

ForcastStockMarket

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R Markdown

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When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
#####
#####
# Script name: ForecastStockMarketARIMA.R
# Porpose : This script is developed to forecast the S&P 500 Index over the 10 years
#           I have used the ARIMA model (Time Series) in R
# Data source: Data source could be off-line (marketPriceHistory.csv) or online SP&500
# R Package usagae:
# ggplot2
# forecast
# plotly
# ggfortify
# tseries
# gridExtra
# docstring
# here
#####
#####
#Developer      Date          Version       Reason
#Saeid Rezaei   2017-12-20    0            Initial Version
#Saeid Rezaei   2018-01-05    1            Added ARIMA method to script
#####
#####
```

#By Milind Paradkar

*#Prediction is very difficult, especially about the future. Many of you must have come across this famous quote by Neils Bohr,
#a Danish physicist. Prediction is the theme of this blog post. In this post, we will cover the popular ARIMA forecasting model
#to predict returns on a stock and demonstrate a step-by-step process of ARIMA modeling using R programming.*

*#What is a forecasting model in Time Series?
#Forecasting involves predicting values for a variable using its historical data points or it can also
#involve predicting the change in one variable given the change in the value of another variable.
#Forecasting approaches are primarily categorized into qualitative forecasting and quantitative forecasting.
#Time series forecasting falls under the category of quantitative forecasting wherein statistical principals and concepts are
#applied to a given historical data of a variable to forecast the future values of the same variable.
#Some time series forecasting techniques used include:*

*#Autoregressive Models (AR)
#Moving Average Models (MA)
#Seasonal Regression Models
#Distributed Lags Models*

```
#What is Autoregressive Integrated Moving Average (ARIMA)?  
#ARIMA stands for Autoregressive Integrated Moving Average. ARIMA is also known as Box-Jenkins approach.  
#Box and Jenkins claimed that non-stationary data can be made stationary by differencing the series,  
#Yt. The general model for Yt is written as,  
  
#identically distributed error terms with zero mean. Here, Yt is expressed in terms of its past values and the  
#current and past values of error terms.  
  
print ("STEP 1.0: Installing the packages...")
```

```
## [1] "STEP 1.0: Installing the packages..."
```

```
#install.packages("ggplot2")  
#install.packages("forecast")  
#install.packages("plotly")  
#install.packages("ggfortify")  
#install.packages("tseries")  
#install.packages("gridExtra")  
#install.packages("docstring")  
#install.packages("here")  
  
library(ggplot2)
```

```
## Warning: package 'ggplot2' was built under R version 3.3.3
```

```
library(forecast)
```

```
## Warning: package 'forecast' was built under R version 3.3.3
```

```
library(plotly)
```

```
## Warning: package 'plotly' was built under R version 3.3.3
```

```
##  
## Attaching package: 'plotly'
```

```
## The following object is masked from 'package:ggplot2':  
##  
##     last_plot
```

```
## The following object is masked from 'package:stats':  
##  
##     filter
```

```
## The following object is masked from 'package:graphics':  
##  
##     layout
```

```
library(ggfortify)
```

```
## Warning: package 'ggfortify' was built under R version 3.3.3
```

```
##  
## Attaching package: 'ggfortify'
```

```
## The following object is masked from 'package:forecast':  
##  
##     gglagplot
```

```
library(tseries)
```

```
## Warning: package 'tseries' was built under R version 3.3.3
```

```
library(gridExtra)
```

```
## Warning: package 'gridExtra' was built under R version 3.3.3
```

```
library(docstring)
```

```
## Warning: package 'docstring' was built under R version 3.3.3
```

```
##  
## Attaching package: 'docstring'
```

```
## The following object is masked from 'package:utils':  
##  
##     ?
```

```
library(here)
```

```
## Warning: package 'here' was built under R version 3.3.3
```

```
## here() starts at C:/CHM136
```

```
# Find the Local / Working directory and copy all the project there  
print ("STEP 1.1: Find the working directory.")
```

```
## [1] "STEP 1.1: Find the working directory."
```

```
here()
```

```
## [1] "C:/CHM136"
```

```
source(here("src",'main_functions.R'))  
# NOTE: For more information on helper functions use ?function_name  
  
print ("STEP 1.2: Loading Data.")
```

```
## [1] "STEP 1.2: Loading Data."
```

```
# LOAD DATA  
dataMaster <- read.csv(here("data", "SP500Data.csv"))  
attach(dataMaster)  
print ("STEP 2.1: Start Analysing.")
```

```
## [1] "STEP 2.1: Start Analysing."
```

```
# EXPLORATORY ANALYSIS  
# I'm going to get valumn from 1995 to present with frq 12  
sp_500 <- ts(dataMaster$sp_500, start=c(1995, 1), freq=12)  
  
# TESTS FOR STATIONARITY  
Box.test(sp_500, lag = 20, type = 'Ljung-Box')
```

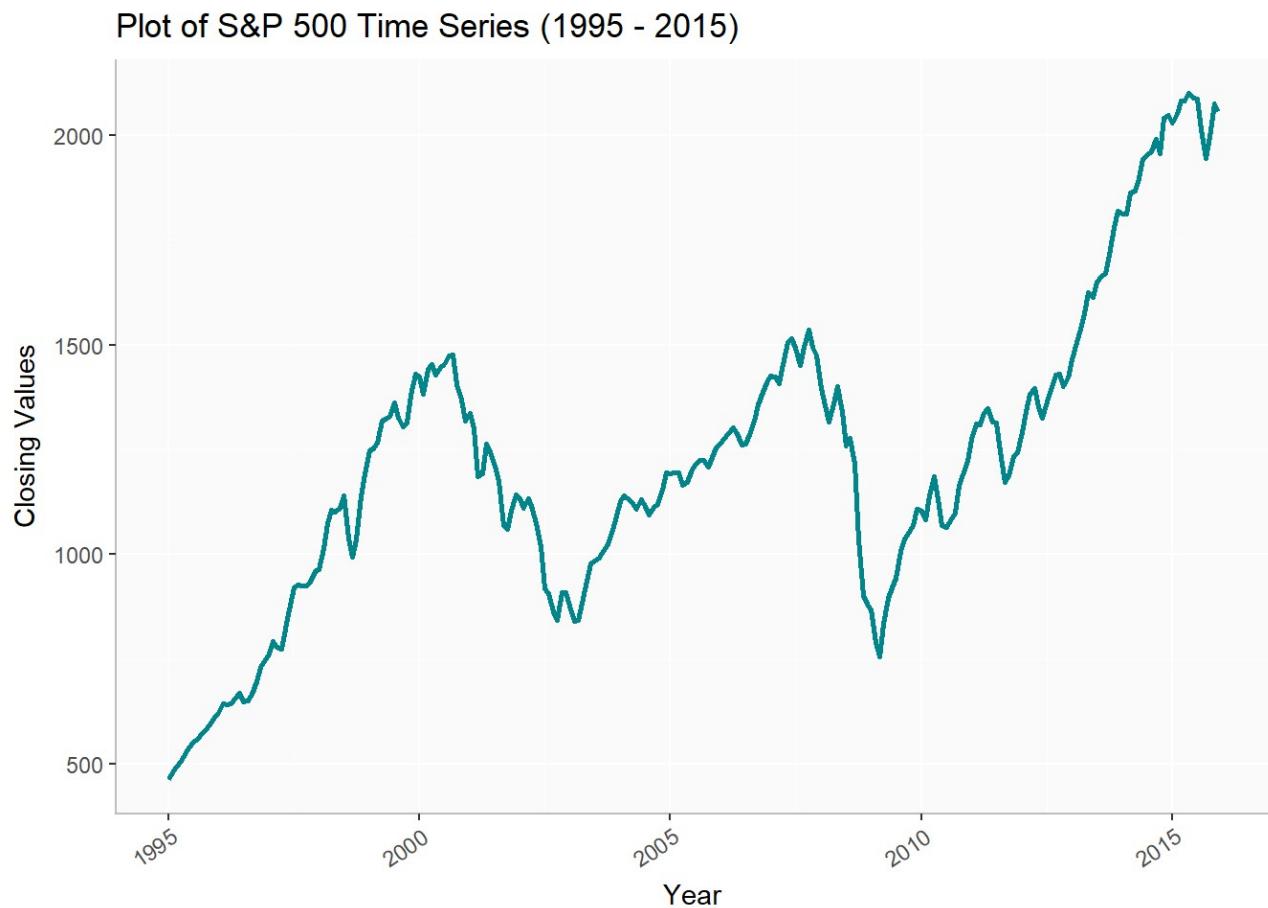
```
##  
## Box-Ljung test  
##  
## data: sp_500  
## X-squared = 2532.4, df = 20, p-value < 2.2e-16
```

```
adf.test(sp_500)
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: sp_500  
## Dickey-Fuller = -1.816, Lag order = 6, p-value = 0.6533  
## alternative hypothesis: stationary
```

