text{Prob} = C(0.2, 0.2, 0.35, 0.15, 0.1)$
 $\rightarrow \text{sum(Prob)}$

C 1) I

cumsum (Prob)

C 1) 0.20 0.40 0.75 0.90 1.00

$$F(x) = 0.1$$

$$= 0.2$$

$$10 \leq x < 20$$

$$= 0.4$$

$$20 \leq x < 30$$

$$= 0.75$$

$$30 \leq x < 40$$

$$= 0.95$$

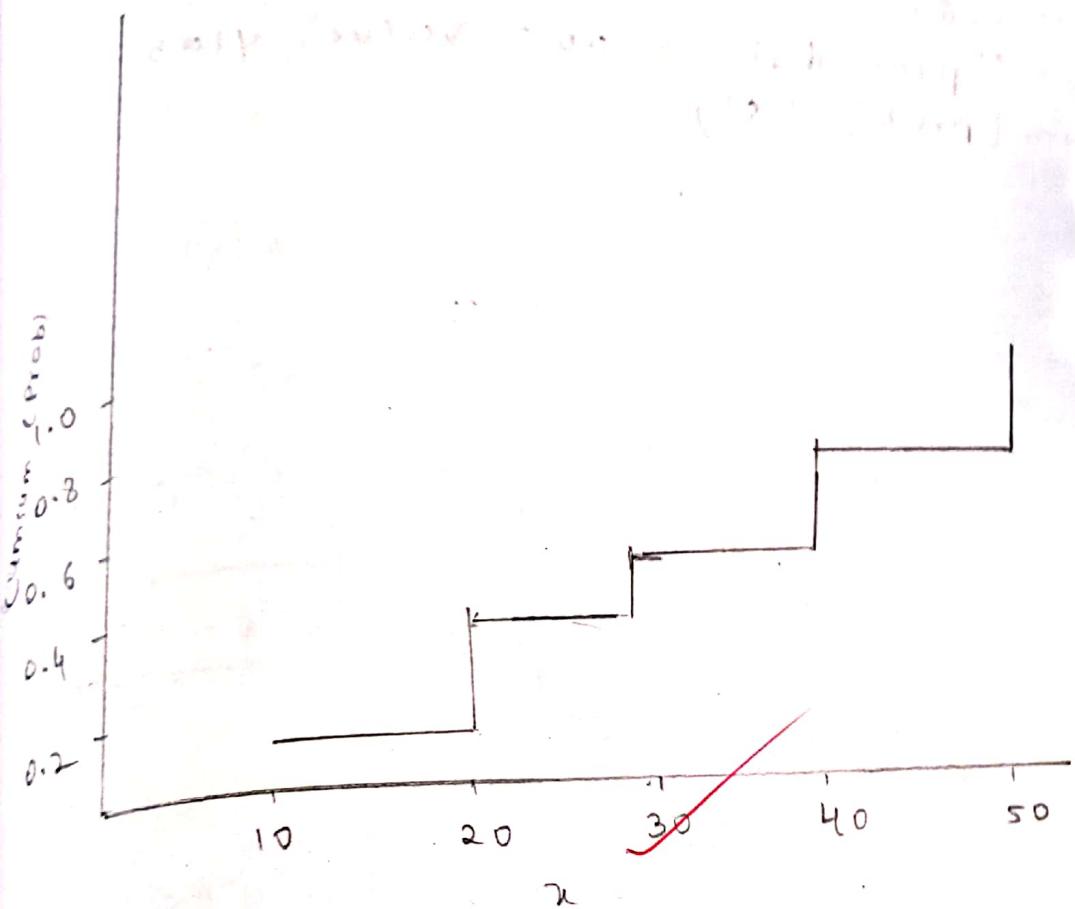
$$40 \leq x < 50$$

$$= 1.0$$

$$x \geq 50$$

$$\rightarrow x = C(10, 20, 30, 40, 50)$$

$\rightarrow \text{plot}(x, \text{cumsum(Prob)}, "s")$



x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.2	0.3 0.2	0.1

$\text{prob} = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$

$\text{sum}(\text{prob})$

c]

cumsum(prob)

