

## (15) Series & Parallel AC Circuits

DC Circuit  $\rightarrow$  Inductor  $\rightarrow$  Short Circuit  
Capacitor  $\rightarrow$  open circuit

Resistor  $\rightarrow$  Heat (active power)

Capacitor, Inductor  $\rightarrow$  Power storage (Reactive Power)

$$\boxed{Z_R = R \angle 0^\circ}$$

$$= R \cos 0 + j R \sin 0$$

$$= R$$

$Z_R = \text{impedance}$

Complex Number:  $a + jb$   
 $\downarrow$   $\downarrow$   
 Real Imaginary

$\rightarrow$  Cartesian or rectangular format

for example:  $2 + j3$

$a + jb \rightarrow M \angle \theta$  [Polar Form]  
 Calculator  $\rightarrow$  Format  $\rightarrow$  Polar

$$M = \sqrt{a^2 + b^2}$$

magnitude

$$\theta = \tan^{-1} \frac{b}{a}$$

$$(a + jb) + (c + jd)$$

$$= (a + c) + j(b + d)$$

$$\left[ \begin{array}{l} j \times j = j^2 = -1 \\ j^3 = j^2 \times j = -j \\ j^4 = j^2 \times j^2 = 1 \end{array} \right]$$

$$M_1 \angle \theta_1 \times M_2 \angle \theta_2$$

$$= M_1 \times M_2 \angle (\theta_1 + \theta_2)$$

$$\frac{M_1 \angle \theta_1}{M_2 \angle \theta_2} = \frac{M_1}{M_2} \angle (\theta_1 - \theta_2)$$

$$M \angle \theta \rightarrow a + jb$$

$$= M \cos \theta + j M \sin \theta$$

$$\boxed{Z_L = X_L \angle 90^\circ}$$

$$= \omega L \angle 90^\circ$$

$$= jX_L \left[ \because X_L \cos 90^\circ + jX_L \sin 90^\circ \right]$$

$$= j\omega L$$

$$\therefore X_L = \omega L$$

Similarly for capacitor,

$$\boxed{Z_C = X_C \angle -90^\circ}$$

Voltage lags current

$$= X_C (\cos(-90^\circ) + jX_C \sin(-90^\circ))$$

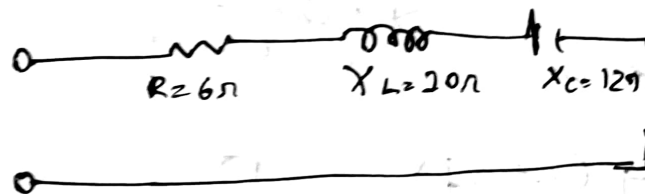
$$= -jX_C$$

Series Configuration:

$$Z_T = Z_1 + Z_2 + Z_3 + \dots + Z_n$$

Ex - 15.23

Find  $Z_T$



Ans:

$$Z_T = Z_1 + Z_2 + Z_3$$

$$= R \angle 0^\circ + X_L \angle 90^\circ + X_C \angle -90^\circ$$

$$= R + jX_L - jX_C$$

$$= R + j(X_L - X_C) = 6\Omega + j(20\Omega - 12\Omega)$$

$$= 6\Omega - j2\Omega$$

$$Z_T = 6.325\Omega \angle -18.43^\circ \text{ (by using Calc.)}$$

$$I = \frac{E/V}{Z_T}$$

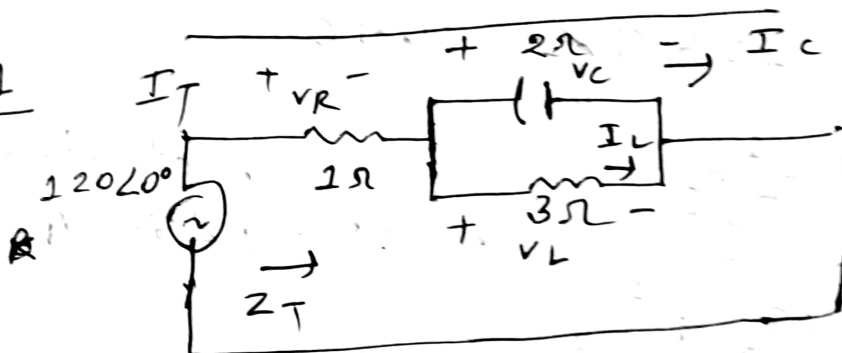
$I$  = current  
 $E$  = supply voltage  
 $Z_T$  = total impedance

$$P = EI \cos \theta_T$$

$P$  = Power  
 $E$  = voltage  
 $I$  = current  
 $\theta_T$  = phase angle between  $\vec{I}$  &  $\vec{E}$   
 $\vec{E} - \vec{I}$

