



**DECISION TREE
PARAMETER**



**MIN IMPURITY
DECREASE**



ตารางข้อมูล

Age	Income	Student	<u>Credit_Rating</u>	<u>Buys_Computer</u>
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no





กำหนด
MIN IMPURITY
DECREASE

=

0.1



การคำนวณค่า GINI

① Class P : buy_computer = "yes" = 9
Class N : buy_computer = "No" = 5

$$\text{gini (buy_computer)} = 1 - \left[\left(\frac{9}{14} \right)^2 + \left(\frac{5}{14} \right)^2 \right] = 0.459$$

② age $\leq 30 \rightarrow$ "yes" = 2 , "No" = 3

$$\text{gini}(\leq 30) = 1 - \left[\left(\frac{2}{5} \right)^2 + \left(\frac{3}{5} \right)^2 \right] = 0.48$$

age 31...40 \rightarrow "yes" = 4 , "No" = 0

$$\text{gini}(31...40) = 1 - \left[\left(\frac{4}{4} \right)^2 + \left(\frac{0}{4} \right)^2 \right] = 0$$

age $> 40 \rightarrow$ "yes" = 3 , "No" = 2

$$\text{gini}(> 40) = 1 - \left[\left(\frac{3}{5} \right)^2 + \left(\frac{2}{5} \right)^2 \right] = 0.48$$

$$\therefore \text{Gini (Avg weight Age)} = \left(0.48 \times \frac{5}{14} \right) + \left(0 \times \frac{4}{14} \right) + \left(0.48 \times \frac{5}{14} \right) = 0.343$$

③ income = high \rightarrow "yes" = 2 , "No" = 2

$$\text{gini (high)} = 1 - \left[\left(\frac{2}{4} \right)^2 + \left(\frac{2}{4} \right)^2 \right] = 0.5$$

income = medium \rightarrow "yes" = 4 , "No" = 2

$$\text{gini (medium)} = 1 - \left[\left(\frac{4}{6} \right)^2 + \left(\frac{2}{6} \right)^2 \right] = 0.44$$

income = low \rightarrow "yes" = 3 , "No" = 1

$$\text{gini (low)} = 1 - \left[\left(\frac{3}{4} \right)^2 + \left(\frac{1}{4} \right)^2 \right] = 0.375$$

$$\therefore \text{Gini (Avg weight income)} = \left(0.5 \times \frac{4}{14} \right) + \left(0.44 \times \frac{6}{14} \right) + \left(0.375 \times \frac{4}{14} \right) = 0.440$$

④

① Class P : buy_computer = "yes" = 9
Class N : buy_computer = "No" = 5

$$\text{gini (buy_computer)} = 1 - \left[\left(\frac{9}{14} \right)^2 + \left(\frac{5}{14} \right)^2 \right] = 0.459$$

② age $\leq 30 \rightarrow$ "yes" = 2 , "No" = 3

$$\text{gini}(\leq 30) = 1 - \left[\left(\frac{2}{5} \right)^2 + \left(\frac{3}{5} \right)^2 \right] = 0.48$$

age 31...40 \rightarrow "yes" = 4 , "No" = 0

$$\text{gini}(31...40) = 1 - \left[\left(\frac{4}{4} \right)^2 + \left(\frac{0}{4} \right)^2 \right] = 0$$

⑤ age $> 40 \rightarrow$ "yes" = 3 , "No" = 2

$$\text{gini}(> 40) = 1 - \left[\left(\frac{3}{5} \right)^2 + \left(\frac{2}{5} \right)^2 \right] = 0.48$$

$$\therefore \text{Gini (Avg weight Age)} = \left(0.48 \times \frac{5}{14} \right) + \left(0 \times \frac{4}{14} \right) + \left(0.48 \times \frac{5}{14} \right) = 0.343$$

