

## Lecture 2

### Stacks and Queues



Your Queue

Though you are able to add DVDs to your queue, your account does not currently allow for movies to be shipped to you.

DVD (242) Instant (42) Questions? Visit our FAQ section Show all DVD activity Update DVD Queue

DVD (237)

List Order	Movie Title	Instant	Star Rating	Genre	Expected Availability	Remove
1	Queen Margot	Instant	★★★★★	Fiction	Now	X
2	Time Out	Instant	★★★★★	Fiction	Now	X
3	The Quiet Family	Instant	★★★★★	Fiction	Now	X
4	The Dinner Game	Instant	★★★★★	Fiction	Now	X
5	American Psycho	Instant	★★★★★	Thriller	Now	X
6	Mystic	Instant	★★★★★	Thriller	Now	X
7	Fathering	Instant	★★★★★	Thriller	Now	X
8	Classless	Instant	★★★★★	Comedy	Now	X
9	Red Dragon	Instant	★★★★★	Thriller	Now	X
10	Chimera Lante	Instant	★★★★★	Thriller	Now	X
11	Freezer	Instant	★★★★★	Drama	Now	X

EECS 281: Data Structures & Algorithms

## Measuring Performance

- Several design choices for implementing ADTs
  - Contiguous data (arrays or vectors)
  - Connected data (pointers or linked lists/trees)
- Runtime speed and size of data structure
  - How much time is needed to perform an operation? (count number of steps)
  - How much space is needed to perform an operation? (count size of data and pointers/metadata)
  - How does size/number of inputs affect these results? (constant, linear, exponential, etc.)
- We formalize performance measurements with complexity analysis

4

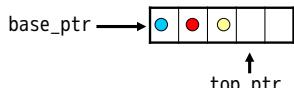
## Choosing a Data Structure for a Given Application

- What to look for
  - The right operations (e.g., add\_elt, remove\_elt)
  - The right behavior (e.g., push\_back, pop\_back)
  - The right trade-offs for runtime complexities
  - Memory overhead
- Potential concern
  - Limiting interface to avoid problems (e.g., no insert\_mid)
- Examples
  - Order tracking at a fast-food drive-through (pipeline)
  - Interrupted phone calls to a receptionist
  - Your TODO list

6

## Stack: Implementation – Array/Vector

Keep a pointer (top\_ptr) just past the last element



Method	Implementation
push(object)	1. If needed, allocate a bigger array and copy data 2. Add new element at top_ptr, increment top_ptr
pop()	Decrement top_ptr
object &top()	Dereference top_ptr - 1
size()	Subtract base_ptr from top_ptr pointer
empty()	Check if base_ptr == top_ptr

How many steps/operations for each method?

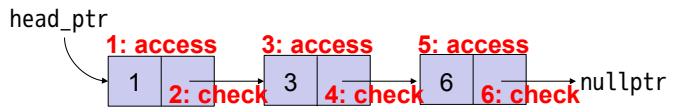
## Data Structures and ADTs

- Need a way to store and organize data in order to facilitate access and modifications
- An **abstract data type (ADT)** combines data with valid operations and their behaviors on stored data
  - e.g., insert, delete, access
  - ADTs define an interface
- A data structure provides a concrete implementation of an ADT

3

## Analysis Example

- How many operations are needed to insert a value at the end of this singly-linked list?



- Can you generalize this for a list with  $n$  elements?

7: Create Node  
8: Insert Value  
9: Update Pointer

$2n + 3$  Linear function is important—coefficients and constants don't matter much

5

## Stack ADT: Interface

- Supports insertion/removal in LIFO order
  - Last In, First Out

Method	Description
push(object)	Add object to top of the stack
pop()	Remove top element
object &top()	Return a reference to top element
size()	Number of elements in stack
empty()	Checks if stack has no elements

### Examples

- Web browser's "back" feature
- Text editor's "Undo" feature
- Function calls in C++



9

## Stack: Implementation – Linked List

Singly-linked is sufficient



Method	Implementation
push(object)	Insert new node at head_ptr, increment size
pop()	Delete node at head_ptr, decrement size
object &top()	Dereference head_ptr
size()	Return size
empty()	Check if size == 0 or head_ptr == nullptr

\*Alternative approach: eliminate size, count nodes each time

How many steps/operations for each method?