c) 0.15 0.40 0.50 0.70 0.90 1.00

$F(x) = 0$

$x < 1$

$1 \leq x < 2$

$2 \leq x < 3$

$3 \leq x < 4$

$4 \leq x < 5$

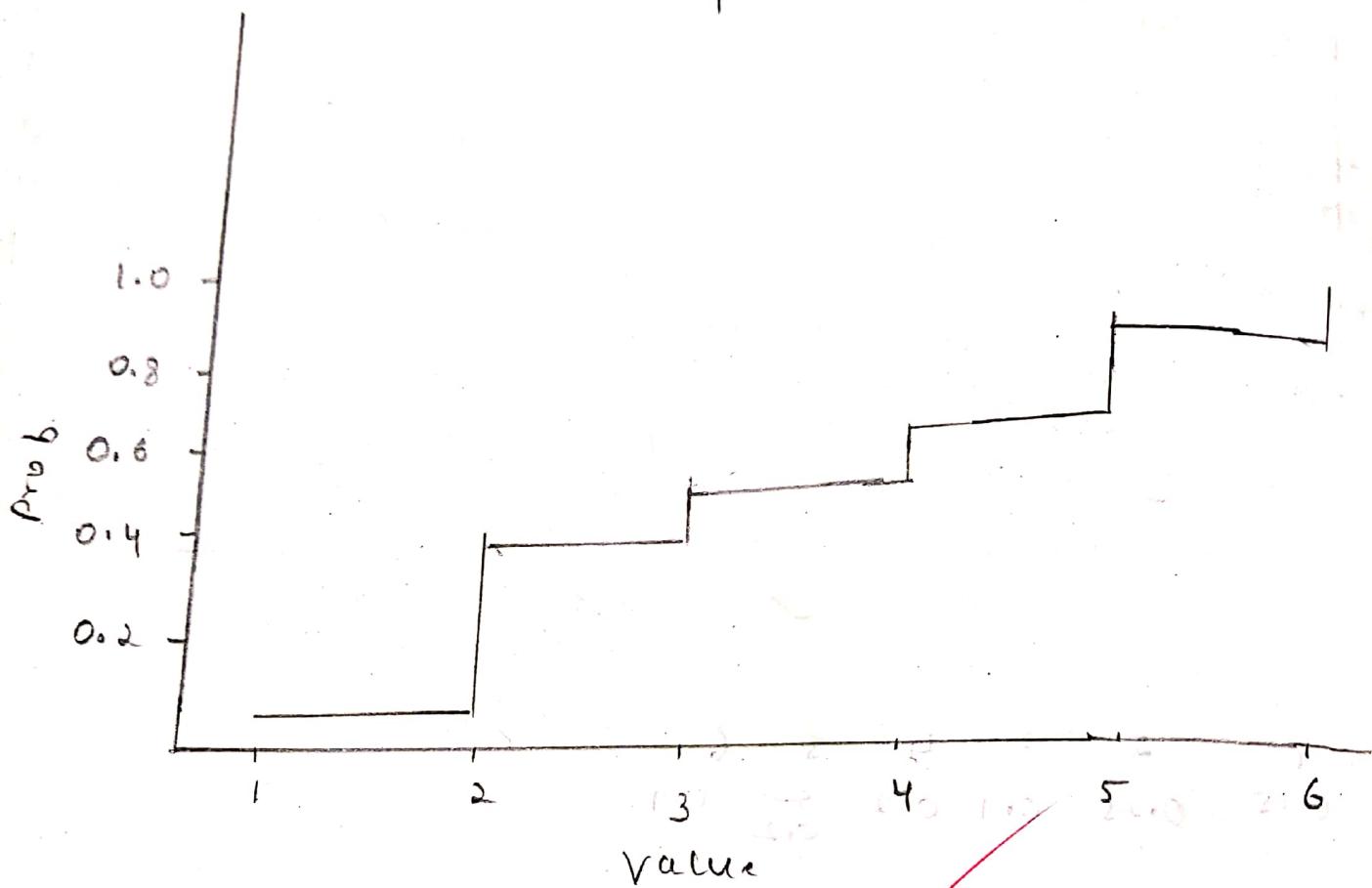
$5 \leq x < 6$

$x \geq 6$

$$X = c(1, 2, 3, 4, 5, 6)$$

\rightarrow plot(x, main = "prob dist", xlab = "value", ylab = "prob",
 cumsum(prob), "s").

prob dist



check whether the following is pdf or not.

$$\text{i) } f(x) = 3 - 2x \quad ; \quad 0 \leq x \leq 1$$

$$\int_0^1 f(x) dx$$

$$\int_0^1 (3 - 2x) dx$$

$$\int_0^1 (3 dx - \int_0^1 2x dx)$$

$$\left[3x - x^2 \right]_0^1 = 2$$

$$= 2$$

~~$$\text{ii) } \int_0^1 3x^2 dx$$~~

~~$$= 3 \int_0^1 x^2 dx$$~~

~~AN
S~~

~~$$= 3 \left[\frac{x^3}{3} \right]_0^1$$~~

~~$$= 3 \left[x^3 \right]_0^1$$~~

~~3~~

~~$$(1 - 0)$$~~

~~$$= 1$$~~

PRATICAL - 3

Q3

Topic :- Binomial distribution.

(i) command:-

(i) $P(X=x) = \text{dbinom}(x, n, p)$.

(ii) $P(X \leq x) = \text{Pbinom}(x, n, P)$.

(iii) $P(X > x) = 1 - \text{Pbinom}(x, n, P)$.

(iv) If x is unknown:

$$P_i = P(X \leq x) \quad q \text{ binom}(P_i, n, P).$$

Problem
Q1

find the probability of exactly 10 success in 100 trials with $p=0.1$.

Q2

Suppose there are 12 mcq. Each questions have 5 option out of which one is correct. find the probability

(i) exactly 4 correct answer

(ii) Almost 4 correct answers

(iii) more than 5 correct answers

Q3) find the complete distribution when $n=5$ and $p=0.1$

Q4) $n=12$, $p=0.25$. find the following probability.

i) $P(X=5)$

ii) $P(X \leq 5)$

iii) $P(X > 7)$

iv) $P(5 < X < 7)$

> dbinom (10, 100, 0.1)
 [1] 0.1318653

> dbinom (4, 12, 0.2)
 [1] 0.1328756

> pbinom (4, 12, 0.2)
 [1] 0.9274445

> 1 - pbinom (5, 12, 0.2)
 [1] 0.01940528

> dbinom (0:5, 5, 0.1)

[1] 0.59049 0.32805, 0.07290 0.00810, 0.00045 0.0009

> dbinom (5, 12, 0.25)

[1] 0.1032414

> pbinom (5, 12, 0.25)

[1] 0.9455978

> 1 - pbinom (7, 12, 0.25)

[1] 0.00278151

> dbinom (6, 12, 0.25)

[1] 0.04014945

Ans 5 > $\text{dbinom}(0, 10, 0.15)$

[1] 0.1968744

> $1 - \text{pbisnom}(3, 20, 0.15)$

[1] 0.3522748

Ans 6 > $\text{qbinom}(0.88, 30, 0.2)$

[1] 9

Ans 7 > $n = 10; p = 0.3$

> $x = 0; n$

> $\text{prob} = \text{dbinom}(x, n, p)$

> $d = \text{data.frame}($ "x value":= x , "probability":= prob)

> $\text{print}(d)$

	x value	probability
1	0	0.0282
2	1	0.12108
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.0001
11	10	0.000059

The probability of a salesman making a sale to a customer is 0.15. find the probability of
 ① no sale out of 10 customer.
 ② more than 3 sells out of 20 customer.

A salesman has a 20% probability of making a sell to a customer out of 30 customer what minimum no of sells the he can make with 88% probability.

~~x follows binomial distribution with $n=10$,
 $p=0.3$, plot the graph of p.m.f and c.d.f.~~