\therefore

③ income = high \rightarrow "yes" = 2 , "No" = 2

$$\text{gini (high)} = 1 - \left[\left(\frac{2}{4} \right)^2 + \left(\frac{2}{4} \right)^2 \right] = 0.5$$

income = medium \rightarrow "yes" = 4 , "No" = 2

$$\text{gini (medium)} = 1 - \left[\left(\frac{4}{6} \right)^2 + \left(\frac{2}{6} \right)^2 \right] = 0.44$$

income = low \rightarrow "yes" = 3 , "No" = 1

$$\text{gini (low)} = 1 - \left[\left(\frac{3}{4} \right)^2 + \left(\frac{1}{4} \right)^2 \right] = 0.375$$

$$\therefore \text{Gini (Avg weight income)} = \left(0.5 \times \frac{4}{14} \right) + \left(0.44 \times \frac{6}{14} \right) + \left(0.375 \times \frac{4}{14} \right) = 0.440$$

AGE ≤ 30 , N=5

on age (≤ 30), n=5

income - high = "yes" = 0, "No" = 2

$$gini = 1 - \left[\left(\frac{0}{2} \right)^2 + \left(\frac{2}{2} \right)^2 \right] = 0$$

- medium = "yes" = 1, "No" = 1

$$gini = 1 - \left[\left(\frac{1}{2} \right)^2 + \left(\frac{1}{2} \right)^2 \right] = 0.5$$

- low = "yes" = 1, "No" = 0

$$gini = 1 - \left[\left(\frac{1}{1} \right)^2 + \left(\frac{0}{1} \right)^2 \right] = 0$$

$$\therefore Gini(Avg \text{ weight income}) = \left[\left(0 \times \frac{2}{5} \right) + \left(0.5 \times \frac{2}{5} \right) + \left(0 \times \frac{1}{5} \right) \right]$$

$$= 0.2 \quad \times$$

student - student_yes = "yes" = 2, "No" = 0

$$gini = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

- student_no = "yes" = 0, "No" = 3

$$gini = 1 - \left[\left(\frac{0}{3} \right)^2 + \left(\frac{3}{3} \right)^2 \right] = 0$$

$$\therefore Gini(Avg \text{ weight student}) = \left[\left(0 \times \frac{2}{5} \right) + \left(0 \times \frac{3}{5} \right) \right]$$

$$= 0 \quad \times$$

credit_rating - fair = "yes" = 1, "No" = 2

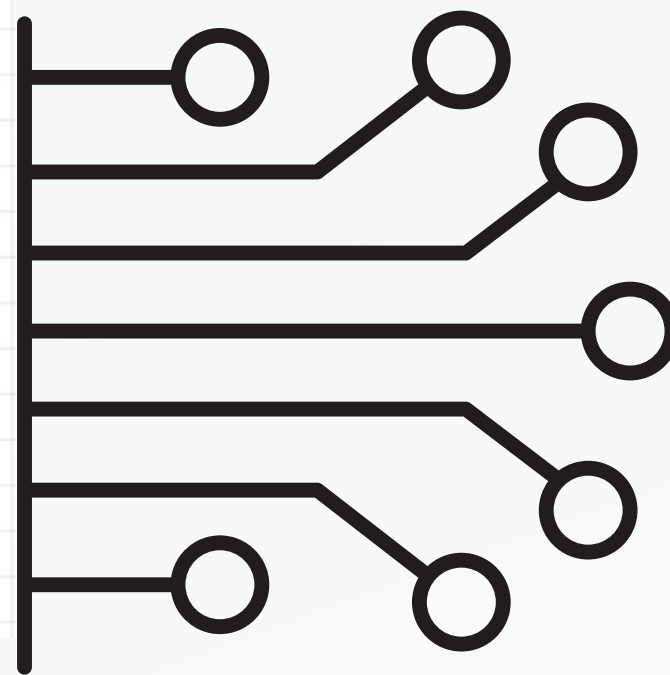
$$gini = 1 - \left[\left(\frac{1}{3} \right)^2 + \left(\frac{2}{3} \right)^2 \right] = 0.4$$

- excellent = "yes" = 1, "No" = 1

$$gini = 1 - \left[\left(\frac{1}{2} \right)^2 + \left(\frac{1}{2} \right)^2 \right] = 0.5$$

$$\therefore Gini(Avg \text{ weight credit_rating}) = \left[\left(0.4 \times \frac{3}{5} \right) + \left(0.5 \times \frac{2}{5} \right) \right]$$

$$= 0.464$$



AGE = 31..40, N=4

age (31-40) $n=4$

income - high = "yes" = 2, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

- medium = "yes" = 1, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{1}{1} \right)^2 + \left(\frac{0}{1} \right)^2 \right] = 0$$

