

## Outline

- Generative Models Basics
- **Autoregressive Models**
- Autoencoder and Variational Autoencoder
- Generative Adversarial Network
- Diffusion Models

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## Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image  $x$  into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i | x_1, \dots, x_{i-1})$$

$\uparrow$                        $\uparrow$   
 Likelihood of              Probability of  $i$ 'th pixel value  
 image  $x$                       given all previous pixels

Then maximize likelihood of training data

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Slide credit: Fei-Fei Li & Justin Johnson & Serena Yeung

## Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image  $x$  into product of 1-d distributions:

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$\uparrow$                        $\uparrow$   
 Likelihood of              Probability of  $i$ 'th pixel value  
 image  $x$                       given all previous pixels

Will need to define ordering of "previous pixels"

Complex distribution over pixel values => Express using a neural network!

Then maximize likelihood of training data

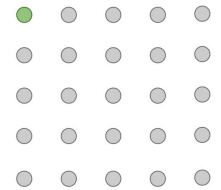
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## PixelRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)



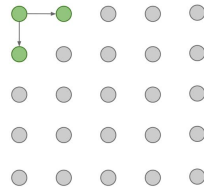
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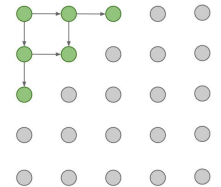
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Generate image pixels starting from corner

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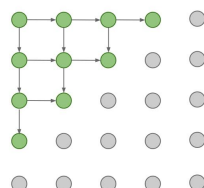
Slide credit: Fei-Fei Li & Justin Johnson & Serena Yeung

## PixelRNN [van der Oord et al. 2016]

Generate image pixels starting from corner

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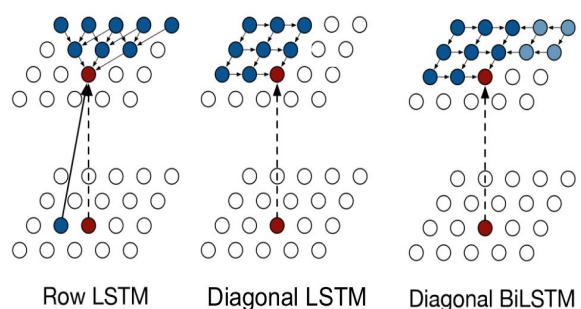
Drawback: sequential generation is slow!



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Slide credit: Fei-Fei Li & Justin Johnson & Serena Yeung

## Variants of Pixel RNN (LSTM)



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Pixel recurrent neural networks, ICML 2016

Slide credit: Yohei Sugawara

## PixelCNN [van der Oord et al. 2016]

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

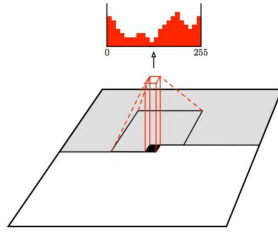


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Slide credit: Fei-Fei Li & Justin Johnson & Serena Yeung

## PixelCNN [van der Oord et al. 2016]

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^n p(x_i | x_1, \dots, x_{i-1})$$

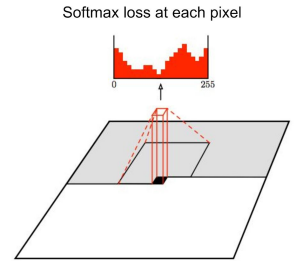


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## PixelCNN [van der Oord et al. 2016]

Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training is faster than PixelRNN  
(can parallelize convolutions since context region values known from training images)

Generation must still proceed sequentially  
=> still slow

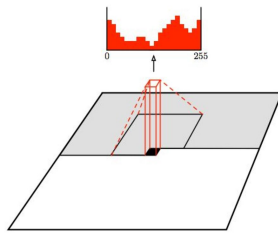


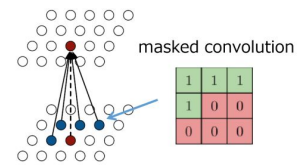
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## PixelCNN

- 2D convolution on previous layer
- Apply masks so a pixel does not see future pixels (in sequential order)

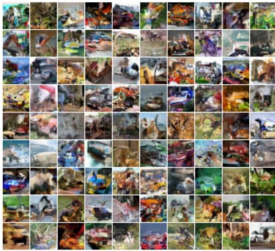


[Pixel recurrent neural networks](#), ICML 2016

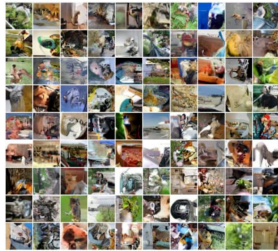
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Slide credit: Yohei Sugawara

## Generation Samples



32x32 CIFAR-10



32x32 ImageNet

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## PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood  $p(x)$
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

- Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

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