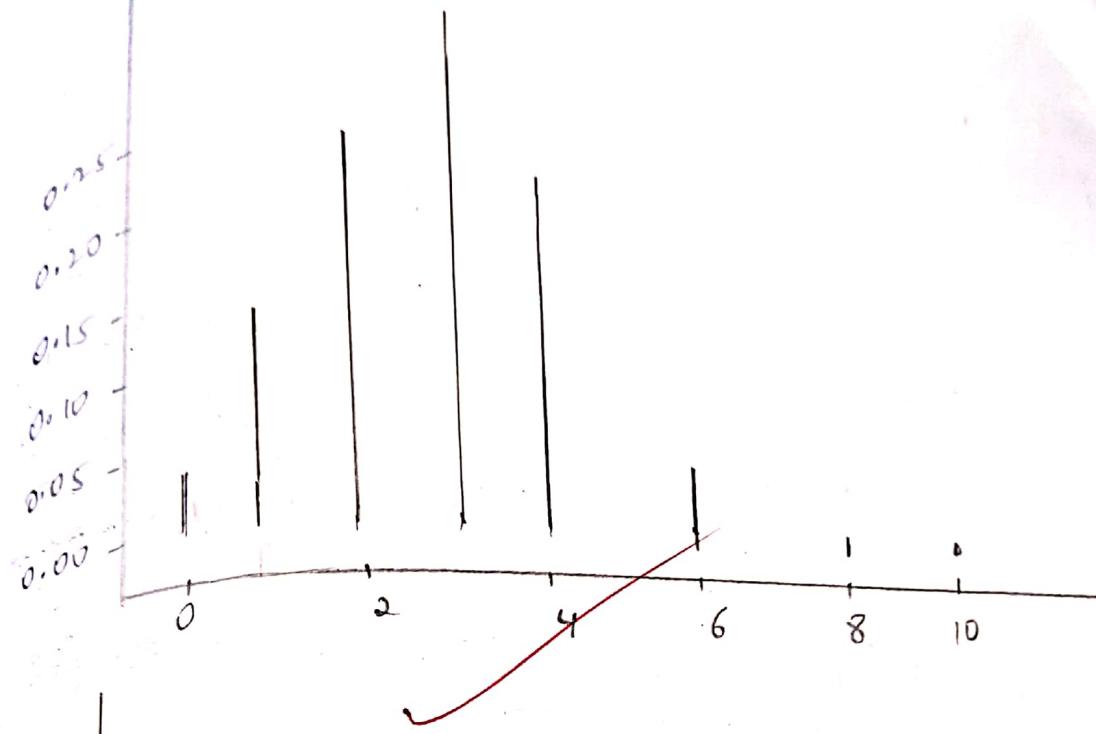
10. 5.2.2

Ans 7

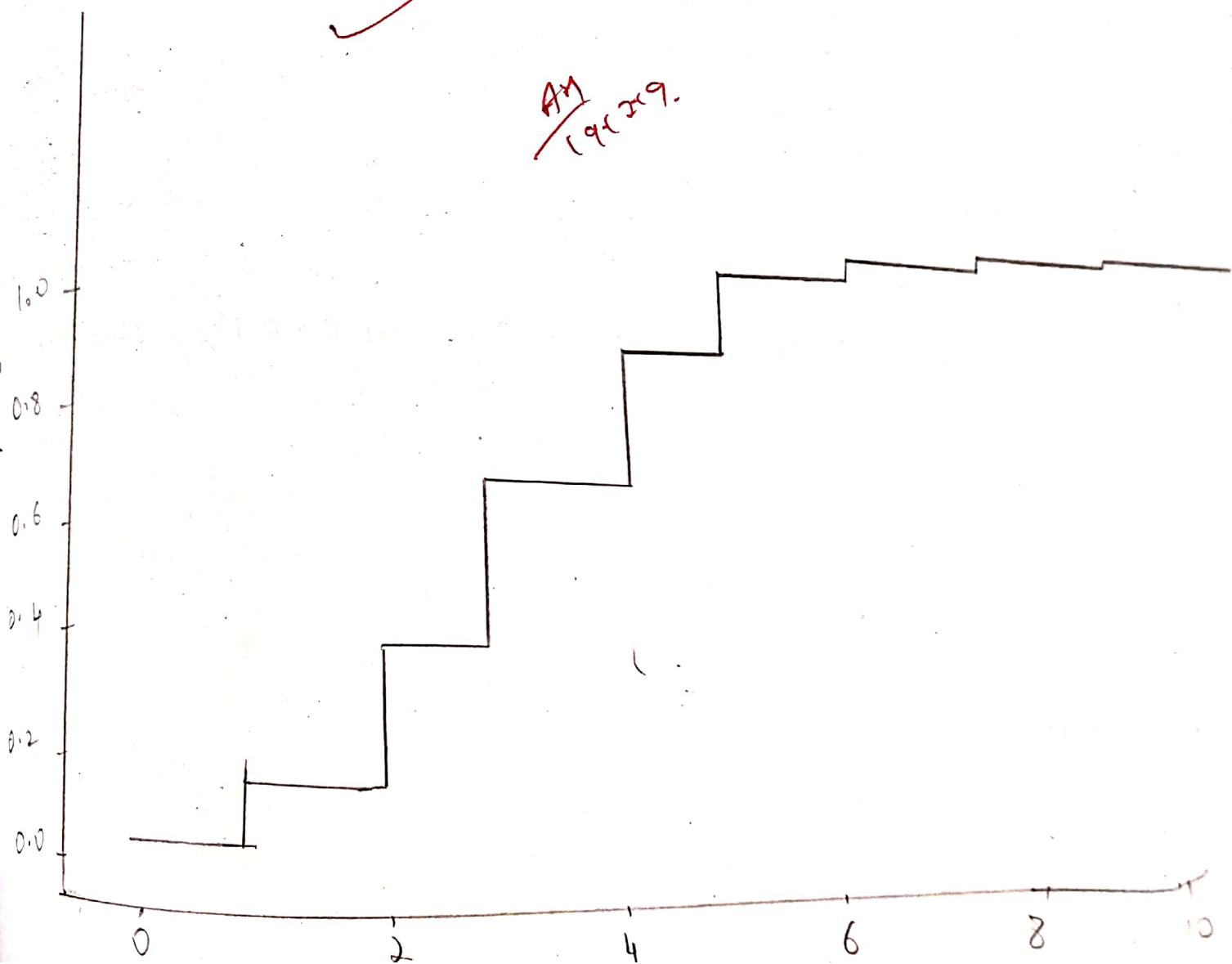
(ii) $\text{plot}(x, \text{prob}, "h")$

Scatter plot of Prob. against h

Prob vs h



$\lim_{x \rightarrow x_0}$



Ans 11)

$$(i) > p_1 = \text{pnorm}(15, 12, 3)$$

> p_1

[1] 0.8413447

$$> cat("P(X \leq 15) = ", p_1)$$

$$P(X \leq 15) = 0.8413447$$

$$> p_2 = \text{pnorm}(13, 12, 3)$$

> p_2

[1] 0.6305587

$$> cat("P(X \leq 13) = ", p_2)$$

$$P(X \leq 13) = 0.6305587$$

$$> p_3 = \text{pnorm}(10, 12, 3) - \text{pnorm}(13, 12, 3)$$

> p_3

[1] 0.3780661

$$> cat("P(10 \leq X \leq 13) = ", p_3)$$

$$P(10 \leq X \leq 13) = 0.3780661$$

$$> p_3 = 1 - \text{pnorm}(14, 12, 3)$$

> p_3

[1] 0.2524925

$$> rnorm(5, 12, 3)$$

[1] 10.000860 11.260263 13.128796 4.060977 10.04136

PRACTICAL 4:

Topic :- Normal distribution.

$$P(X=x) = dnorm(x, \mu, \sigma)$$

$$P(X \leq x) = pnorm(x, \mu, \sigma)$$

$$P(X > x) = 1 - pnorm(x, \mu, \sigma)$$

To generate random numbers from a normal distribution (in random numbers).

The R code is:-

`rnorm(n, mu, sigma)`

problems

- (i) A random variable X follows normal distribution with mean $\mu = 12$ and S.D $= \sigma = 3$ find
- (i) $P(X \leq 15)$
 - (ii) $P(10 \leq X \leq 13)$
 - (iii) $P(X > 14)$
 - (iv) Generate 5 observations (random numbers)

- (ii) X follows Normal Distribution with $\mu = 10$ $\sigma = 2$. find : (i) $P(X \leq 7)$ (ii) $P(5 < X < 12)$
 (iii) $P(X > 12)$ (iv) Generate 10 observation
 (v) Find μ such that probability $P(X \leq \mu) = 0.4$

Q3-

(Q3) Generate 5 random numbers from a normal distribution $\mu = 15$, $\sigma = 4$ find sample mean, median, S.D and print it

(Q4) X follows $X \sim N(30, 100)$ $\mu = 30$, $\sigma = 10$.