- low = "yes" = 1, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{1}{1} \right)^2 + \left(\frac{0}{1} \right)^2 \right] = 0$$

$$\therefore \text{Gini(Avg weight income)} = \left[\left(0 \times \frac{2}{4} \right) + \left(0 \times \frac{1}{4} \right) + \left(0 \times \frac{1}{4} \right) \right] \\ = 0 \quad \text{✗}$$

student - Student_yes = "yes" = 2, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

- Student_no = "yes" = 2, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

$$\therefore \text{Gini(Avg weight student)} = \left[\left(0 \times \frac{2}{4} \right) + \left(0 \times \frac{2}{4} \right) \right] \\ = 0 \quad \text{✗}$$

Credit_rating - fair = "yes" = 2, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

- excellent = "yes" = 2, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{2}{2} \right)^2 + \left(\frac{0}{2} \right)^2 \right] = 0$$

$$\therefore \text{Gini(Avg weight credit_rating)} = \left[\left(0 \times \frac{2}{4} \right) + \left(0 \times \frac{2}{4} \right) \right] \\ = 0 \quad \text{✗}$$

AGE > 40, N=5

for age > 40, n = 5

income - high = "yes" = 0, "No" = 0

$$\text{gini} = 1 - [0 + 0] = 0$$

- medium = "yes" = 2, "No" = 1

$$\text{gini} = 1 - \left[\left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)^2 \right] = 0.44$$

- low = "yes" = 1, "No" = 1

$$\text{gini} = 1 - \left[\left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2 \right] = 0.5$$

$$\therefore \text{Gini(Avg weight income)} = \left[\left(0 \times \frac{0}{5}\right) + \left(0.44 \times \frac{3}{5}\right) + \left(0.5 \times \frac{2}{5}\right) \right]$$

$$= 0.464$$

student - student_yes = "yes" = 2, "No" = 1

$$\text{gini} = 1 - \left[\left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)^2 \right] = 0.44$$

- student_no = "yes" = 1, "No" = 1

$$\text{gini} = 1 - \left[\left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2 \right] = 0.5$$

$$\therefore \text{Gini(Avg weight student)} = \left[\left(0.44 \times \frac{3}{5}\right) + \left(0.5 \times \frac{2}{5}\right) \right]$$

$$= 0.464$$

credit_rating - fair = "yes" = 3, "No" = 0

$$\text{gini} = 1 - \left[\left(\frac{3}{3}\right)^2 + \left(\frac{0}{3}\right)^2 \right] = 0$$

- excellent = "yes" = 0, "No" = 2

$$\text{gini} = 1 - \left[\left(\frac{0}{2}\right)^2 + \left(\frac{2}{2}\right)^2 \right] = 0$$

$$\therefore \text{Gini(Avg weight credit_rating)} = \left[\left(0 \times \frac{3}{5}\right) + \left(0 \times \frac{2}{5}\right) \right]$$

$$= 0$$

กำหนดให้ค่า MIN_IMPURITY_DECREASE = 0.1

ค่า min_impurity_decrease

กำหนดให้ min_impurity_decrease = 0.1

จากสูตร

The weighted impurity decrease equation is the following:

$$N_t / N * (impurity - N_{t_R} / N_t * right_impurity - N_{t_L} / N_t * left_impurity)$$