```
# p-values are relatively high so we should do visual inspection and  
# Look at ACF and PACF plots to make appropriate transformation  
# for stationarity.
```

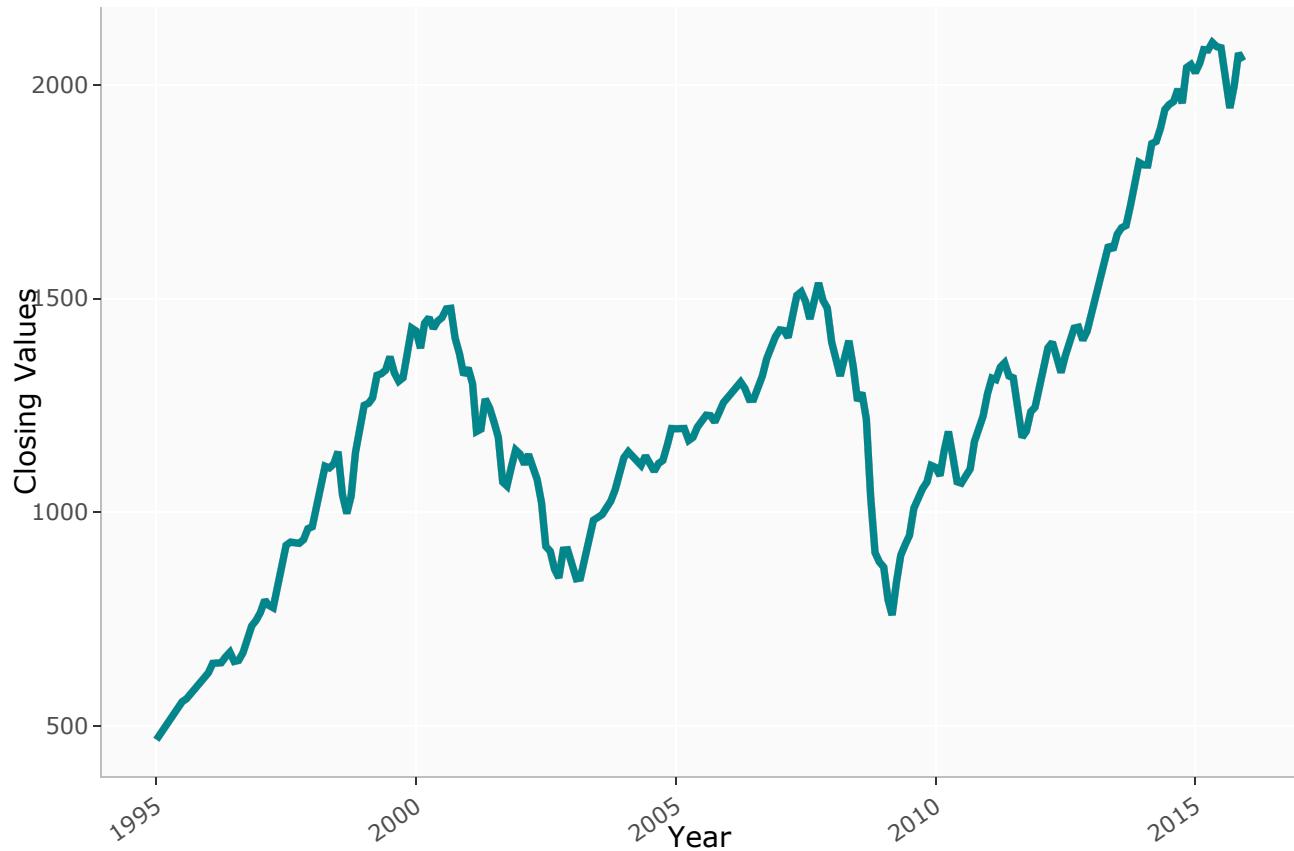
```
# TIME SERIES PLOT OF S&P  
tsSp <- plot_time_series(sp_500, 'S&P 500')  
  
tsSp
```



```
ggplotly(tsSp)
```

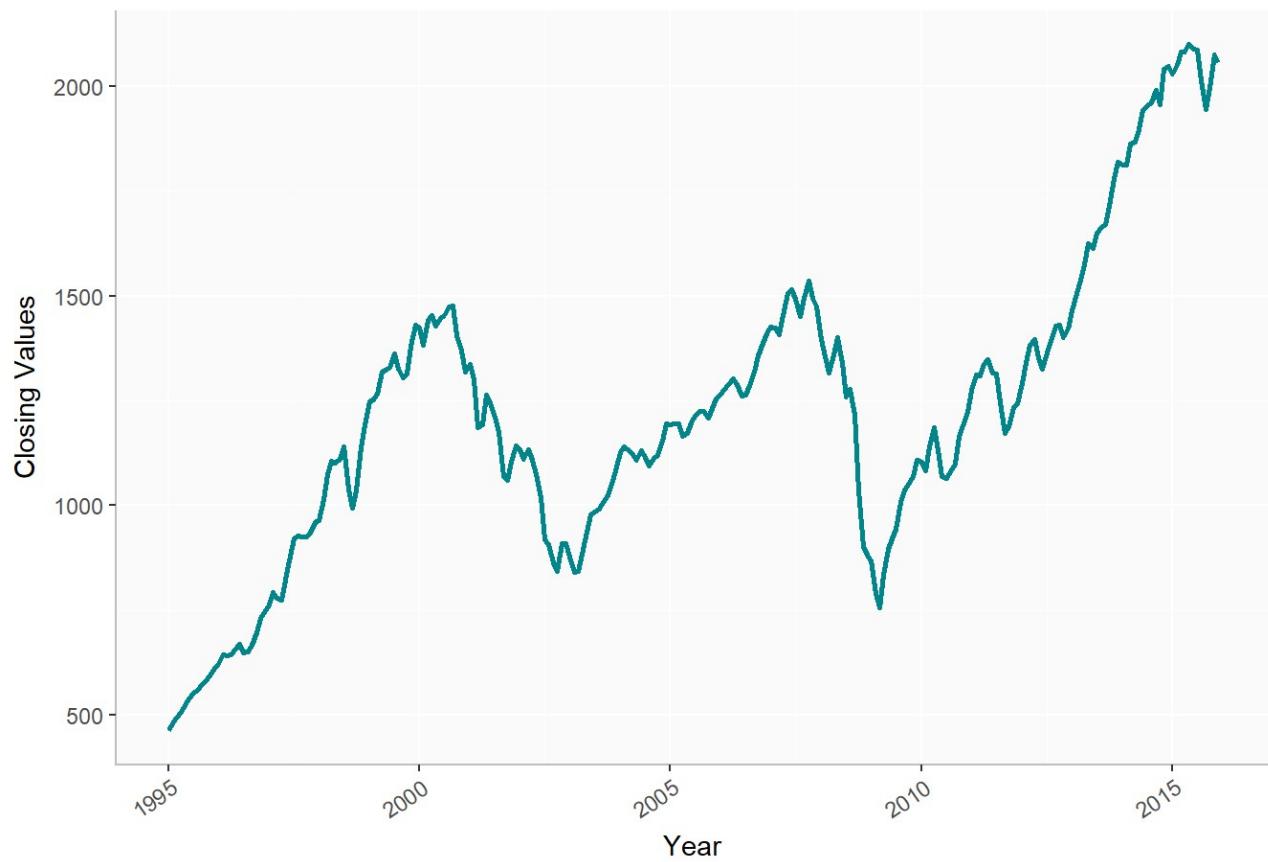
```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Plot of S&P 500 Time Series (1995 - 2015)



```
# Here we create the training set where we will compare the values for 2015  
sp500_TR <- ts(sp_500, start=c(1995, 1), end=c(2014, 12), freq=12)  
plot_time_series(sp_500, 'S&P 500 Training Set')
```

Plot of S&P 500 Training Set Time Series (1995 - 2015)

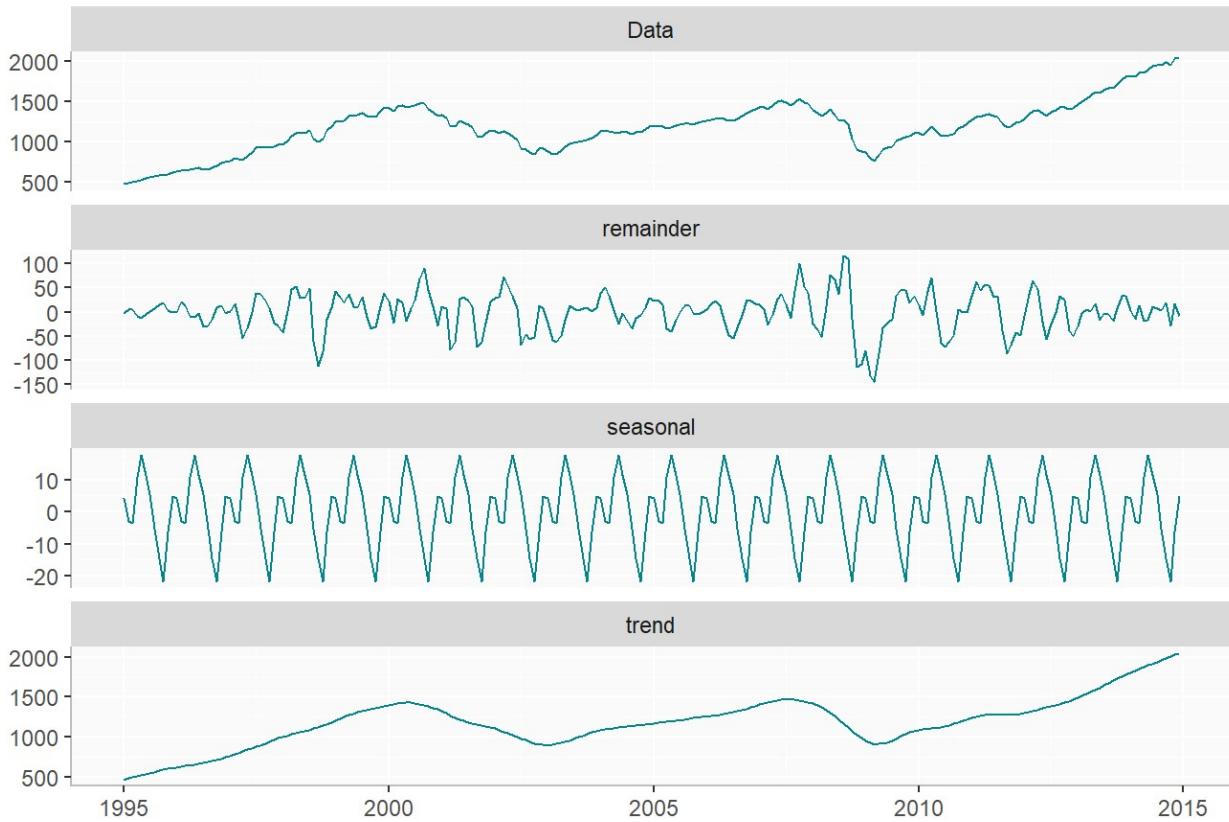


```
print ("STEP 2.2: plotting the SP500")
```

```
## [1] "STEP 2.2: plotting the SP500"
```

```
# DECOMPOSING TIME SERIES
sp500_stl <- plot_decomp(sp500_TR, 'S&P 500')
sp500_stl
```

