

The lower bound function computes a best possible bandwidth for a partially determined matrix (with the first  $m$  columns fixed and the first  $m$  or  $m-1$  rows fixed) as the maximum of the following-

- (i) for the fixed portion at top left; count from the diagonal of the fixed portion along the rows and columns to locate the last non-zero element; within the fixed portion ( $m$  by  $m$  or  $m$  by  $m-1$ ) the elements are fixed, while beyond the fixed portion it is assumed that the non-zero elements could be positioned immediately following the fixed columns or rows. Repeat this for each row and column within the fixed portion, taking the maximum count found.
- (ii) for the unfixed portion at bottom right; count the number of elements in each row and column and assume that these could be placed symmetrically about the diagonal - hence bound to bandwidth here is maximum of

both these matrices are  
minimal