

Sample Paper
Answer 5 questions

Question 1 (Set Theory)

[20 marks]

1. Fill in the blanks with \in , \notin , \subseteq , $=$ or \neq . Recall that \mathbb{Z} is the set of all integers and ϕ is the empty set. (10 marks)
 - i. 2 ----- $\{2, 4, 7\}$
 - ii. 7 ----- \mathbb{Z}^+
 - iii. $\{1, -2, 8\}$ ----- \mathbb{Z}
 - iv. 21 ----- $\{168, 147, 126, \dots\}$
 - v. $\{16\}$ ----- $\{4, 8, 12\}$
2. Given the universal set $U = \{1, 2, 3, 4, 5, 7, 9, 11, 13, 15\}$, $A = \{1, 3, 9, 15\}$, $B = \{3, 9, 11\}$, $D = \{2, 4\}$ find the following.
 - i. $A \cap B$ (2 marks)
 - ii. $(A \cup D)'$ (2 marks)
 - iii. $D \times B$ (2 marks)
 - iv. Find all subsets of A. (2 marks)
3. In a class of 30 students, 16 like English, 13 students like Science and English, 6 students do not like Science or English. How many Students like only Science? (2 marks)

Question 2 (Propositional Logic)

[20 marks]

1. Given that p, q and r are propositions, construct truth tables and verify the following:
 - i. $\sim(p \vee q) = \sim p \wedge \sim q$ (4 marks)
 - ii. $p \wedge (q \wedge r) = (p \wedge q) \wedge r$ (4 marks)
 - iii. $\sim((p \vee q) \wedge r) = (\sim p \wedge \sim q) \vee \sim r$ (4 marks)
2. Determine whether the following compound propositions are tautologies, contradictions or contingent propositions?
 - i. $p \wedge (q \wedge \sim q)$ (4 marks)
 - ii. $p \Leftrightarrow (\sim p \wedge q)$ (4 marks)

Question 3 (Coordinate Geometry)

[20 marks]

1. The general form of the equation of a straight line(L_1) is $8x - 2y - 6 = 0$.
 - i. Write L_1 in $y = mx + c$ format. (2 marks)

- ii. What is the slope? (2 marks)
- iii. What is the intercept? (2 marks)
- iv. Find the line equation parallel to L_1 going through the point (3, 2) (2 marks)

2. $L_{xy}: x - y + 1 = 0$ $L_{xz}: 3x + y - 13 = 0$ $L_{yz}: x + 3y - 7 = 0$ are line equations of the sides of the triangle XYZ.

- i. Find the vertices (X, Y and Z) of the triangle. (6 marks)
- ii. Determine equation of the circle through X, Y and Z points. (6 marks)

Question 4 (Matrix Algebra)

[20 marks]

If $A = \begin{bmatrix} 1 & 5 \\ 3 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 2 \\ -1 & 4 \end{bmatrix}$

1. Find the following:
 - i. $A + B$ (2 marks)
 - ii. Determinant of $A - B$ (3 marks)
 - iii. AB (3 marks)
2. Solve the following system of linear equations using matrix inversion. (12 marks)

$$\begin{aligned} x - 2y + z &= 7 \\ 2x + y - 2z &= -3 \\ x + 2y - 3z &= -9 \end{aligned}$$

Question 5 (Logarithms)

[20 marks]

1. Use the Laws of Logarithms to expand each expression.
 - i. $\log_2 2x^2$ (3 marks)
 - ii. $\log_3 (x^2 y^{-3})$ (3 marks)
 - iii. $\ln \left(\frac{a^2 \sqrt{b^3}}{\sqrt[5]{c^2}} \right)$ (3 marks)
2. Evaluate the following:
 - i. $\log_7 5$ (2 marks)
 - ii. $\log_3 81 \log_5 0.008 \log_8 0.125$ (4 marks)
3. Solve the equation $5^{2x} - 12(5^x) + 35 = 0$. Find the value of x for three decimal places. (5 marks)

Question 6 (Statistics)**[20 marks]**

1. Briefly describe the terms 'Median', and "Mode"? (4 marks)
2. The Bookstall Inc. is a special bookstore selling used books. Paperbacks are \$ 1.00 each and hardcover books are \$ 3.50 each. Last Tuesday morning 50 books were sold. Out of that 40 were paperbacks and the rest were hardcover. What was the weighted mean price of a book sold? (3 marks)
3. The following data selected randomly, represent the daily temperature measurements (in Celsius degrees) of eleven days of a town.

27, 23, 28, 19, 34, 28, 32, 20, 28, 25 and 18

Find the following:

- a. Mean (2 marks)
- b. Median (2 marks)
- c. Mode (2 marks)
- d. Interquartile range (3 marks)
- e. Standard Deviation (4 marks)

Question 7 (Statistics)**[20 marks]**

1. Explain the following terms briefly
 - a. Population (2 marks)
 - b. Census (2 marks)
2. The table given below is a frequency distribution that shows the profit made by 100 businesses.

Profit (Rs. in 000s)	Number of companies
20 – 25	02
25 – 30	05
30 – 35	14
35 – 40	20
40 – 45	25
45 – 50	17
50 – 55	10
55 – 60	07

Calculate the following statistical parameters:

- | | |
|------------------------|-----------|
| a. Mean | (3 marks) |
| b. Median | (4 marks) |
| c. Mode | (4 marks) |
| d. Standard Deviation. | (5 marks) |

Note: Median, Mode and Standard Deviation for grouped data are calculated as follows:

$$Median = L + \frac{\left(\frac{n}{2}\right) - m}{f} \times c \quad Mode = L + \frac{(f_1 - f_0)}{(f_1 - f_0) + (f_1 - f_2)} \times c \quad Std = \sqrt{\frac{\sum f_i (x_i - \bar{x})^2}{n-1}}$$

End of Paper