Decomposition Plot of S&P 500

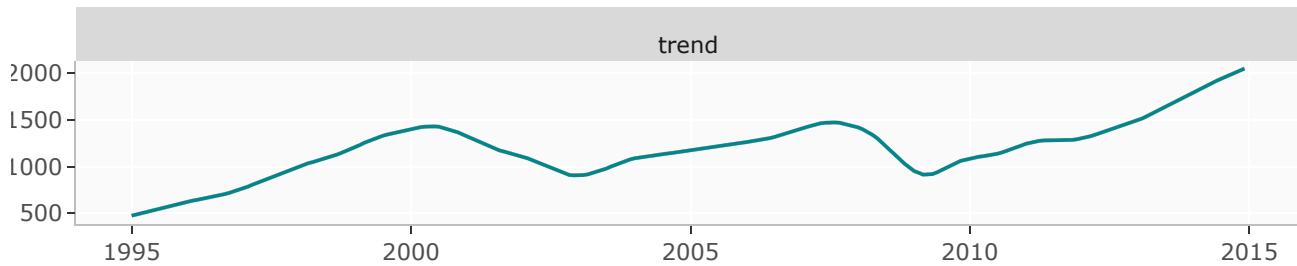


```
ggplotly(sp500_stl)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Decomposition Plot of S&P 500

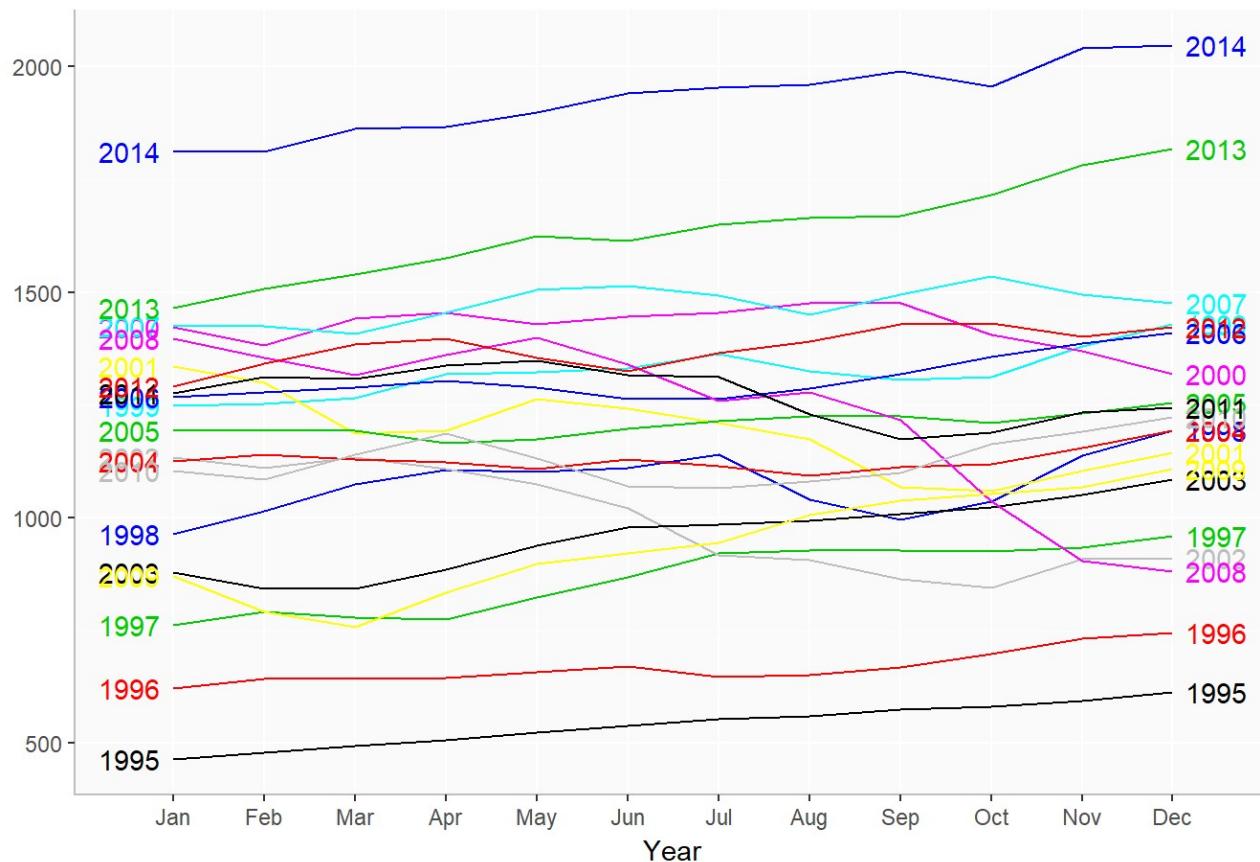




```
# SEASONAL PLOT
seasonal_Plot <- plot_seasonal(sp500_TR, 'S&P 500')

seasonal_Plot
```

Seasonal Plot of S&P 500

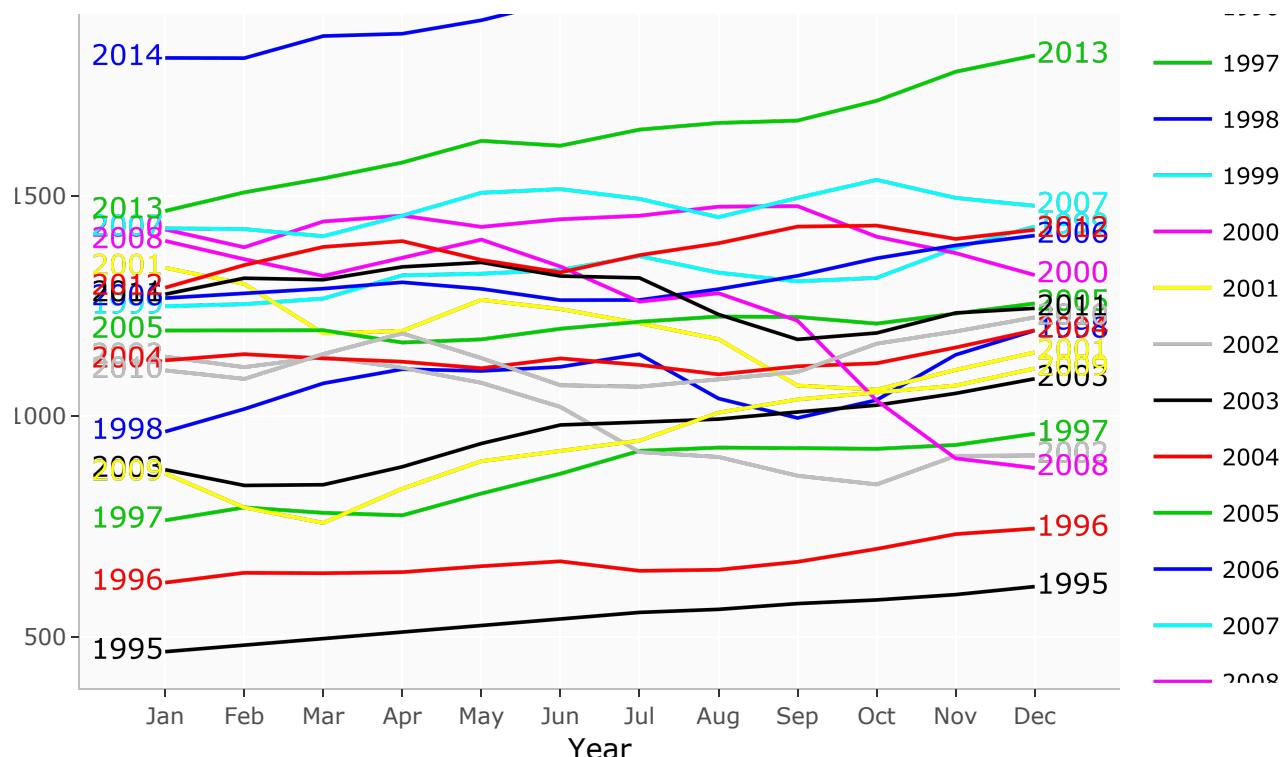


