

Assignment-03

$-17 \bmod 23$

$$\begin{array}{r} 23 \overline{) -17} \quad (-1) \\ \underline{-23} \\ (+) \\ \hline 6 \end{array}$$

$$-17 = (-1 \times 23) + 6$$

$$-17 \bmod 23 = 6$$

Multiplicative Inverse of $-13 \bmod 23$

The multiplicative inverse of a number $a \bmod m$ is a number x such that:

$$ax \equiv 1 \bmod m$$

In our case, we are looking for a number x such that:

$$-13x \equiv 1 \bmod 23$$

To simplify, we first convert -13 into a positive equivalent module 23.

$$-13 \bmod 23 = -13 + 23 = 10$$

So, the equation becomes 3:

$$10x \equiv 1 \bmod 23$$

if $x=1$, $10 \times 1 = 10 \not\equiv 1 \pmod{23}$

if $x=2$, $10 \times 2 = 20 \not\equiv 1 \pmod{23}$

if $x=3$, $10 \times 3 = 30 \equiv 7 \pmod{23}$

if $x=4$, $10 \times 4 = 40 \equiv 17 \pmod{23}$

if $x=5$, $10 \times 5 = 50 \equiv 4 \pmod{23}$

if $x=6$, $10 \times 6 = 60 \equiv 14 \pmod{23}$

if $x=7$, $10 \times 7 = 70 \equiv 1 \pmod{23}$

if we found it: $10 \times 7 = 70 \equiv 1 \pmod{23}$

since $-13 \equiv 10 \pmod{23}$ and $10^{-1} \pmod{23} = 7$

We conclude,

The multiplicative inverse of $-13 \pmod{23}$ is 7