Is an array or linked list more efficient for stacks?

10

## Stack: Which Implementation?

Method	Array/Vector	Linked List
push(object)	Constant (linear when resizing vector)*	Constant
pop()	Constant	Constant
object &top()	Constant	Constant
size()	Constant	Constant (with tracked size)
empty()	Constant	Constant

\*Averages out to constant with many pushes (amortized constant)

- The asymptotic complexities of each are similar
- The constant factor attached to the complexity is lower for vector
  - Constant number of operations, but there is "less" to do
  - The linked list must allocate memory for each node individually!
- The linked list also has higher memory overhead
  - i.e. Pointers between nodes as well as the actual data payload

12

## Queue ADT: Interface

- Supports insertion/removal in FIFO order
  - First In, First Out

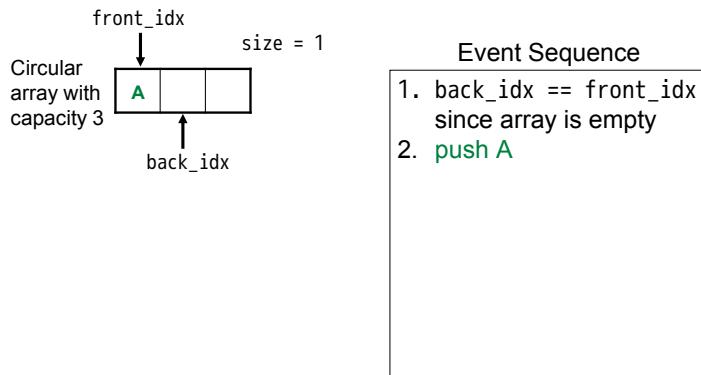
Method	Description
push(object)	Add object to back of queue
pop()	Remove element at front of queue
object &front()	Return reference to element at front of queue
size()	Number of elements in queue
empty()	Checks if queue has no elements