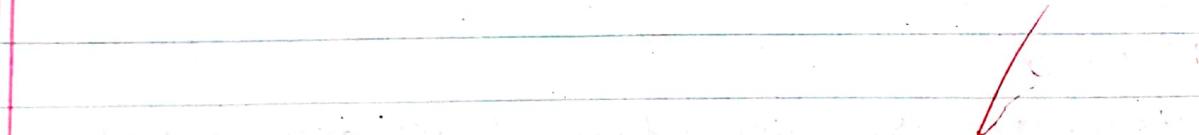
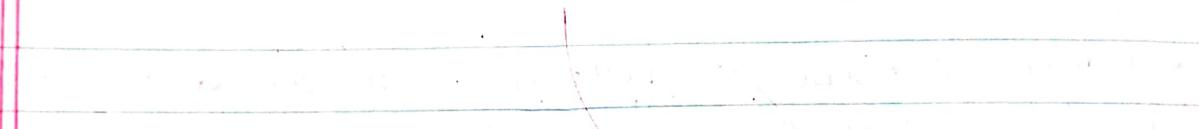
i) $P(X \leq 40)$

ii) $P(X > 35)$

iii) $P(25 \leq X \leq 35)$

iv) find k such that $P(X \leq k) = 0.6$

(Q5) plot the standard normal graph.



prg
→ $p_1 = \text{pnorm}(7, 10, 2)$

→ p_1

[1] 0.0668072

→ $p_2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$

→ p_2

[1] 0.7935544

→ $p_2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$

→ p_2

[1] 0.8351351

→ $p_3 = 1 - \text{pnorm}(12, 10, 2)$

→ p_3

[1] 0.1586553

→ $\text{qnorm}(10, 10, 2)$

→ [1] 7.214873 6.846673 12.425003 10.724589 11.129223

→ [1] 9.917492 10.114098 10.856805 11.489663

→ $\text{qnorm}(0.4, 10, 2)$

→ [1] 9.493306

prg

→ $p_1 = \text{pnorm}(40, 30, 10)$

→ p_1

[1] 0.8413447

→ $p_2 = 1 - \text{pnorm}(35, 30, 10)$

→ p_2

[1] 0.3085375

cat [$P(X \leq 40) =$ ", p_1]

$P(X \leq 40) = 0.8413447$

cat [$P(X \geq 35) =$ ", p_2]

$P(X \geq 35) = 0.3085375$

→ $p_3 = \text{pnorm}(35, 30, 10) - \text{pnorm}(25, 30, 10)$

→ p_3

[1] 0.3829249

→ $\text{qnorm}(0.6, 30, 10)$

[1] 32.083347

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Ans 3 $\rightarrow x = \text{rnorm}(5, 15/4)$

$\rightarrow \text{am} = \text{mean}(x)$

$\rightarrow \text{me} = \text{median}(x)$

$\rightarrow n = 5$

$\rightarrow \text{variance} = (n-1) * \text{var}(x)/n$

$\rightarrow \text{sd} = \text{sqrt}(\text{variance})$

$\rightarrow x$

(1) 14.72018 (15.11361 (2) 39856 (1) 39826 (1) 70728

$\rightarrow \text{am}$

(1) 13.4677

$\rightarrow \text{me}$

(1) 13.70728

$\rightarrow \text{variance}$

(1) 1.9516858

$\rightarrow \text{cat}("sample mean is", \text{am})$

Sample mean is = 13.4677 $\rightarrow \text{cat}("sample median is", \text{me})$

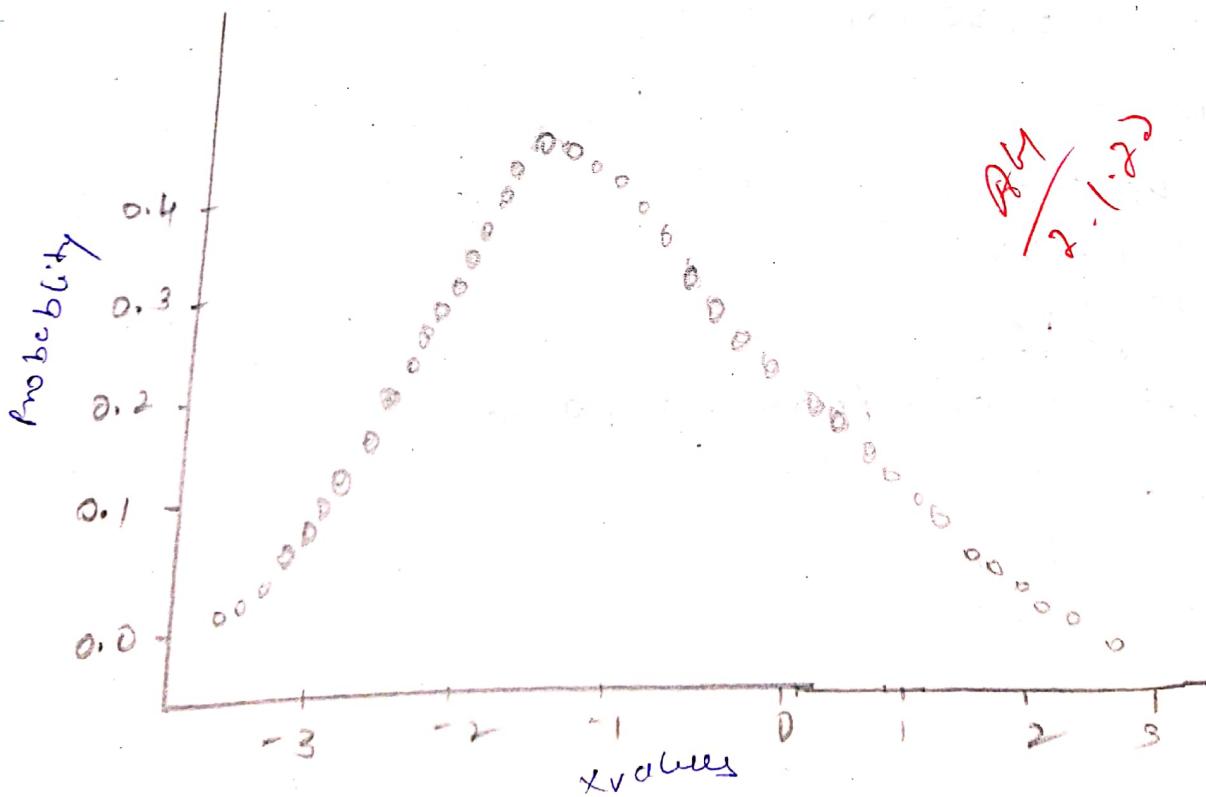
Sample median is 13.70728 $\rightarrow \text{cat}("sample sd is", \text{sd})$

sample sd is 1.397018

Ans 5 $\rightarrow x = \text{seq}(-3, 3, \text{by} = 0.1)$

$\rightarrow y = \text{dnorm}(x)$

$\rightarrow \text{plot}(x, y, \text{xlab} = "xvalues", \text{ylab} = "probability", \text{main} = "standard normal graph")$



PRATICAL-5

Normal and t-Test

- 1) Test the hypothesis $H_0: \mu = 15$, $H_1: \mu \neq 15$ where H_0 : Null Hypothesis and H_1 : Alternative Hypothesis. A random sample mean is 14 and s.d is 3. Test the hypothesis at 5% level of significance.