```
ggplotly(seasonal_Plot)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Seasonal Plot of S&P 500

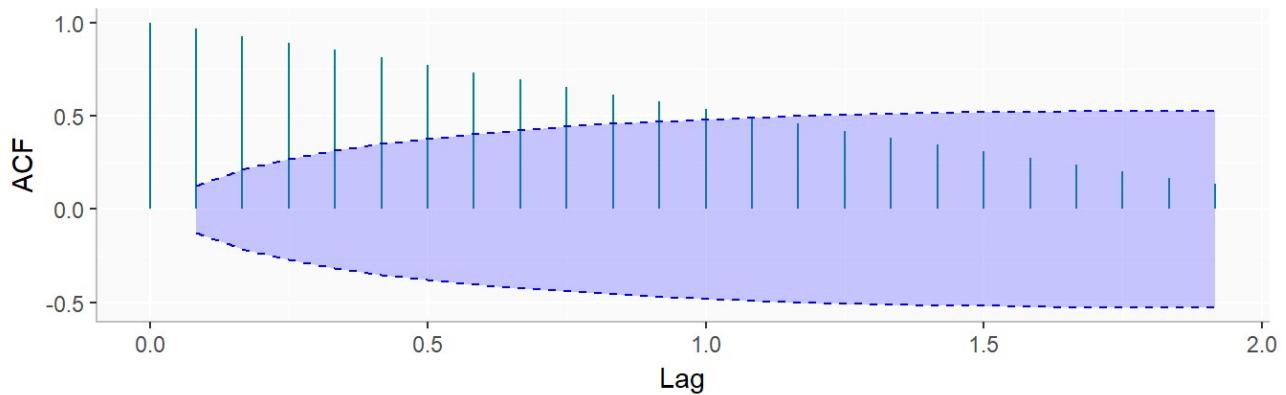




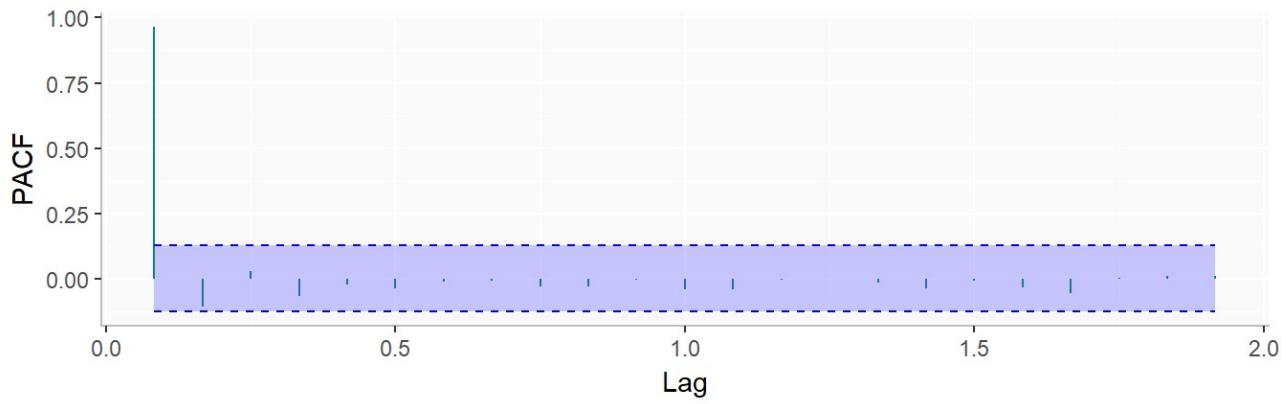
```
# DIAGNOSING ACF AND PACF PLOTS
plot_acf_pacf(sp500_TR, 'S&P 500')
```

```
## Warning: package 'bindrcpp' was built under R version 3.3.3
```

ACF plot of S&P 500



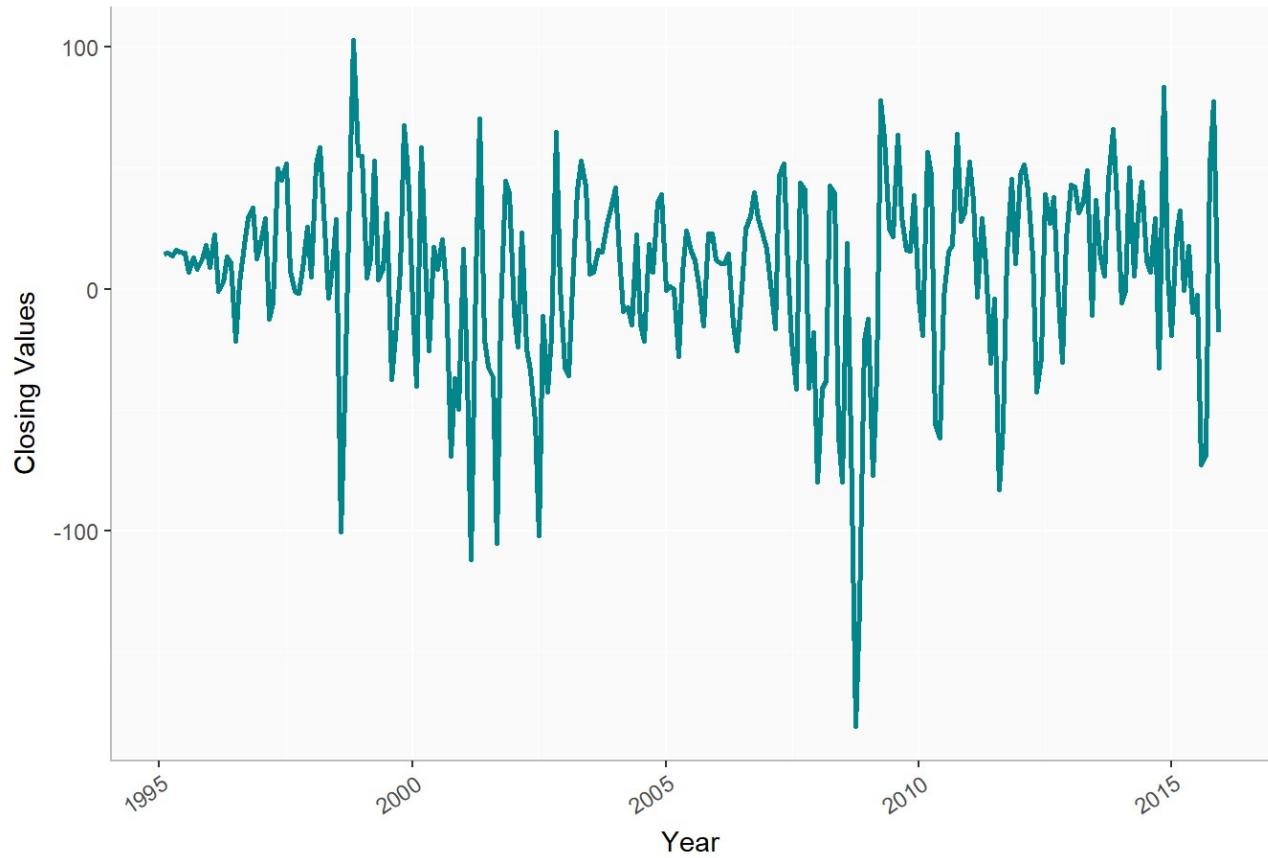
PACF plot of S&P 500



```
# TRANSFORMING OUR DATA TO ADJUST FOR NON STATIONARY
diff <- diff(sp_500)

tsDiff <- plot_time_series(diff, 'First Difference')
tsDiff
```

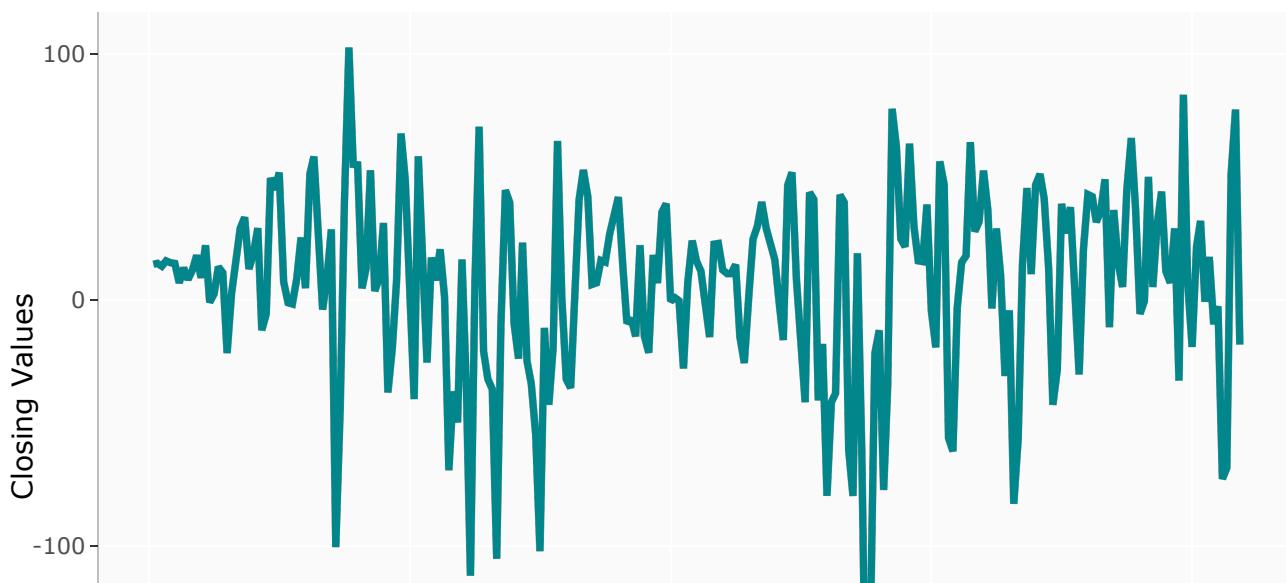
Plot of First Difference Time Series (1995 - 2015)