### Examples

- Waiting in line for lunch
- Adding songs to the end of a playlist

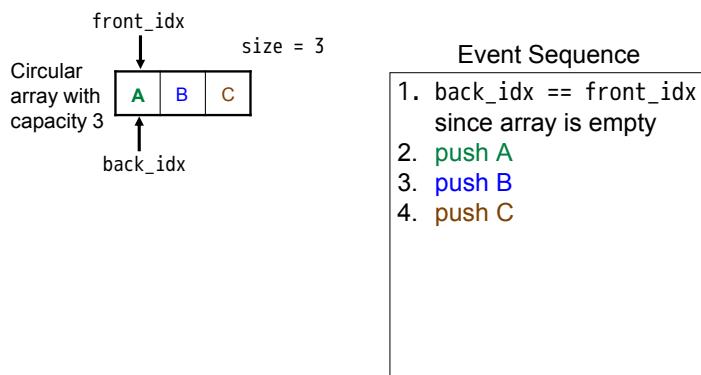
16

## Queue: Implementation – Circular Buffer



18

## Queue: Implementation – Circular Buffer



20

## STL Stacks: std::stack<>

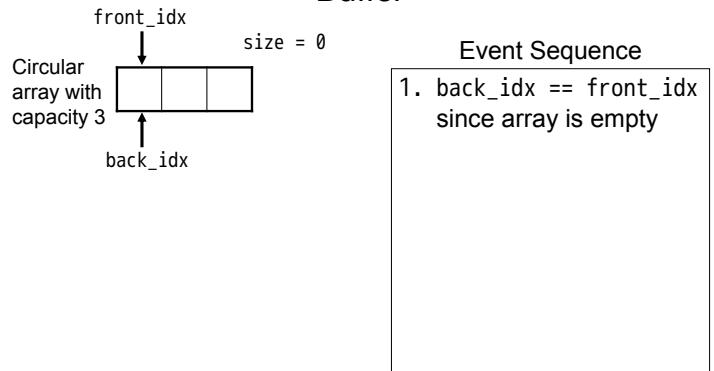
- Code: `#include <stack> Stack<int, std::vector<int> ...`
- You can choose the underlying container
- All operations are implemented generically on top of the given container
  - No specialized code based on given container

	Stack
Default Underlying Container	<code>std::deque&lt;&gt;</code>
Optional Underlying Container	<code>std::list&lt;&gt;†</code> <code>std::vector&lt;&gt;</code>

†`std::list<>` is a doubly-linked list

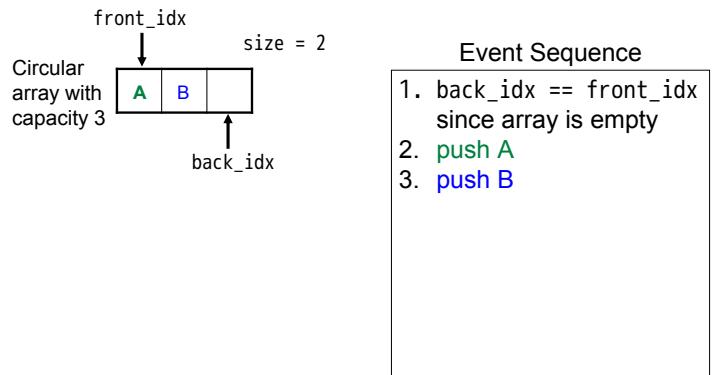
13

## Queue: Implementation – Circular (Ring) Buffer



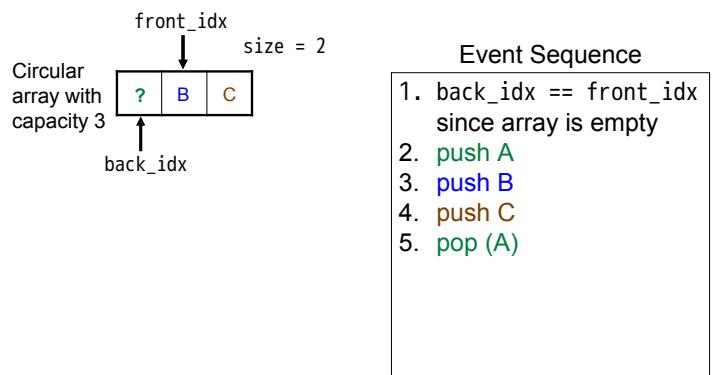
17

## Queue: Implementation – Circular Buffer



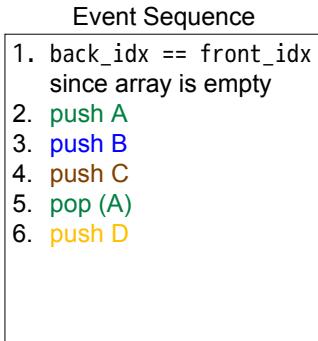
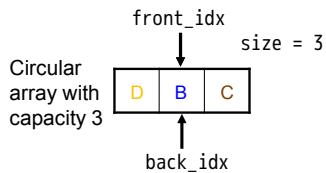
19