$$\rightarrow m_0 = 15; m_x = 14; s_d = 3; n = 400$$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

z_{cal}

[1] -6.666667

> cat ("calculated value at z is:", z_{cal})

> pvalue = 2 * (1 - pnorm (abs (z_{cal})))

> pvalue

[1] 2.616796e-11

∴ Pvalue is less than 0.05, we reject $H_0: \mu = 15$

- 2) Test the Hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$. If random sample of size 100 is drawn with sample mean 10.2 and s.d 2.25. Test the hypothesis at 5% level of significance

$$\Rightarrow m_0 = 10; m_x = 10.2; s_d = 2.25; n = 400$$

$$> z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

> $-z_{\text{cal}}$

[1] 1.77778

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" calculated value at 2: " , zcat)

$$\begin{aligned} & \text{" calculated value at 2 is } 1.77778 \\ & = 2 * (1 - \text{Norm}(\text{abs}(zcat))) \end{aligned}$$

value
0.07544036

i) pvalue is more than 0.05, we accept H_0 . i.e. 10

Test the Hypothesis (H_0). Proportion of smokers in our college is 0.125. A sample is calculated and it is collected and calculated 0.125. Test the Hypothesis at 5% level of significance
sample size is 4000

$$\begin{aligned} & p = 0.125; n = 4000; q = 1 - p \\ & p = (p - q) / (\sqrt{q * p * n}) \\ & z_{\text{cal}} = \end{aligned}$$

z_{cal}

$$\begin{aligned} & \text{at } z_{\text{cal}} \text{ calculated value at 2 is } 2.75 \\ & \text{calculated value at 2 is } 3.75 \\ & \text{pvalue } = 2 * (1 - \text{Norm}(\text{abs}(zcat))) \end{aligned}$$

pvalue
0.000146834

i) pvalue is less than 0.05, we reject H_0 : ~~= 0.2~~

Last year, farmers lost 20% of their crops. A random sample of 60 fields are collected and it is found that 9 fields are insect polluted. Test the Hypothesis at 1% of significance

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> p = 20/100; p = 9/60; n = 60; q = 1-p

> zcal = 2 * (1 - pnorm(abs(zcal)))

[1] -0.9682458

> cat("calculated value at z is", zcal)

Calculated value at z is -0.9682458

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.3324216

∴ pvalue is more than 0.05, we accept H_0 .

5) Test the Hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

> x = c(12.25, 11.97, 12.15, 12.08, 13.31, 12.28, 11.94, 11.89, 12.06, 12.04)

> n = length(x)

> n

[1] 10

> m0 = 12.5

> m0

[1] 12.5

> mx = mean(x)

> mx

> var = (n-1) * var(x)/n

> var

[1] 0.019821

> sd = sqrt(var).

> sd

[1] 0.1397176

> zcal = (mx - m0) / (sd / (sqrt(n)))

> zcal

[1] -8.894909

> cat("calculated value is", zcal)

calculated value is -8.894909.

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0

∴ pvalue is less than 0.05, we reject H_0 .

PRACTICAL - 6 (Large Sample Test) • 67

$m_0 = 280$; $m_1 = 275$; $s_d = 20$; $n = 100$

$$z_{\text{cal}} = (m_1 - m_0) / (s_d / \sqrt{n})$$

z_{cal} ("calculated value of z_{cal} "),

calculated value is -2.582333 .

$$p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

p_{val} :

(i) $\alpha = 0$
"cut" since, Pralue is less than 0.05 , Hence we reject H_0
since, Pralue is less than 0.05 , Hence we reject H_0

$\hat{P} = 0.8$, $\hat{Q} = 1 - \hat{P}$; $P = 80/1000$; $Q = 200/1000$

$$z_{\text{cal}} = (\hat{P} - P) / (\sqrt{P * Q / n})$$

z_{cal} ("calculated value is", z_{cal})

calculated value is -3.652847

$$p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

p_{val} :

(ii) $7.72268e-0.5$

"cut" since, Pralue is less than 0.05 , Hence, we reject H_0 at 5% level")

since, Pralue is less than 0.05 , Hence, we reject H_0 at 5% level of significance.

\rightarrow 3) $n_1 = 1000; n_2 = 2000; \bar{m}_x_1 = 67.5; \bar{m}_x_2 = 68; s_d = 2.5;$

$$s_d = 2.5.$$

$$\rightarrow z_{\text{cal}} = (\bar{m}_x_1 - \bar{m}_x_2) / \sqrt{(s_d^2/n_1) + (s_d^2/n_2)}.$$

$\rightarrow \text{cat} (" \text{calculated value is } ", z_{\text{cal}})$

$\rightarrow \text{calculated value is } -5.163978$

$$\rightarrow p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$\rightarrow p_{\text{val}}.$

$$[1] 2.41754e-07$$

$\rightarrow \text{cat} (" \text{since, pvalue is less than } 0.05). \text{ Hence,}$

$\rightarrow \text{we reject } H_0 \text{ at } 5\% \text{ level of significance")}$

$\rightarrow \text{since pvalue is less than } 0.05. \text{ Hence, we reject}$

$H_0 \text{ at } 5\% \text{ level of significance.}$

\rightarrow 4) $n_1 = 84; n_2 = 34; \bar{m}_x_1 = 61.2; \bar{m}_x_2 = 59.4; s_d = 7; s_d = 7$

$$\rightarrow z_{\text{cal}} = (\bar{m}_x_1 - \bar{m}_x_2) / \sqrt{(s_d^2/n_1) + (s_d^2/n_2)}$$

$\rightarrow \text{cat} (" \text{calculated value is } ", z_{\text{cal}})$

$\rightarrow \text{calculated value is } 1.162528$

$$\rightarrow p_{\text{val}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$\rightarrow p_{\text{val}}.$

$$[1] 0.245024$$

$\rightarrow \text{cat} (" \text{since, pvalue is greater than } 0.05). \text{ Hence, we accept } H_0 \text{ at } 1\% \text{ level of significance")}$

$\rightarrow \text{since pvalue is greater than } 0.05. \text{ Hence we accept that } H_0 \text{ at } 1\% \text{ level of significance.}$

PA

Questions (Prac 6)

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Let the population mean (amount spent per customer in a restaurant) is 250. A sample of 100 customer is selected. The sample mean is calculated as 275 and S.D is 30. Test the hypothesis that population is 250 or not at 5% level of significance.

- In a random sample of 1000 student, it is found that 750 use blue pen. Test the hypothesis that population proportion is 0.8 at 1% of significance.
- 2 random sample of size 1000 + 2000 are drawn from 2 population with the same S.D = 2.5. The sample means are 67.5 + 68 respectively. Test the hypothesis at 5% level of significance.
- A study of noise level of 2 hospitals is given below. Test the claim that the 2 hospitals have same level of noise at 1% level of significance.