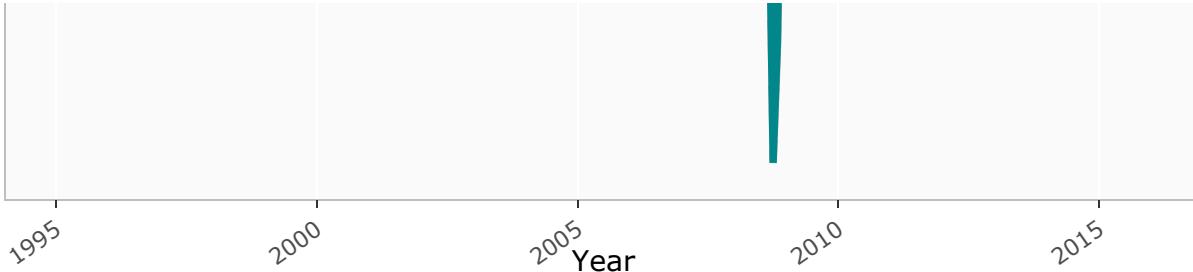


```
ggplotly(tsDiff)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Plot of First Difference Time Series (1995 - 2015)





```
# TESTS FOR STATIONARITY FOR DIFFERENCED TIME SERIES OBJECT  
Box.test(diff, lag = 20, type = 'Ljung-Box')
```

```
##  
## Box-Ljung test  
##  
## data: diff  
## X-squared = 58.2, df = 20, p-value = 1.347e-05
```

```
adf.test(diff)
```

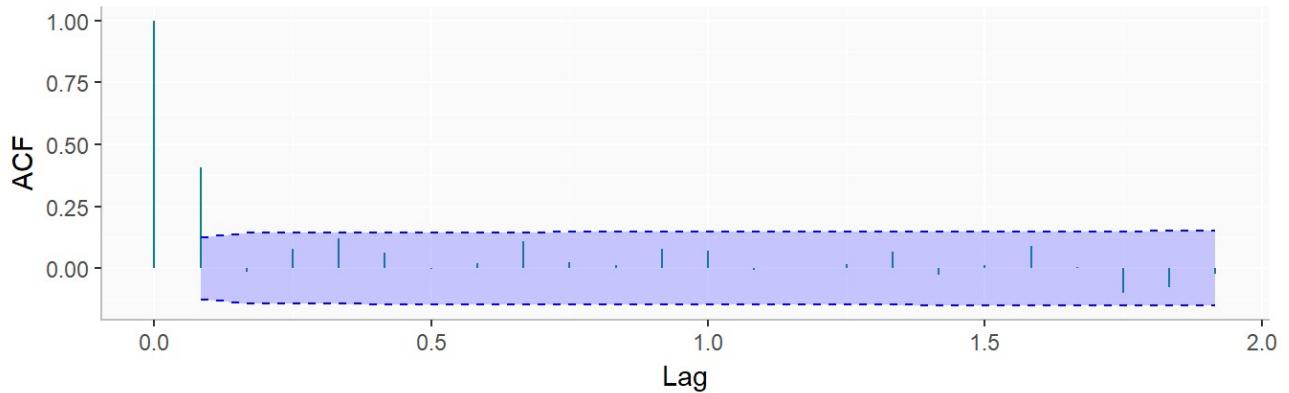
```
## Warning in adf.test(diff): p-value smaller than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: diff  
## Dickey-Fuller = -4.9552, Lag order = 6, p-value = 0.01  
## alternative hypothesis: stationary
```

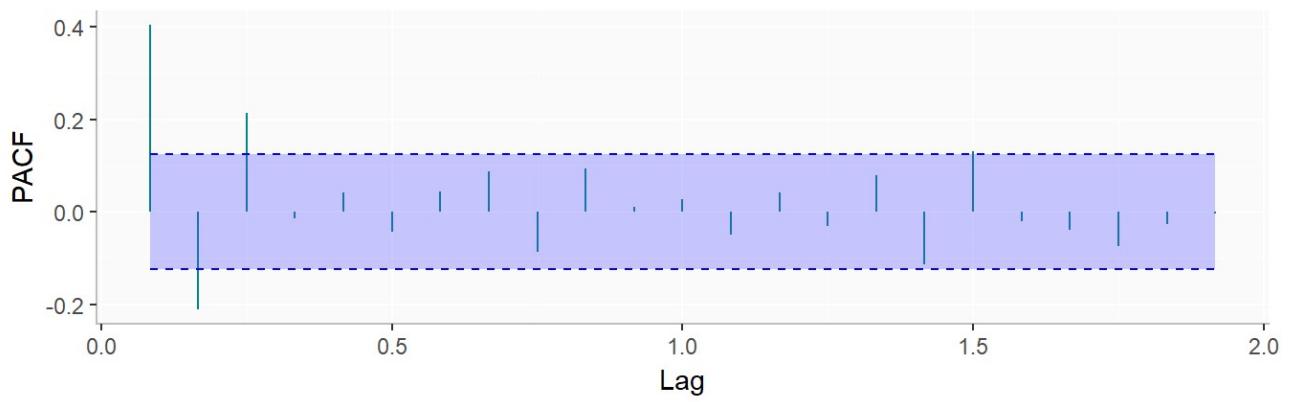
```
# p-values seems small enough to infer stationarity for the first difference  
# Let's begin analysis with visually inspecting ACF and PACF plots
```

```
# DIAGNOSING ACF AND PACF PLOTS FOR DIFFERENCED TIME SERIES OBJECT  
plot_acf_pacf(diff, 'First Difference Time Series Object')
```

ACF plot of First Difference Time Series Object

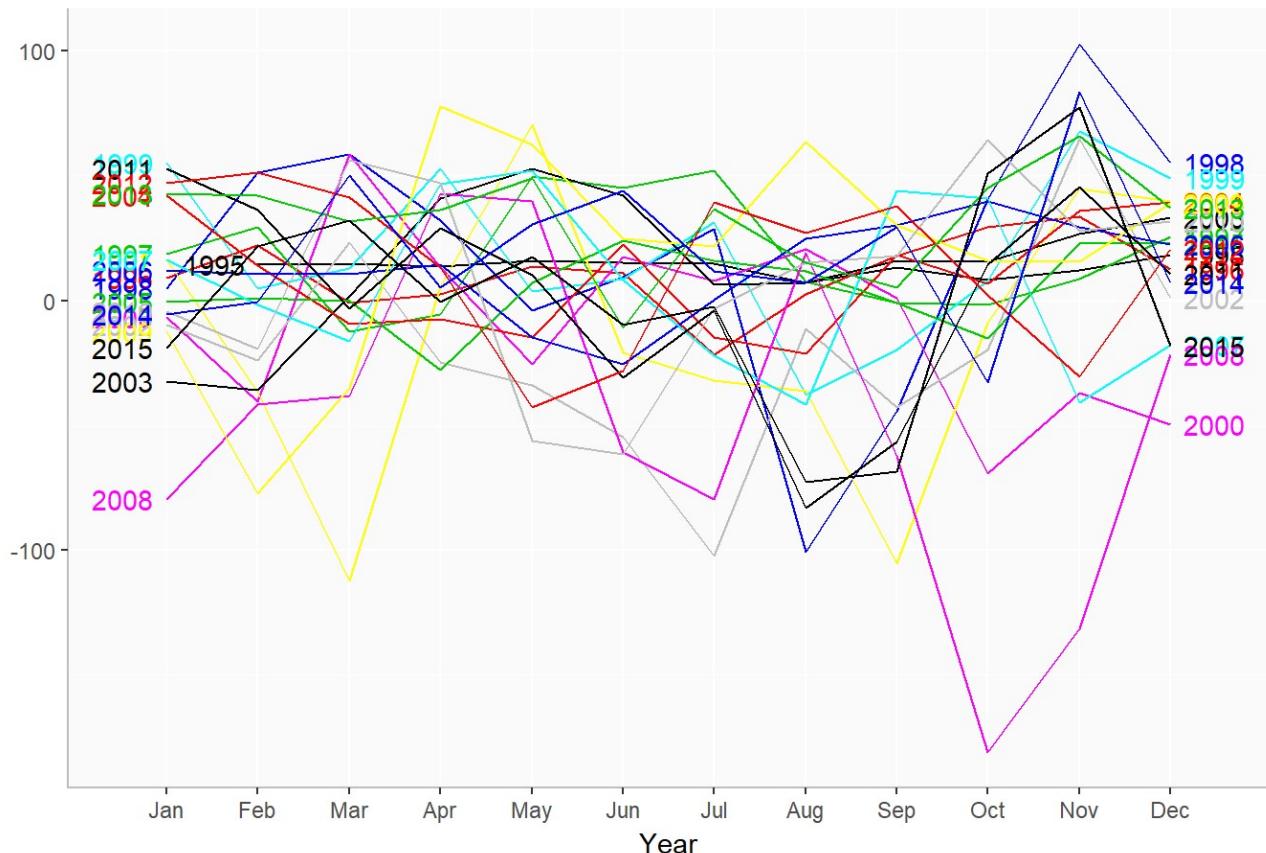


PACF plot of First Difference Time Series Object