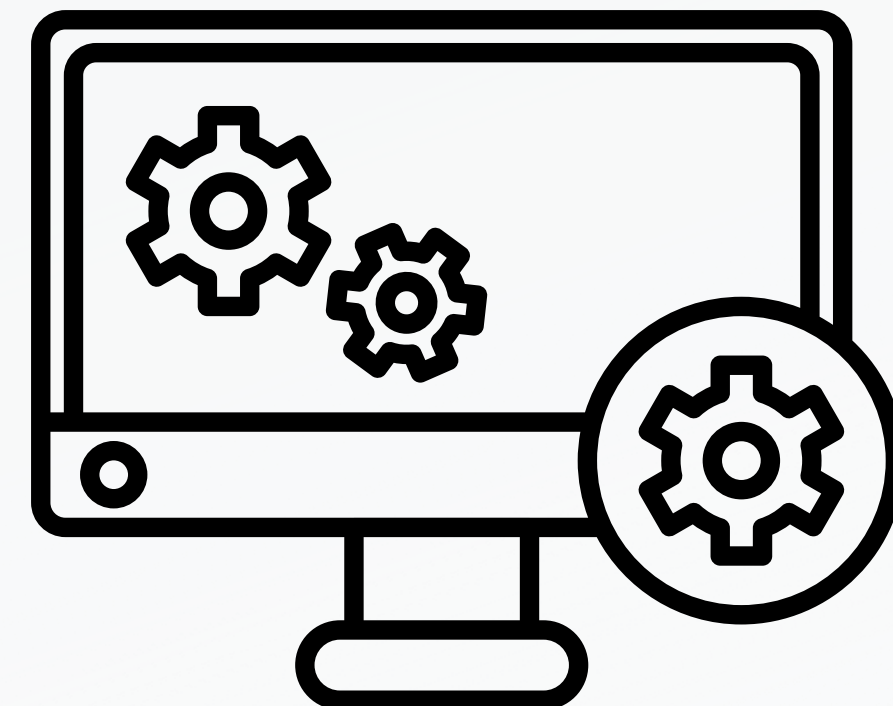
where N is the total number of samples, N_t is the number of samples at the current node, N_{t_L} is the number of samples in the left child, and N_{t_R} is the number of samples in the right child.

จะได้ Age $\rightarrow \frac{14}{14} \times (0.459 - \frac{5}{14}(0.48) - 0 - \frac{5}{14}(0.48))$
 $= 0.117$ ซึ่ง ≥ 0.1 จึงมีการแยก Node ต่อไป ✖

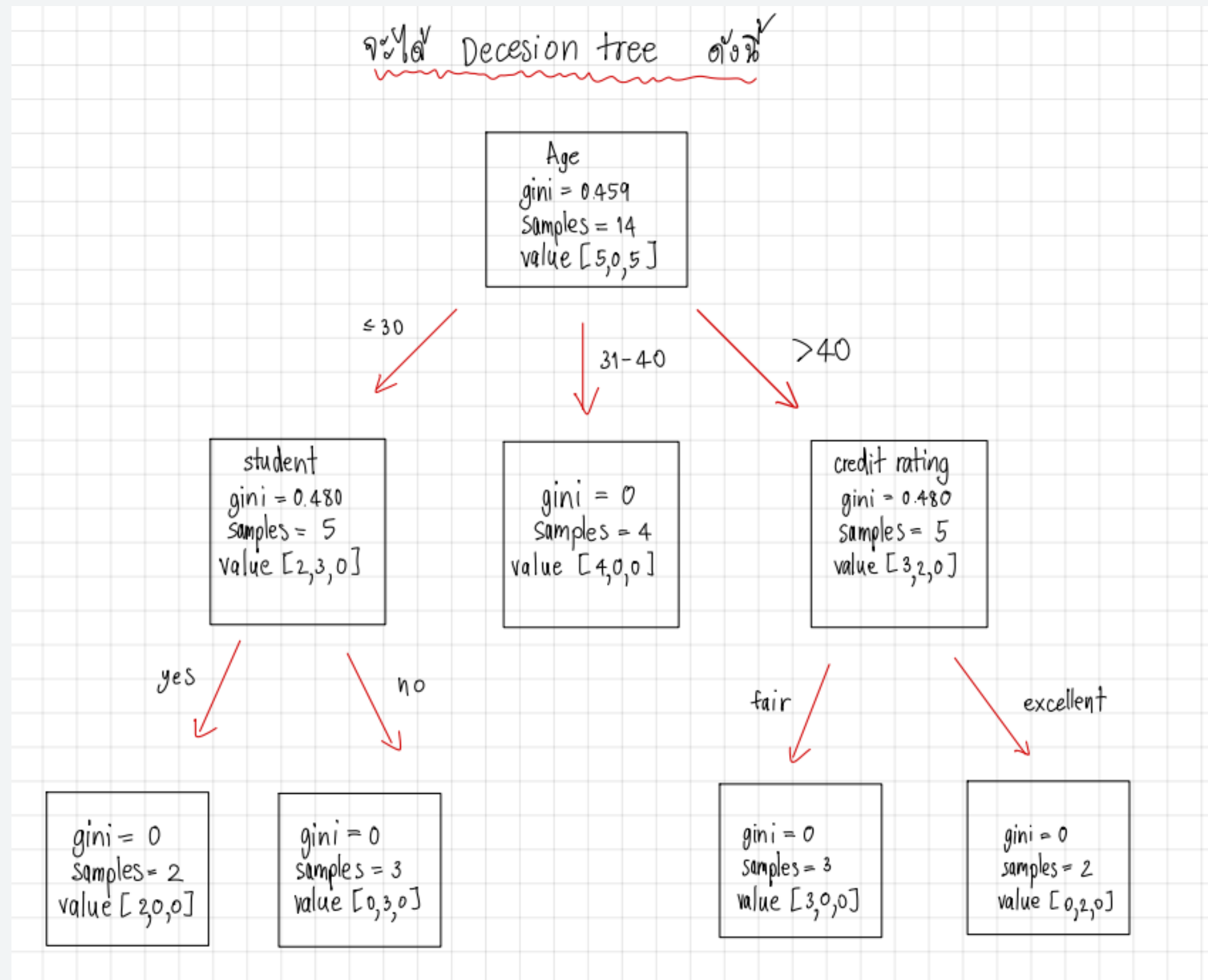
income $\rightarrow \frac{14}{14} \times (0.459 - \frac{4}{14}(0.5) - \frac{6}{14}(0.44) - \frac{4}{14}(0.375))$
 $= 0.020$ ซึ่ง < 0.1 จึงไม่มีการแยก Node ✖