	Hospital A	Hospital B
size	34	34
Mean	61.2	59.4
S.D	7.9	7.5

- In a sample of 500 students in a college, 400 use blue ink in another college from a sample of 900, 450 use blue ink. Test the hypothesis that the proportion of students using blue ink using 2 colleges are equal or not at 1% level of significance.

5) $H_0: P_1 = P_2$ against, $H_1: P_1 \neq P_2$
 $n_1 = 600; n_2 = 900; P_1 = 400/600; P_2 = 450/900$
 $P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$

$$q = 1 - P$$

 $Z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$
cat ("calculated value is", Z_{cal})

Calculate value is 6.381534.

$$P_1 = 0.666667$$

$$P_{\text{val}} = 2 * (1 - pnorm(\text{abs}(Z_{\text{cal}})))$$

$$P_{\text{val}} = 1.753222e-10$$

cat ("since, pvalue is less than 0.05. Hence we reject the H_0 at 1% level of significance.")
since, pvalue is less than 0.05. Hence we reject
 H_0 at 1% level of significance.

6) for sample size, $n_1 = 200, n_2 = 200, P_1 = 44/200, P_2 = 30/200$
Test at 5% level of significance.

$$\rightarrow n_1 = 200; n_2 = 200; P_1 = 44/200; P_2 = 30/200$$

 $P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$
 P

$$P = 0.4185$$

$$q = 1 - P$$

$$q = 0.5815$$

$$P_{\text{val}} = 0.315$$

```
> zcal =  $(p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$ 
> zcal ("calculated value is ", zcal)
> calculated value is 1.802741
> pval = 2 * (1 - pnorm (abs(zcal)))
> pval
> 0.07142888
C1) since, pvalue is greater than 0.05 (hence we accept
> at 5% level of significance!)
H0 at 5% level of significance!
H1 since pvalue is greater than 0.05 (hence we accept
H0 at 5% level of significance.)
```

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PRATICAL - 7

Aim: Small sample size

- 1) The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from the population with the average 66. $H_0: \mu = 66$.
Since p-value is less than 0.05 we reject the hypothesis $H_0: \mu = 66$ at 5% level of significance.

code :-

```
> x = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)
```

```
> t.test(x)
```

One sample t-test.

data: x

t = 68.319, df = 9, p-value = 1.558e-17

alternative hypothesis: true mean is not equal to 66. 95 percent confidence interval:

65.65171 70.14829

sample estimates:

mean of x

67.9

Two groups of students score the following marks test the hypothesis that there is no significant difference between the two group.

Group 1: 18, 22, 21, 17, 20, 17, 23, 20, 22, 21
 Group 2: 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H_0 : There is no difference between the two group.

c (18, 22, 21, 17, 20, 17, 23, 20, 22, 21)

x: c (16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

t-test (u, 4)

welch Two Sample t-test

data: x and y

$t = 2.2573$, $df = 16.376$, P-value = 0.03798

alternative hypothesis: true difference in means is not equal to 0

95 per cent confidence interval:

0.1628205 5.0371795

sample estimates:

mean of x mean of y

20.175 17.5

pvalue = 0.0378

$\{ \text{if } (\text{Pvalue} > 0.05) \& \text{cat}(\text{"accept } H_0\text{"}) \} \text{ else cat}(\text{"reject } H_0\text{"}) \}$

Ans: Since p-value is less than 0.05

we reject the hypothesis at 5% level of significance.

Q3:

Q3

Sale data of 6 shop before and after special campaign given below:

Before: 53, 28, 31, 48, 50, 42

After: 58, 29, 30, 55, 56, 45

Test the hypothesis the campaign is effective or not.

H₀: There is no significant difference of sales before and after the campaign

$\bar{x} = \text{c}(53, 28, 31, 48, 50, 42)$

$\bar{y} = \text{c}(58, 29, 30, 55, 56, 45)$

statistic (x, y, paired = T, alternative = "greater")

paired t-test.

data: x and y

t = -2.7815, df = 5 p-value = 0.9806

alternative hypothesis : true difference in means greater than 0.

-6.035547 Inf

sample estimate:

mean of the differences

-3.5

pvalue = 0.9806

if (pvalue > 0.05) { cat("Accept H₀") } else { cat("Reject") }

Accept: H₀

Two medicines are applied to 2 group of patient

Group1: 10, 12, 13, 11, 14

Group2: 8, 9, 12, 14, 15, 10, 9

is there any significance between two groups

c(10, 12, 13, 11, 14)
 a) c(13, 9, 12, 14, 15, 10, 9)
 b) t-test
 select two sample t-test
 a and b

data
 0.65591 df = 9.567 , pvalue = 0.527
 f:

alternatives hypothesis: true difference in mean is
 not equal to 0 as per cent confidence interval

: 1.954382 3.534382

sample estimates

mean of x, mean of y

11.8 11.0,

> pvalue = 0.5273

> if (pvalue > 0.05) { cat("Accept H₀") } else
 & cat("Reject H₁") }

∴ We Accept H₀.

Q5) H_0 : There is no significant difference between before and after

$\geq A = c(120, 125, 115, 130, 123, 119)$

$\geq B = c(100, 114, 95, 90, 115, 99)$

t . test (A, B, paired = T, alternative = "less")

paired t-test

data: A and B

$t = 4.345$, $df = 5$, pvalue = 0.9963

alternative hypothesis : True difference in mean is less than 0.95 percent confidence interval:

Inf: 29.0295

sample estimates:

19.83333

\geq pvalue : 0.9963

\geq if (pvalue > 0.05) 2 cat = ("Accept H₀") else,

{ cat ("Reject H₀") }

Accept H₀.

AM

PRACTICAL - 8.

73

$$H_0: \mu = 55$$

$$H_1: \mu \neq 55$$

$$> n = 100$$

$$> mx = 52$$

$$> mo = 65$$

$$> sd = 7$$

$$> z_{\text{cal}} = (mx - mo) / (sd / \sqrt{n})$$

$$(1) - 4.285714$$

$$> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> 1.82153e-05$$

since the pvalue is less than 0.5 $\therefore H_0: \mu = 55$ at 5% level of significance is rejected.

$$(2) H_0: p = \frac{1}{2} = ?$$

$$\> p = 0.5$$

$$\> Q = 1 - p$$

$$\> P = 350/700$$

$$\> n = 700$$

$$\> z_{\text{cal}} = (p - Q) / \sqrt{(P + Q/n)}$$

$$\> z_{\text{cal}}$$

$$(1) 0$$

Q3:

```
> pralue = 2 * (1 - pnorm( abs(zcal) ))  
> pralue  
[1] 1
```

Accept the pralue at $H_0: \mu = 1/2$

Q3:

```
> n1 = 1000  
> n2 = 1500  
> p1 = 0.02  
> p2 = 0.01  
> p = (n1 * p1 + n2 * p2) / (n1 + n2)  
> Q = 1 - p  
> zcal = (p1 - p2) / sqrt(p * Q * (1/n1 + 1/n2))  
> zcal  
[1] 2.084842  
> Pralue = 2 * (1 - pnorm( abs(zcal) ))  
> pralue  
[1] 0.03708364.
```

since the pralue is less than 0.05 \therefore we reject the pralue at 5% level of significance.

$$H_0: \mu = 100$$

$$m_x = 99 \quad s_d = 8$$

$$m_o = 100 \quad n = 400$$

$$z_{\text{ref}} = (m_x - m_o) / (s_d / (\sqrt{n}))$$

$$z_{\text{cal}}$$

$$C1] -2.5$$

$$\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$p\text{value}$$

$$C1] 0.01241933$$

we reject the value at 5% level of significance.

$$3) x = c(63, 63, 68, 69, 71, 71, 72)$$

t-test(x)

One sample t-test

data: x

f = 47.94, df = 6, p-value = 5.522e-09.