```
# SEASONAL PLOT FOR DIFFERENCED TIME SERIES OBJECT
spDiff <- plot_seasonal(diff, 'First Difference Time Series Object')
spDiff
```

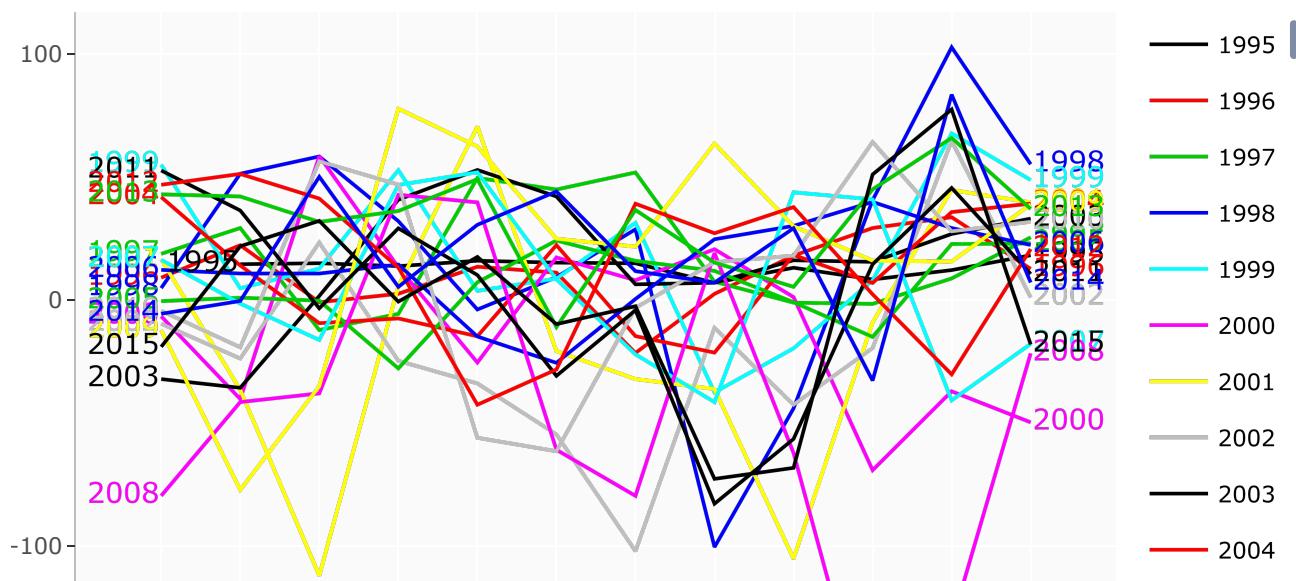
Seasonal Plot of First Difference Time Series Object

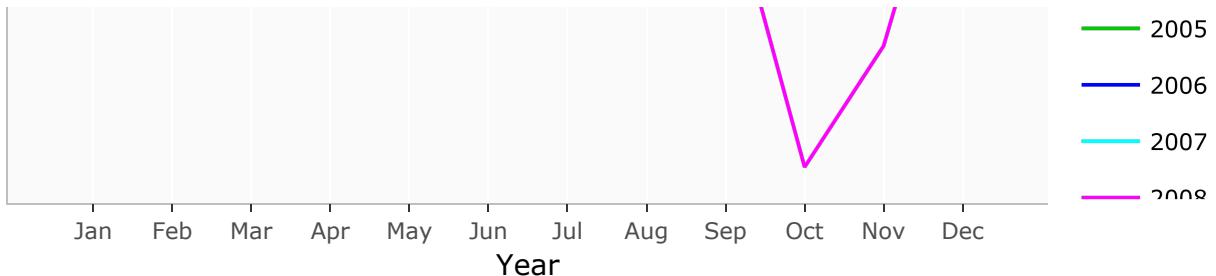


```
ggplotly(spDiff)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Seasonal Plot of First Difference Time Series Object





```
# AUTO.ARIMA ESTIMATION
auto.arima(sp500_TR)
```

```
## Series: sp500_TR
## ARIMA(0,1,1) with drift
##
## Coefficients:
##         ma1   drift
##       0.5666  6.4975
## s.e.  0.0551  3.4326
##
## sigma^2 estimated as 1161:  log likelihood=-1181.58
## AIC=2369.17  AICc=2369.27  BIC=2379.59
```

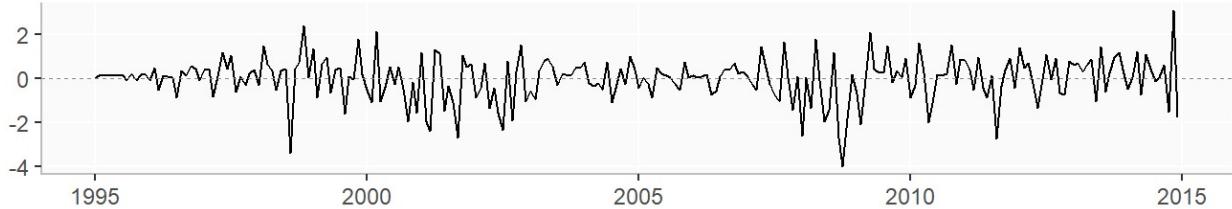
*# From our visual inspection and auto.arima model we will choose an
ARIMA(0, 1, 1) with drift*

```
# BUILD MODEL
fit <- Arima(sp500_TR, order = c(0,1,1), include.drift = TRUE)
summary(fit)
```

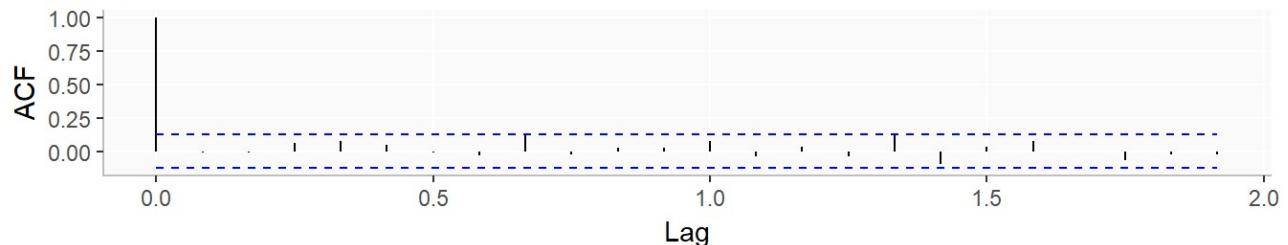
```
## Series: sp500_TR
## ARIMA(0,1,1) with drift
##
## Coefficients:
##         ma1   drift
##       0.5666  6.4975
## s.e.  0.0551  3.4326
##
## sigma^2 estimated as 1161:  log likelihood=-1181.58
## AIC=2369.17  AICc=2369.27  BIC=2379.59
##
## Training set error measures:
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.00911296 33.85289 24.84955 -0.00840343 2.141218 0.1310854
##                   ACF1
## Training set -0.01137429
```

```
# RESIDUAL DIAGNOSTICS
ggtsdiag(fit) +
  theme(panel.background = element_rect(fill = "gray98"),
        panel.grid.minor = element_blank(),
        axis.line.y = element_line(colour="gray"),
        axis.line.x = element_line(colour="gray"))
```