## Queue: Implementation – Circular Buffer



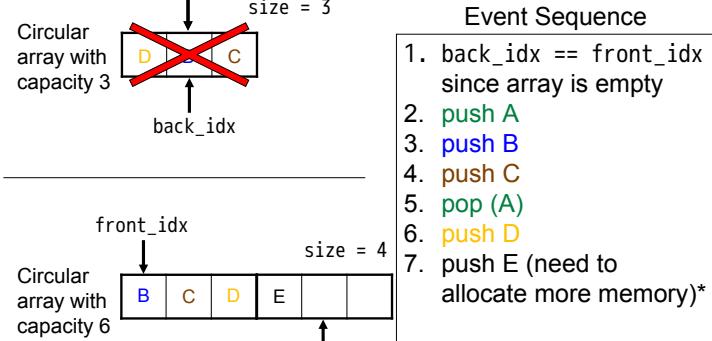
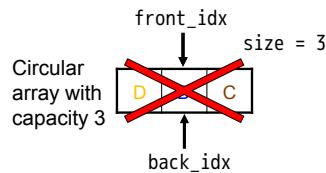
21

## Queue: Implementation – Circular Buffer



22

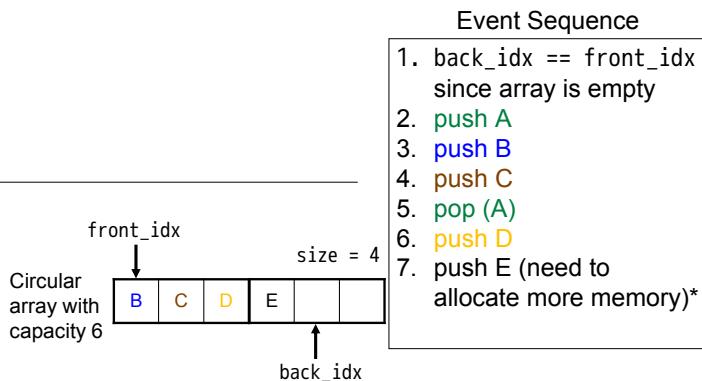
## Queue: Implementation – Circular Buffer



\* When allocating more memory, it is common to double memory

23

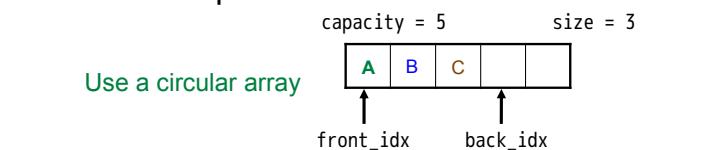
## Queue: Implementation – Circular Buffer



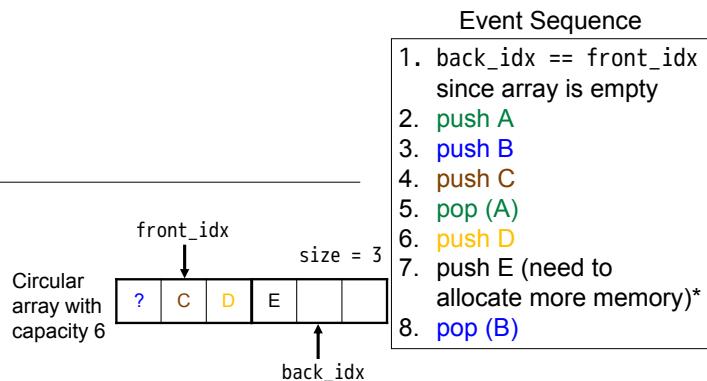
\* When allocating more memory, it is common to double memory

24

## Queue: Implementation – Circular Buffer

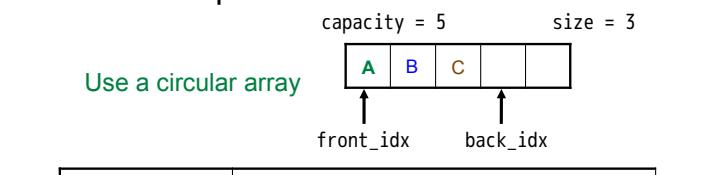


## Queue: Implementation – Circular Buffer



25

## Queue: Implementation – Circular Buffer



Method	Implementation
<code>push(object)</code>	1. If <code>size == capacity</code> , reallocate larger array and copy over elements, "unroll" as you go unroll: start <code>front_idx</code> at 0, insert all elements 2. Insert value at <code>back_idx</code> , increment <code>size</code> and <code>back_idx</code> , wrapping around either as needed
<code>pop()</code>	Increment <code>front_idx</code> , decrement <code>size</code>
<code>object &amp;front()</code>	Return reference to element at <code>front_idx</code>
<code>size()</code>	Return <code>size</code>
<code>empty()</code>	Check if <code>size == 0</code>

How many steps/operations for each method?