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

64.66479, 71.62092

sample estimates:

mean of x

68.14286

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R code:

7) $H_0: \mu = 100$

$\bar{x}_{mx} = 1150$

$\bar{x}_{mo} = 1200$

$s_{sd} = 125$

$n = 100$

$z_{cal} = (\bar{x}_{mx} - \bar{x}_{mo}) / (s_{sd} / \sqrt{n})$

$|z_{cal}|$

(1)-4

$p\text{-value} = 2 * (1 - \text{pnorm}(|z_{cal}|))$

$p\text{-value}$

$6.334248e-05$

we reject the value at 5% level of significance

6) $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

$y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

$\text{var.test}(x, y)$

f test to compare two variances

data: x and y

f = 0.70686, num df = 8, denom df = 10, p-value: 0.635

alternative hypothesis: true ratio of variances is not equal to 1

95 percent confidence interval:

0.1833662 3.036093

Sample estimates:

ratio of variances

0.7068567

we accept

$$\text{Q) } n_1 = 200$$

$$n_2 = 300$$

$$p_1 = 44/200$$

$$p_2 = 56/300$$

$$\rightarrow P = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$Q = 1 - P$$

$$z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * Q * (1/n_1 + 1/n_2)}$$

$$(1) 0.9128709$$

$$\text{pvalue} = 1 - \text{pnorm}(\text{abs}(z))$$

pvalue

$$0.17 \quad 0.3613104$$

P

0.2

we accept the value at 5% level of significance.

~~reject H₀~~ 1. P
1. 0.3613104

PRACTICAL - 9

AIM: Chi square test of ANOVA
(Analysis of variance)

- D) Use the following data to test whether the condition of the home and child are independent or not.

Condition of Home

	Clean	Dirty
Clean	70	50
Fairly clean	80	20
Dirty	35	45

H₀: Condition of home and child are independent.

> x = c(70, 80, 35, 50, 20, 45).

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

	C, 1]	C, 2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

> Pv = chisq.test(y)

> Pv

Pearson's Chi-squared test

data:
 $\chi^2 = 25.646$, $df = 2$, p-value = $2.698e-06$ 76
p-value is less than 0.05
∴ we reject H_0

Test the hypothesis that vaccines and disease are independent or not?

Vaccines

	Affected	Not Affected
Affected	70	46
Not Affected	35	37

H_0 : vaccines and disease are independent.

$x = \begin{pmatrix} 70 & 35 \\ 46 & 37 \end{pmatrix}$

$m = 2$

$n = 2$

$y = \text{matrix}(x, nrow = m, ncol = n)$

$y =$

$\begin{bmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{bmatrix}$

$[1,1] = 70$

$[1,2] = 46$

$[2,1] = 35$

$[2,2] = 37$

$\text{pr} = \text{chisq.test}(y)$

$\text{pr} =$

Pearson's chi-squared test with Yates' continuity correction

data: y

$\chi^2 = 2.0275$, $df = 1$, p-value = 0.1545

p-value is greater than 0.05

∴ we accept H_0 .

Q3] Perform ANOVA for following data

Type	Observation
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

→ H_0 : The mean are equal for A, B, C, D

$$\rightarrow x_1 = c(50, 52)$$

$$\rightarrow x_2 = c(53, 55, 53)$$

$$\rightarrow x_3 = c(60, 58, 57, 56)$$

$$\rightarrow x_4 = c(52, 54, 54, 55)$$

d = stack (list (b1 = x1, b2 = x2, b3 = x3, b4 = x4))

names(d)

c1] "values" "ind"

one way. test (values ~ ind, data = d, var.equal = T)
One-way analysis of means.

data: values and ind

F = 11.735, num df = 3, denom df = 9, Pr(> F) = 0.001

anova = aov(values ~ ind, data = d)

summary(anova)

	df	sum sq	mean sq	F value	Pr(> F)
ind	3	71.06	23.688	11.73	0.001
residual	9	18.17	2.019		

signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1

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The following data of 4 brands gives the life of the tyre.

Type

A

Life

20, 23, 17, 18, 22, 24

B

19, 15, 17, 20, 16, 19

C

21, 19, 22, 17, 20

D

15, 14, 16.

H0 : The average life A, B, C and D are equal.

$x_1 = c(20, 23, 18, 17, 18, 22, 24)$

$x_2 = c(B)$

$x_3 = C(C)$

$x_4 = C(D)$

$d = stack(list(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$
 $\text{names}(d)$

CY value "ind"

$\text{one way. test}(\text{value} = \text{ind}, \text{data} = d, \text{var.equal} = \text{T})$

One-way analysis of means.

data: values find

f = 6.8445, num df = 3, denom df = 20

P-value = 6.002349.

\therefore P-value is less than 0.05 we reject the hypothesis.

anova = aov(values ~ ind, data = d)

summary(anova)

	Df	sumsq	meansq	fvalue	Pr(>f)
ind	3	91.49	30.479	6.845	6.002349
Residuals	20	89.06	4.453		

Signif codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 , . 0.1 , 1

> $x = \text{read.csv("C:/users/adm1/Desktop/markss.csv")}$

> x

	stats	maths
1	40	60
2	45	48
3	42	47
4	15	20
5	37	25
6	36	27
7	49	52
8	59	58
9	20	25
10	27	27

> $Am = \text{mean}(x\$stats)$

(1) 37

> $Am1 = \text{mean}(x\$maths)$

(1) Am1

(1) 39.4

> $m1 = \text{median}(x\$stats)$

(1) m1

(1) 38.5

> $m_1 = \text{median}(x\$maths)$

(1) m1

> $n = \text{length}(x\$stats)$

(1) n

(1) 10

> $s_d = \sqrt{(n-1) * \text{var}(x \$ \text{stats}) / n}$

78

> $s_d = 12.64911$

C1) $\text{length}(x \$ \text{maths})$

> n

C1) $10 = \sqrt{(n-1) * \text{var}(x \$ \text{maths}) / n}$

> s_d

C1) 15.2

> $\text{cor}(x \$ \text{stats}, x \$ \text{maths})$

C1) 0.830618

AM

PRATICAL - 10

80

Aim: Non parametric test.

following are the amounts of sulphur oxide emitted by industries in 20 days. Apply sign test. to test the hypothesis that the population median is 21.5 at 5% LOS.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20
17, 6, 24, 14, 15, 23, 24, 26.