## (16) Series-Parallel ac Networks

Ex 16.1



- a)  $Z_T$     b)  $I_T$     c)  $V_R$  &  $V_C$   
 d)  $I_C$     e) Power delivered    f) power factor

Ans:

$$a) Z_T = 1 + (-j2 \parallel j3)$$

series

parallel

$$= 1 + \left( \frac{1}{-j2} + \frac{1}{j3} \right)^{-1} \left[ \begin{array}{l} \text{capacitor } -j \\ \text{inductance } j \end{array} \right]$$

$$= 6.08 \angle -80.54^\circ \Omega$$

$$b) I_T = \frac{V}{Z_T} = \frac{120 \angle 0^\circ}{6.08 \angle -80.54^\circ} = 19.74 \angle 80.54^\circ \text{ A}$$

$$c) V_R = I_T \times R = 19.74 \angle 80.54^\circ \times 1 = 19.74 \angle 80.54^\circ$$

(Resistor has across voltage)

$$V_L = V_C \quad [\text{Parallel (2T22 Voltage same)}]$$

$$V_{\text{supply}} = V_R + V_C$$

$$\Rightarrow 220 \angle 0^\circ = 19.74 \angle 80.54^\circ + V_C$$

$$\Rightarrow V_C = 118.4 \angle -9.46^\circ$$

$$d) I_C = \frac{\frac{1}{-j2}}{\frac{1}{-j2} + \frac{1}{j3}} \times 19.74 \angle 80.54^\circ$$

(current divider rule)

$$= 59.22 \angle 80.54^\circ$$

$I_C$  across  $V_C$  (2T22)

$$V_C = I_C \times -j2$$

e) Real Power.

$$P = I^2 R$$

$$= I_T^2 R$$

$$= (19.74 \angle 80.54^\circ)^2 \times 1$$

$$= (19.74)^2$$

$$= 389.67 \text{ W}$$

$$f) \text{PF} = \cos \theta$$

$$= \cos 80.54^\circ$$

$$= 0.164 \text{ (leading)}$$

2T22 angle

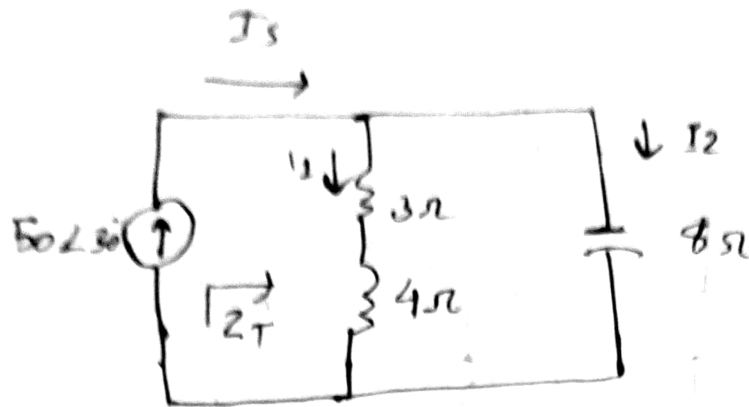
If  $\theta \rightarrow -$

Leading

Power factor

$\theta \rightarrow +$ , lagging

Ex - 26.2



Find  $I_1$ ,  $I_2$ ,  $I_s$ ,  $Z_T$

Ans:

$I_1$

$$= \frac{1}{3+j4}$$

(current divider rule)

$$\frac{1}{\frac{1}{3+j4} + \frac{1}{-j8}}$$

$\times 50\angle 30^\circ$  (total)

$$= 80\angle -6.87^\circ$$

$$I_2 = \frac{1}{-8j}$$

$$\frac{1}{\frac{1}{3+j4} + \frac{1}{-j8}}$$

$\times 50\angle 30^\circ$

$$= 50\angle 136.26^\circ$$

$$I_s = I_1 + I_2$$

$$Z_T = \left( \frac{1}{3+j4} + \frac{1}{-j8} \right)^{-1}$$

$$= 8\angle 16.26^\circ \Omega$$

$$P.F. = \cos \theta \text{ (} Z_T \text{ angle)}$$

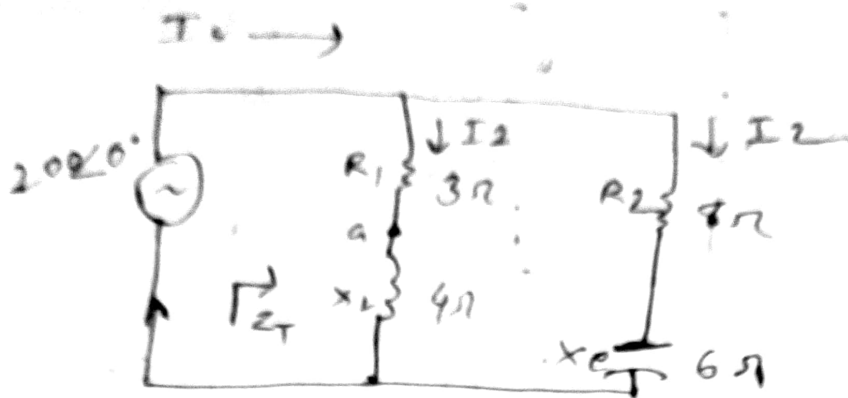
$$= \cos 16.26$$

$$= 0.96 \text{ (lagging)} - \text{2\% leading}$$

$$P = |I_2|^2 R$$

$$= 80^2 \times 3 = 1920 \text{ W}$$

Ex - 26.4



i) Find  $Z_T = (3+j4) \parallel (8-j6)$

$$= \left( \frac{1}{3+j4} + \frac{1}{8-j6} \right)^{-1}$$

~~$= 0.098 \angle 37.99^\circ$~~

$$= 4.47 \angle 26.56^\circ$$

ii) Find  $I_S = \frac{V}{Z_T} \left( \frac{V}{R} \text{ or } \frac{V}{X} \right)$   
(Total current)

$$= \frac{100 \angle 0^\circ}{4.47 \angle 26.56^\circ} = 22.3 \angle -26.56^\circ \text{ A}$$

iii)  $I_1 = \frac{1}{3+j4}$

$$\frac{1}{3+j4} + \frac{1}{8-j6} \times 22.3 \angle -26.56^\circ \text{ A}$$

$$= 19.24 \angle -53.12^\circ \text{ A}$$

$$\underline{\text{iv)}} \quad I_2 = \frac{\frac{1}{8-j6}}{\frac{1}{8-j6} + \frac{1}{3+j4}} \times 22.3 \angle -26.56^\circ$$

$$= 9.97 \angle 36.87^\circ \text{ A}$$

[  $I_1, I_2$  calculation  
 6/12/23 ]

$V_A$  voltage point to voltage, after ground  $\rightarrow$   
 $V_L$  is,

$$\underline{\text{v)}} \quad \text{Find } V_L / V_A$$

$$V_A = (I_2) \times (j X_L)$$

$$= 9.97 \angle -53.12^\circ \times j4$$

$$= \cancel{79.76 \angle -53.12^\circ \text{ V}}$$

$$= 79.76 \angle 36.88^\circ \text{ V}$$

$$\underline{\text{vi)}} \quad V_b = I_2 \times -j X_C$$

$$= 9.97 \angle 36.87^\circ \times -j6$$

$$= \cancel{59.82 \angle -53.13^\circ \text{ V}}$$

$$= 59.82 \angle -53.13^\circ \text{ V}$$

$$\underline{\text{vii)}} \quad V_{ab} = V_A - V_b$$

$$= (79.76 \angle 36.88^\circ) - (59.82 \angle -53.13^\circ)$$

$$\underline{\text{viii)}} \quad \text{P.F} = \cos \theta = \frac{100 \angle 73.74^\circ}{100 \angle 26.56^\circ} = 0.89 \text{ (lagging)}$$

$$\underline{\text{ix)}} \quad \text{Power delivered} = |I_1|^2 R_1 + |I_2|^2 R_2$$

$$= (29.94^2 \times 3) + (9.97^2 \times 8) = 1788.026$$