26

## Queue: Which Implementation?

Method	Array/Vector	Linked List
<code>push(object)</code>	Constant (linear when resizing vector)*	Constant
<code>pop()</code>	Constant	Constant
<code>object &amp;front()</code>	Constant	Constant
<code>size()</code>	Constant	Constant (with tracked size)
<code>empty()</code>	Constant	Constant

\*Averages out to constant with many pushes (amortized constant)

- The asymptotic complexities of each are similar
- The constant factor attached to the complexity is lower for vector
  - Constant number of operations, but there is "less" to do
  - The linked list must allocate memory for each node individually!
- The linked list also has higher memory overhead
  - i.e. Pointers between nodes as well as the actual data payload

28

## STL Queues: `std::queue<>`

- Code: `#include <queue>`
- You can choose the underlying container
- All operations are implemented generically on top of the given container
  - No specialized code based on given container

	Queue
Default Underlying Container	<code>std::deque&lt;&gt;</code>
Optional Underlying Container	<code>std::list&lt;&gt;</code>

29

## Deque Terminology Clarification

- "Deque" is an abbreviation of Double-Ended Queue.  
Pronounced "deck"
- "Dequeue" is another name for removing something from a queue.  
Pronounced "dee-queue"
- The STL includes `std::deque<>`, which is an implementation of a Deque, and is usually based on a growable collection of fixed-sized arrays.

## Deque ADT: a queue and stack in one (Double-ended Queue)

- ADT that allows efficient insertion and removal from the front and the back
- 6 major methods
  - `push_front()`, `pop_front()`, `front()`
  - `push_back()`, `pop_back()`, `back()`
- Minor methods
  - `size()`, `empty()`
- Can traverse using iterator



32

## Simple Deque Implementation

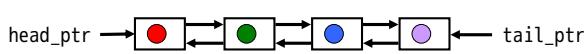
### Circular Buffer

- `front_idx` and `back_idx` both get incremented/decremented



### Doubly-linked list

- Singly-linked doesn't support efficient removal
- Other operations map directly to doubly-linked list operations

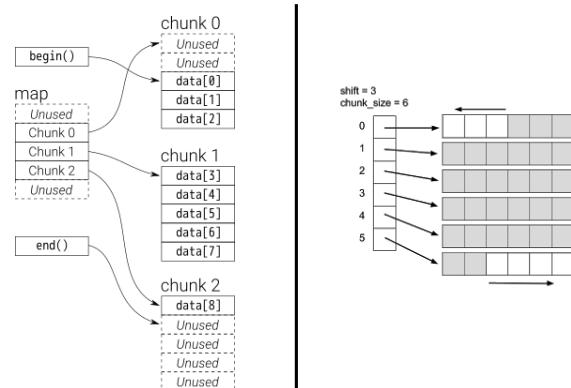


34

## STL Deques: `std::deque<>`

- Code: `#include <deque>`
- Stack/Queue-like behavior at both ends
- Random access with `[]` or `.at()`

## STL Deque, Two Internal Views



Taken from: <https://stackoverflow.com/questions/6292332/what-really-is-a-deque-in-stl> and <http://cpp-tip-of-the-day.blogspot.com/2013/11/how-is-stddeque-implemented.html>

