

Presentation

EE2227- Control Systems

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Outline

Problem Statement

Polar Plot

Solution

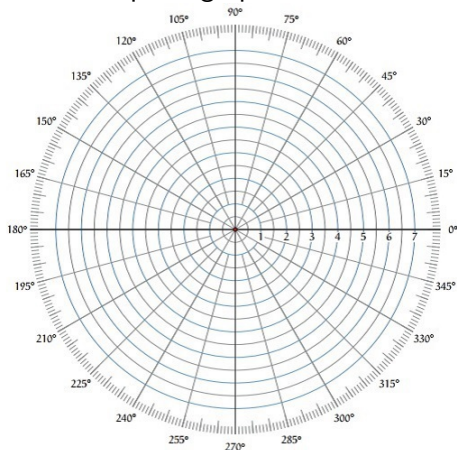
Verification

Q. The polar plot for the transfer function $G(s) = \frac{10(s+1)}{10+s}$ for $0 \leq \omega < \infty$ will be in the

- (A) first quadrant
- (B) second quadrant
- (C) third quadrant
- (D) fourth quadrant

Polar Plot

The Polar plot is a plot, which can be drawn between the magnitude and the phase angle of $G(j\omega)H(j\omega)$ by varying ω from 0 to ∞ . The polar graph sheet is shown in the following figure.



Solution

Substituting $s = j\omega$ in the given transfer function gives

$$G(j\omega) = \frac{10(1+j\omega)}{(10+j\omega)}$$

Here, taking $1 + j\omega = \sqrt{1 + \omega^2} e^{j \tan^{-1}(\omega)}$,

and $10 + j\omega = \sqrt{10^2 + \omega^2} e^{j \tan^{-1}(\frac{\omega}{10})}$,

$$G(j\omega) = 10 \sqrt{\frac{1+\omega^2}{100+\omega^2}} e^{j(\tan^{-1}(\omega) - \tan^{-1}(\frac{\omega}{10}))}$$

Solution

As $0 \leq \omega < \infty$,

$$10\sqrt{\frac{1+\omega^2}{100+\omega^2}} > 0 \text{ and } 0 \leq \tan^{-1}(\omega), \tan^{-1}\left(\frac{\omega}{10}\right) < \frac{\pi}{2}$$

and as \tan^{-1} is a monotonically increasing function,

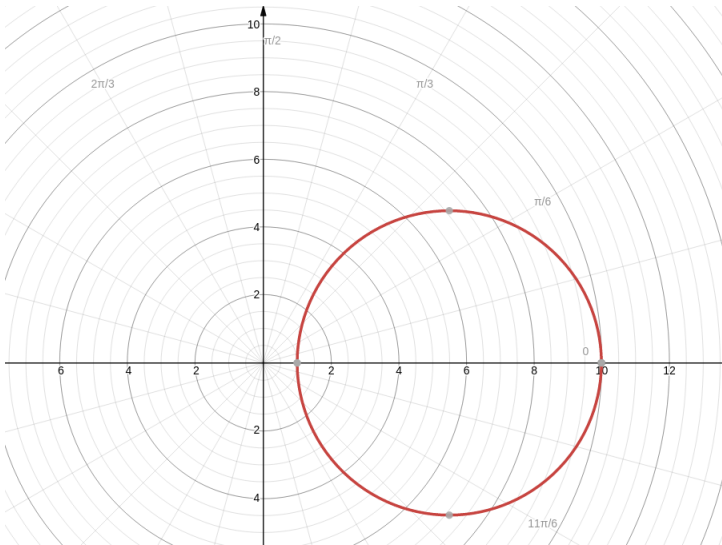
$$\tan^{-1}(\omega) \geq \tan^{-1}\left(\frac{\omega}{10}\right), \text{ with equality as } \omega \rightarrow \infty$$

$$\text{So, } |G(j\omega)| > 0 \text{ and } 0 \leq \angle G(j\omega) < \frac{\pi}{2}$$

Therefore, the polar plot of $G(s)$ lies in the first quadrant.

The plot of $G(s)$ is:

Plot of $G(s)$



THANK YOU