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Assignment-1

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Github repository

https://github.com/Sadiq0123/C-and-DS/tree/main/Assignment-1

1 Problem

Consider the following C program:

```
#include <stdio.h>

int counter = 0;
int calc (int a, int b) {
   int c;

   counter++;
   if (b==3) return (a*a*a);
   else {
       c = calc(a, b/3);
       return (c*c*c);
   }
}

int main (){
   calc(4, 81);
   printf ("%d", counter);
}
```

The output of this program is _.

2 Solution

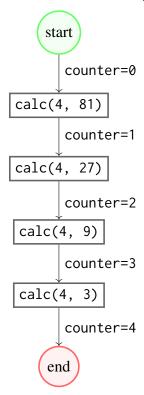
Answer: 4.

The variable counter is a global variable with initial value set to 0, and is incremented by 1 everytime the function calc is called.

The function calc returns a^b only if b is a power of 3; else the function returns nothing. The code behaves this way because eventually the function calls calc(a, b/3) where b < 3, which leads to an infinite recursive call of calc(a, \emptyset). So, the stack overflow causes Segmentation Fault

error during runtime.

If b is valid, then calc recursively calls itself for b/3. So, the total number of times counter is incremented is $\log_3(b)$ times. The following table shows the value of counter at every step.



As $log_3(81) = 4$, the output of the code would be equal to 4.

3 Mathematical Formula

One function call of calc(a, b) increments counter by 1, and calls the function calc(a, b/3). This can be mathematically written using a function f, that returns the counter variable value as shown below.

$$f(b) = 1 + f(b/3)$$
 (3.0.1)

Also, when b = 3, counter is incremented once and returns.

$$f(3) = 1$$
 (3.0.2)

The recurrence equation would then be

$$f(b) = 1 + f(b/3)$$
 (3.0.3)

$$f(b/3) = 1 + f(b/3^2)$$
 (3.0.4)

...
$$f(3) = 1$$
 (3.0.5)

The number of times the function is called can be derived from the equation

$$b/3^{counter} = 1 \tag{3.0.6}$$

$$\log_3 b = \log_3 3^{\text{counter}} \implies \text{counter} = \log_3 b$$
(3.0.7)

Therefore, The general mathematical relation between input (a, b) and output counter is: counter = $log_3(b)$