35

## What is a Priority Queue?

- Each datum paired with a priority value
  - Priority values are usually numbers
  - Should be able to compare priority values (`<`)
- Supports insertion of data and inspection
- Supports removal of datum with highest priority
  - "Most important" determined by given ordering



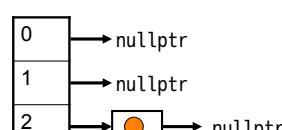
Like a group of bikers where the fastest ones exit the race first

39

## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

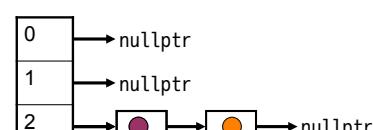
1. Level 2 call comes in



## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

1. Level 2 call comes in
2. Level 2 call comes in



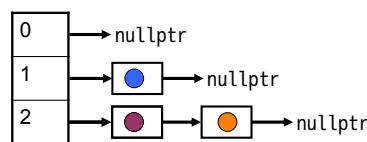
40

41

## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

1. Level 2 call comes in
2. Level 2 call comes in
3. Level 1 call comes in

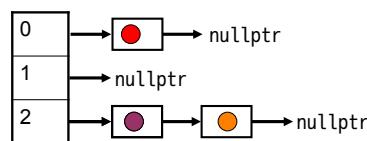


42

## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

1. Level 2 call comes in
2. Level 2 call comes in
3. Level 1 call comes in
4. A call is dispatched
5. Level 0 call comes in



44

## Priority Queue ADT: Interface

- Supports insertion, with removal in descending priority order

Method	Description
push(object)	Add object to the priority queue
pop()	Remove highest priority element
const object &top()	Return a reference to highest priority element
size()	Number of elements in priority queue
empty()	Checks if priority queue has no elements

### Examples

- Hospital queue for arriving patients
- Load balancing on servers

46

## A Customizable Container

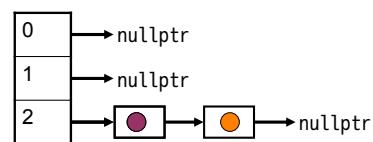
- By default `std::priority_queue<>` uses `std::less<>()` to determine relative priority of two elements
- A "default PQ" is a "max-PQ", where the largest element has highest priority
- If a "min-PQ" is desired, customize with `std::greater<>()`, so the smallest element has highest priority
- If the PQ will hold elements that cannot be compared with `std::less<>()` or `std::greater<>()`, customize with custom comparator (function object)
- Custom comparators can work with objects, perform tie-breaks on multiple object members, and other functionality

48

## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

1. Level 2 call comes in
2. Level 2 call comes in
3. Level 1 call comes in
4. A call is dispatched

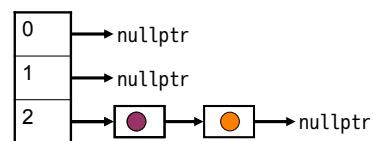


43

## Priority Queue Example: Emergency Call Center

- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

1. Level 2 call comes in
2. Level 2 call comes in
3. Level 1 call comes in
4. A call is dispatched
5. Level 0 call comes in
6. A call is dispatched



45

## Priority Queue Implementations

Underlying Implementation	Insert	Remove
Unordered sequence container	Constant	Linear
Sorted sequence container	Linear	Constant
Heap (presented in a future lecture)	Logarithmic	Logarithmic
Array of linked lists (for priorities of small integers)	Constant	Constant

47

## STL PQs: `std::priority_queue<>`

- STL will maintain a Heap in any random access container
  - `#include <queue>`
- Common `std::priority_queue<>` declarations
  - "Max" PQ using `std::less<>()`  
`std::priority_queue<T> myPQ;`
  - PQ using a custom comparator type, COMP  
`std::priority_queue<T, vector<T>, COMP> myPQ;`
- Manual priority queue implementation with standard library functions
  - `#include <algorithm>`
  - `std::make_heap()`
  - `std::push_heap()`
  - `std::pop_heap()`

49