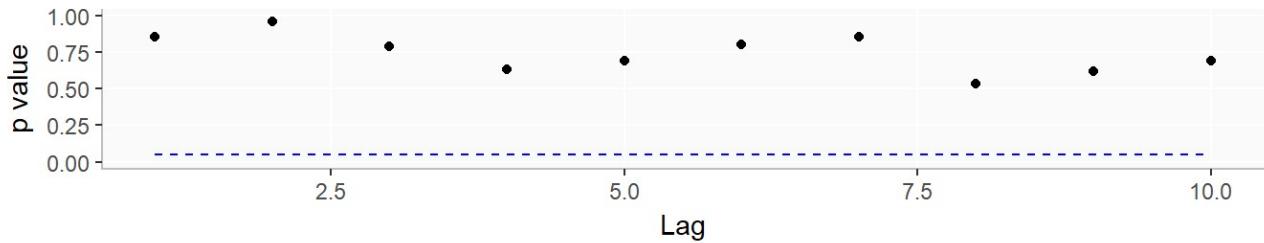
Standardized Residuals



ACF of Residuals



p values for Ljung-Box statistic

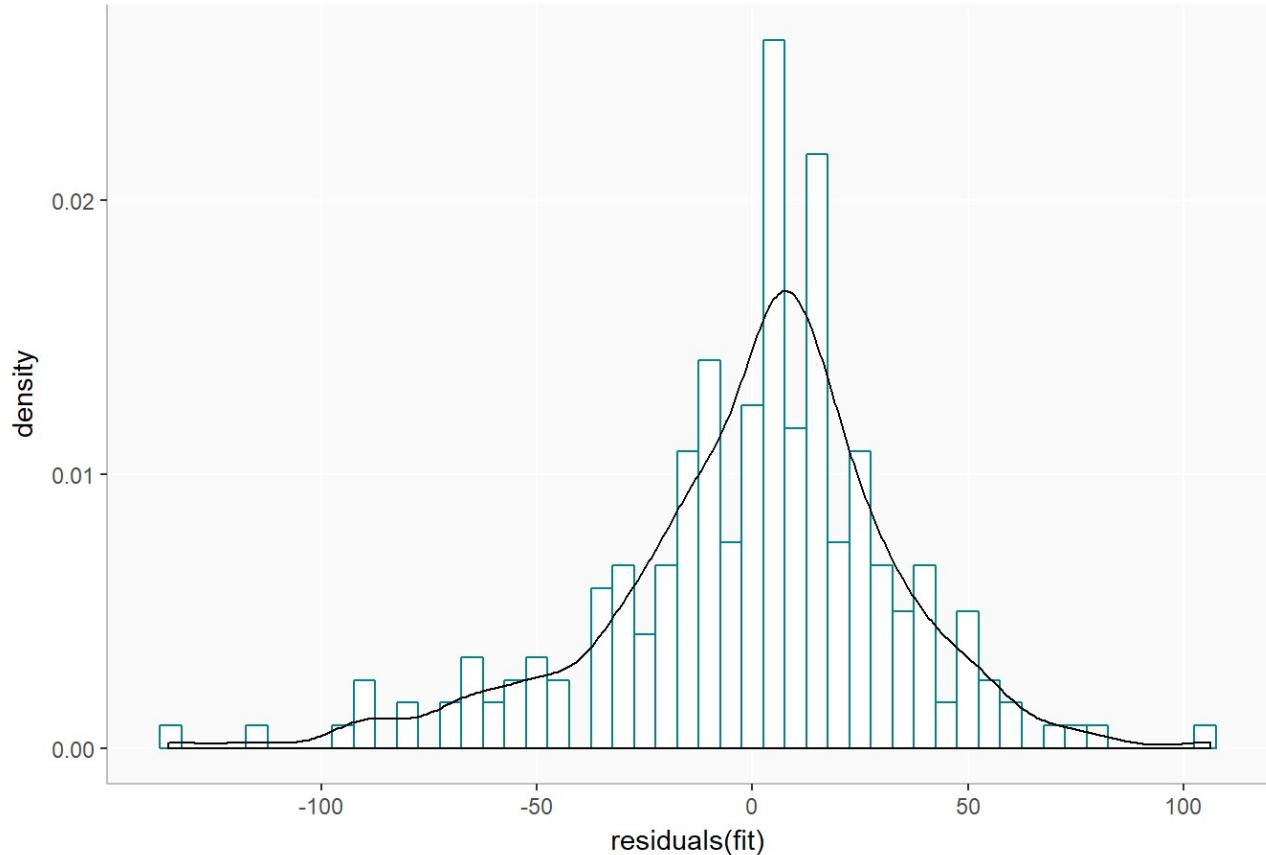


```
residFit <- ggplot(data=fit, aes(residuals(fit))) +
  geom_histogram(aes(y = ..density..),
                 binwidth = 5,
                 col="turquoise4", fill="white") +
  geom_density(col=1) +
  theme(panel.background = element_rect(fill = "gray98"),
        panel.grid.minor = element_blank(),
        axis.line = element_line(colour="gray"),
        axis.line.x = element_line(colour="gray")) +
  ggtitle("Plot of SP 500 ARIMA Model Residuals")
```

```
residFit
```

```
## Don't know how to automatically pick scale for object of type ts. Defaulting to continuous.
```

Plot of SP 500 ARIMA Model Residuals



```
# TEST SET THAT WE WILL COMPARE OUR FORECAST AGAINST
dataMaster_TS <- dataMaster[-c(1:240), ]
act_sp500_2015_ts <- ts(dataMaster_TS$sp_500, start = c(2015, 1), freq = 12)
act_sp500_2015_ts
```

```
##          Jan       Feb       Mar       Apr       May       Jun       Jul
## 2015 2028.592 2050.415 2082.582 2081.860 2099.355 2089.485 2086.920
##          Aug       Sep       Oct       Nov       Dec
## 2015 2014.085 1945.723 1996.758 2074.260 2056.100
```

```
print ("STEP 2.2: Forcasting.")
```

```
## [1] "STEP 2.2: Forcasting."
```

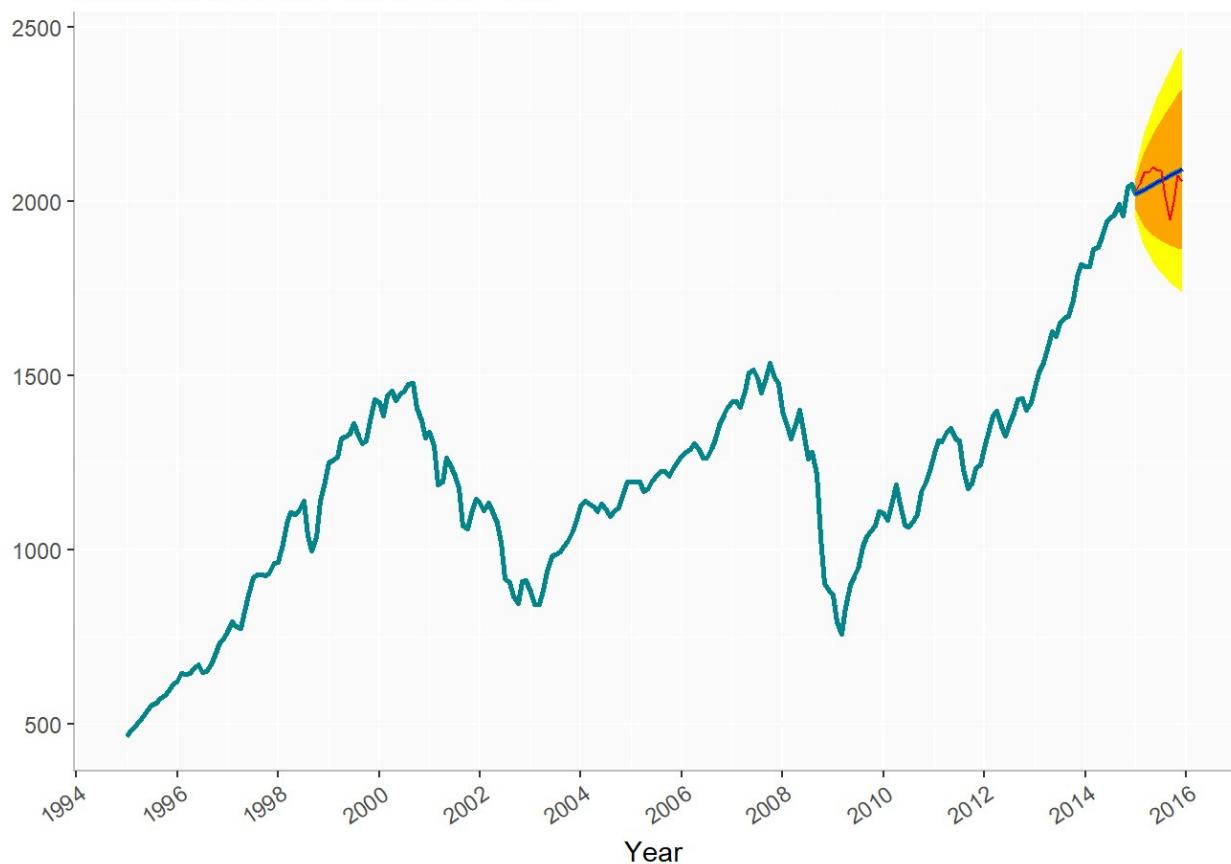
```

# FORECASTING
# METHOD CHOSEN THROUGH BOX JENKINS METHODOLOGY WAS ARIMA(0,1,1) WITH DRIFT
## ARIMA MODEL CHOSEN
fit_arima <- forecast(fit, h = 12)
forSp500 <- autoplot(fit_arima,
                      holdout = act_sp500_2015_ts,
                      ts_object_name = 'ARIMA')

forSp500

