

# Math 4580: Abstract Algebra I

Lecturer: **Professor Michael Lipnowski**

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## 1 January 6, 2025

We didn't have any but Dr. Lipnowski did post a module on [carmen](#) about the syllabus and the course. This semester we will be covering the first few chapters of the book *Abstract Algebra: Theory and Applications* by Thomas Judson.

### Definition 1

**Set:** A collection of distinct objects, considered as an object in its own right.

**Axioms:** A collection of objects  $S$  with assumed structural rules is defined by axioms.

**Statement:** In logic or mathematics, an assertion that is either true or false.

**Hypothesis and Conclusion:** In the statement "If  $P$ , then  $Q$ ",  $P$  is the hypothesis and  $Q$  is the conclusion.

**Mathematical Proof:** A logical argument that verifies the truth of a statement.

**Proposition:** A statement that can be proven true.

**Theorem:** A proposition of significant importance.

**Lemma:** A supporting proposition used to prove a theorem or another proposition.

**Corollary:** A proposition that follows directly from a theorem or proposition with minimal additional proof.

## 2 January 8, 2025