H₀: Population median is 21.5

$$\rightarrow x = c(17, 15, 20, \dots, 24, 26, 26)$$

$$\rightarrow m_e = 21.5$$

$$\rightarrow SP = \text{length}(x > m_e)$$

$$\rightarrow SP$$

$$(1) 9$$

$$\rightarrow S_n = \text{length}(x < m_e)$$

$$\rightarrow S_n$$

$$(1) 11$$

$$\rightarrow n = SP + S_n$$

$$\rightarrow n$$

$$(1) 20$$

$$\rightarrow P_V = \text{fbinom}(SP, n, 0.5)$$

$$\rightarrow P_V$$

$$(1) 0.419015$$

∴ If P_r is less than 0.05 we accept H_0 at 5% level of significance.

If $H_1: m_e \neq$

or $m_e <$

then, $P_r = P\text{binom}(sp, n, 0.5)$

If $H_1: m_e >$ then,

$P_r = P\text{binom} > C_{sn}, n, 0.5$

Q2) following is the data of 10 observations, apply sign test. The population median is 625. The alternative H_1 is more than 625.

612, 619, 631, 628, 643, 640, 655, 649,
670, 663

$\rightarrow H_0: \text{Population median is } 625$

$H_1: m_e > 625$

$x = c(612, 619, 631, 628, 643, 640, 655, 649,$
 $670, 663)$

$\rightarrow m_e = \cancel{625}$

$\rightarrow sp = \text{length}(x > m_e)$

$ssp = \text{length}(x < m_e)$

(1) ~~n~~ $n = sp + ssp$

$\rightarrow n$

(1) 10

Pr vs binom ($n=10, \alpha=0.5$)
 } Pr
 } 0.9292578

(i) Pr vs binom ($n=10, \alpha=0.5$)

Pr 0.0546875

(ii) As Pr is greater than 0.05 we accept H_0 at 5% level of significance

(iii) Following are the data of samples. Test the hypothesis that the population median is 60 against the alternatives i.e. more than 60 at 5% level of significance using wilcoxon signed rank test

63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 37, 69

$H_0: \text{me} = 60$ against $H_1: \text{me} > 60$

$\Sigma x = 63 + 65 + 60 + 89 + \dots + 69$

wilcoxon test ("alter = "greater", $\mu = 60$)

wilcoxon signed rank test with continuity correction data: x

p: 0.02298

alternative hypothesis: true location is greater than 60.
 p-value is less than 0.05 we reject H_0 at 5% level of significance

Note:- If $\text{H}_1: \text{me} < \text{alter}$ = "less"

$\text{H}_1: \text{me} < \text{alter}$ = "two-sided".

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- Q4) Using wsr test. The population median or less than 12.

$15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26$

Soln: $H_0: \text{me} = 12$ against $H_1: \text{me} < 12$.

$\sum x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26)$

$\rightarrow \text{wilcox.test}(x, \text{alter} = \text{"less"}, \text{mu} = 12)$

data: x

V = 66, p-value = 0.9986.

alternative hypothesis : true location is less than 12
 \therefore pvalue is greater than 0.05 we accept H_0 .

- Q5) The weights of students before and after they stopped smoking are given below. Using wsr test that there is no significant change.

Before

65

75

75

62

72

After

72

74

72

66

73

- Soln: $H_0:$ Before and after there is no change against $H_1:$ There is change.

$\sum x = c(65, 75, 75, 62, 72)$

$\sum y = c(72, 74, 72, 66, 73)$

$\sum d = n - y$

$\rightarrow \text{wilcox.test}(d, \text{alter} = \text{"two-sided"}, \text{mu} = 0)$

data is d

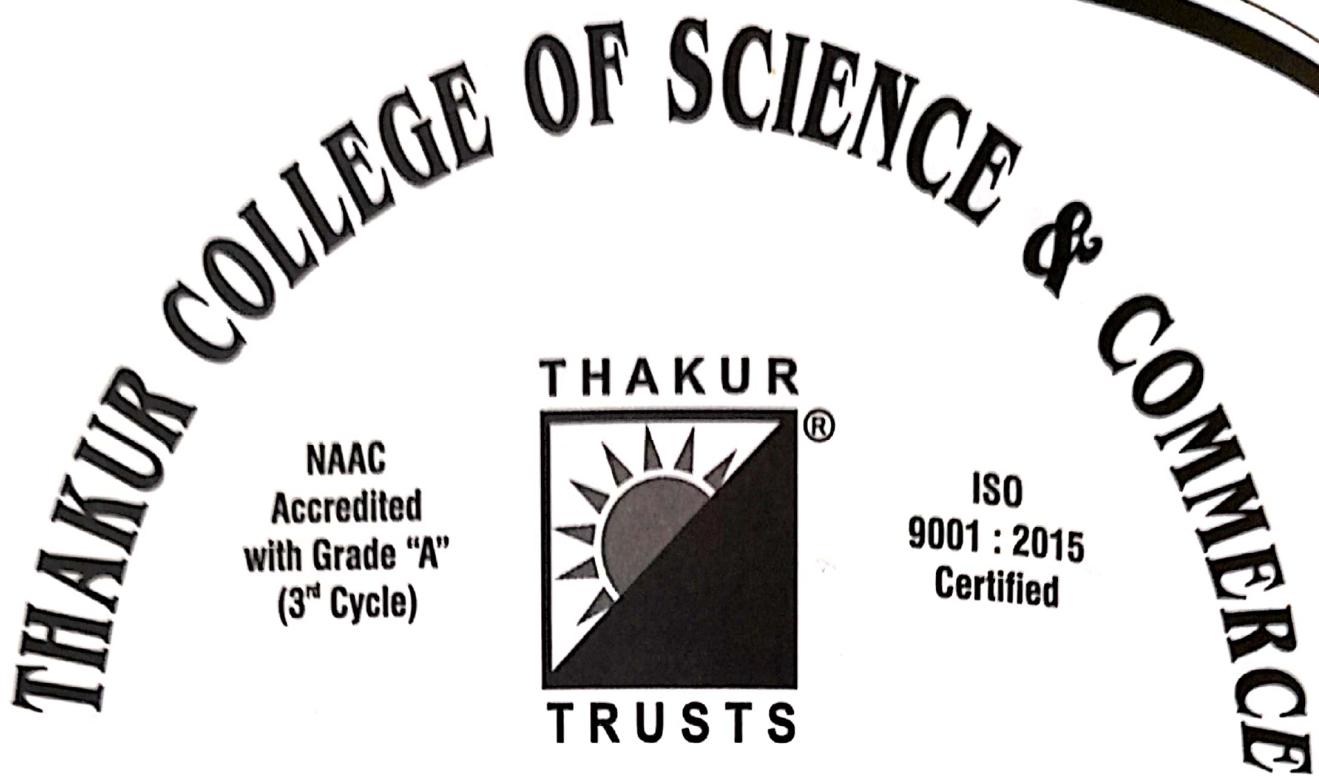
v = 4.5, P-value = 0.4982

alternative hypothesis: true location is not equal to 0.

P-value is greater than 0.05 therefore we accept H_0 .

Ans
27-02

★ ★ INDEX ★ ★



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