student $\rightarrow \frac{14}{14} \times (0.459 - \frac{7}{14}(0.245) - \frac{7}{14}(0.489))$
 $= 0.092$ ซึ่ง < 0.1 จึงไม่มีการแยก Node ✖

credit_rating $\rightarrow \frac{14}{14} \times (\frac{6}{14} \times (0.375) - \frac{6}{14}(0.5))$
 $= 0$ ซึ่ง < 0.1 จึงไม่มีการแยก Node ✖



DECISION TREE



- เนื่องจากใน $\text{age} < 30$ student มีค่า gini = 0 ซึ่งมีค่าน้อยที่สุด จึงไม่มีการแยก Node ต่อ
- เนื่องจากใน $\text{age } 31-40$ income, student และ credit_rating มีค่าเป็น 0 ดังนั้นจึงไม่มีการแยก Node ต่อ
- เนื่องจากใน $\text{age} > 40$ credit rating มีค่า gini = 0 ซึ่งมีค่าน้อยที่สุด จึงไม่มีการแยก Node ต่อ

สรุป

- จากข้อมูล การซื้อคอมพิวเตอร์ (buy computer) ที่มีตัวอย่าง คือ 14 คน
- โดยที่ - ในอายุ น้อยกว่า 30 จะมีนักเรียนซื้อคอมพิวเตอร์ 2 คน และคนที่ไม่ใช่ นักเรียน จะไม่ซื้อคอมพิวเตอร์ 3 คน
- ในอายุ 31 ถึง 40 จะซื้อคอมพิวเตอร์ ทุกคน
 - ในอายุ 40 ปีขึ้นไป ผู้ที่มี credit rating ในระดับ fair จะซื้อคอมพิวเตอร์ 3 คน และ ผู้ที่มี credit rating ในระดับ excellent จะไม่ซื้อคอมพิวเตอร์ 2 คน

MEMBER

นางสาวกรวรรณ อุ่จอหอ	643020495-5
นายธนบดี ภูชมศรี	643020502-4
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นางสาวอิงอร พลพา	643021279-6
นางสาวทิพย์วัลย์ สุโพธิ์	643020062-6
นางสาวสุชานาถ พิลาภ	643021276-2

THANK YOU