```

ARIMA Forecast Plot of S&P 500



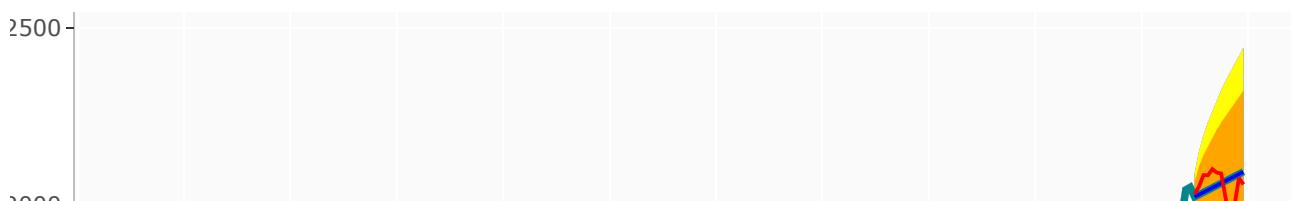
```
ggplotly(forSp500)
```

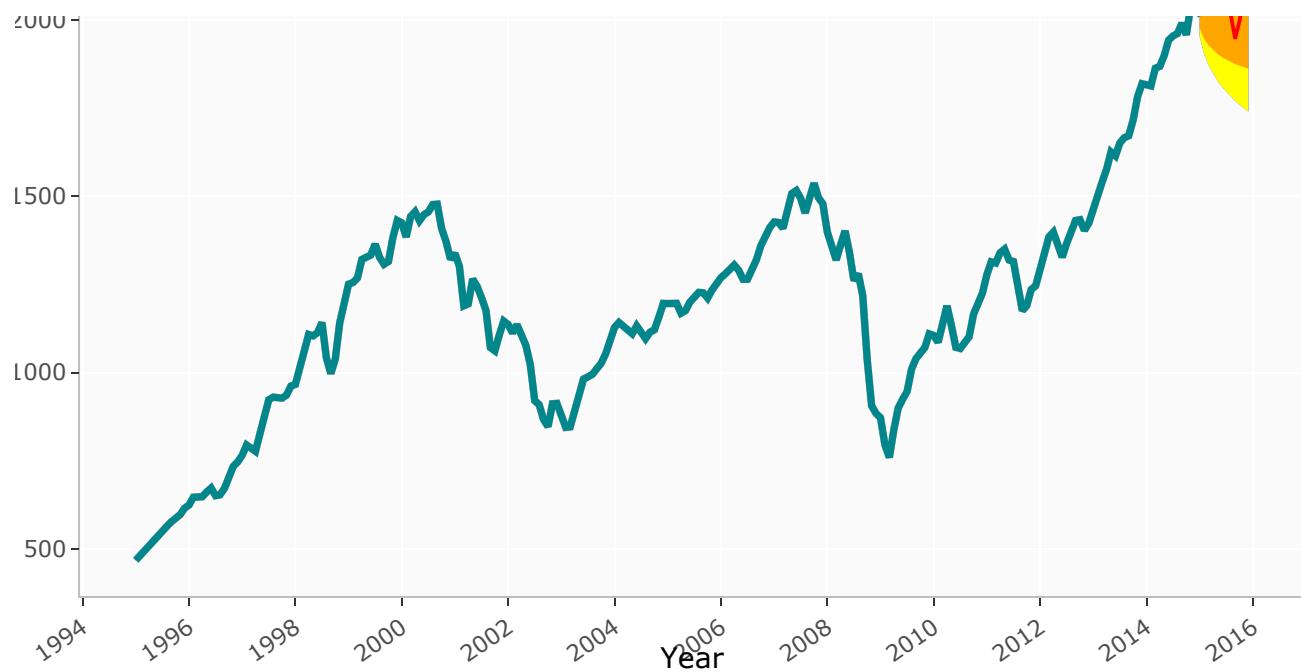
```

## We recommend that you use the dev version of ggplot2 with `ggplotly()`
## Install it with: `devtools::install_github('hadley/ggplot2')`

```

ARIMA Forecast Plot of S&P 500

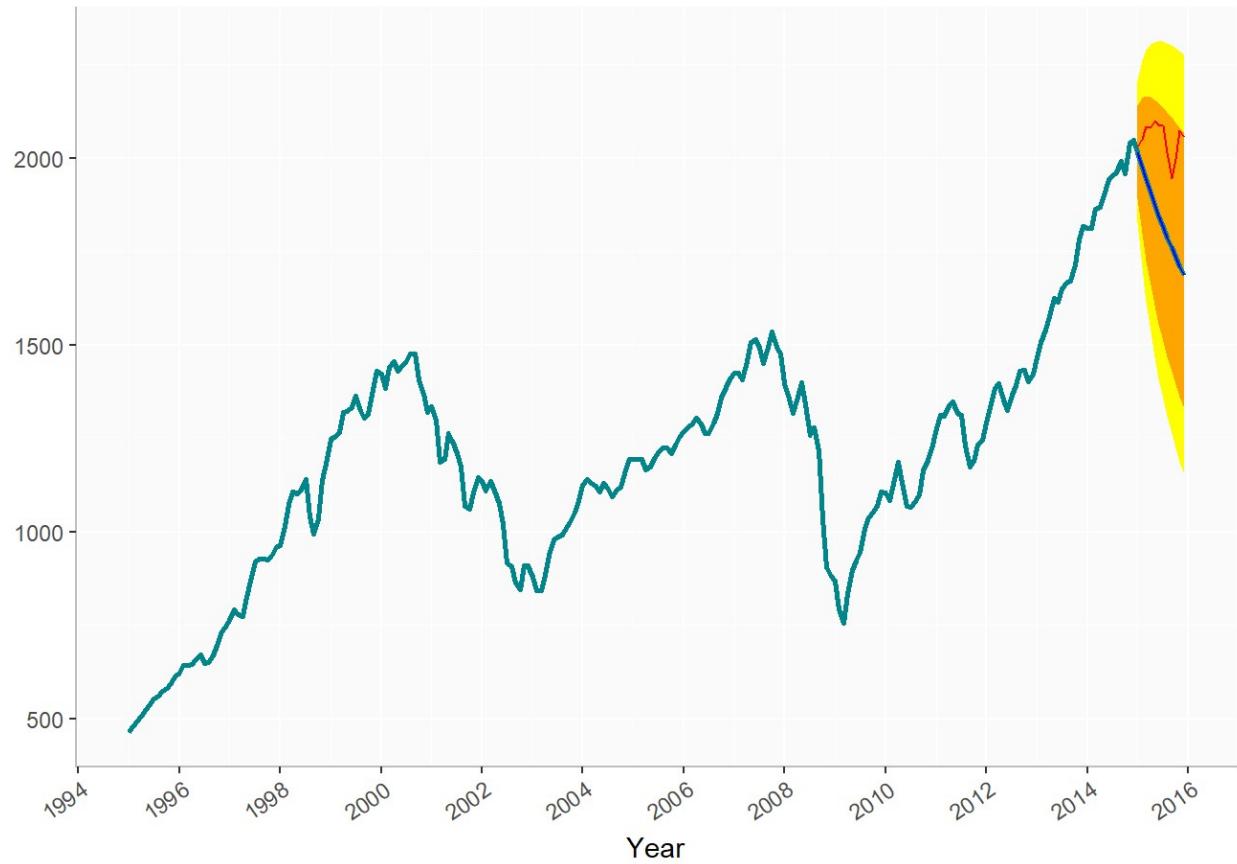




```
## BOX COX TRANSFORMATION
lambda <- BoxCox.lambda(sp500_TS)
fit_sp500_BC <- ar(BoxCox(sp500_TS,lambda))
fit_BC <- forecast(fit_sp500_BC,h=12,lambda=lambda)

s <- autoplot(fit_BC,
              holdout = act_sp500_2015_ts,
              ts_object_name = 'Box-Cox Transformation')
s
```

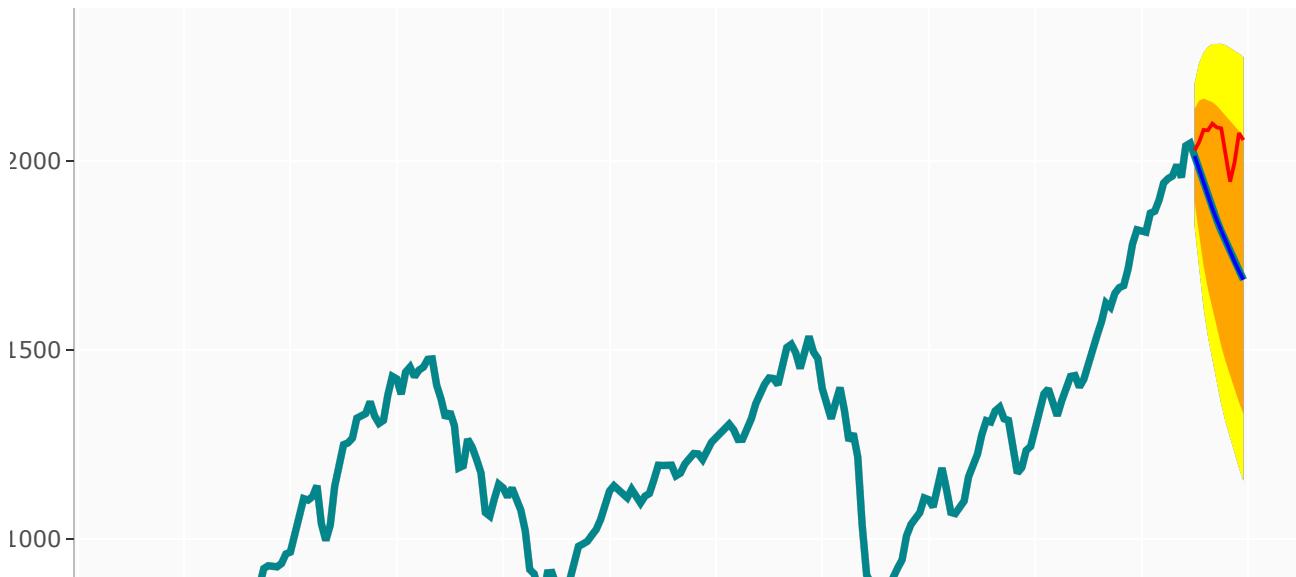
Box-Cox Transformation Forecast Plot of S&P 500

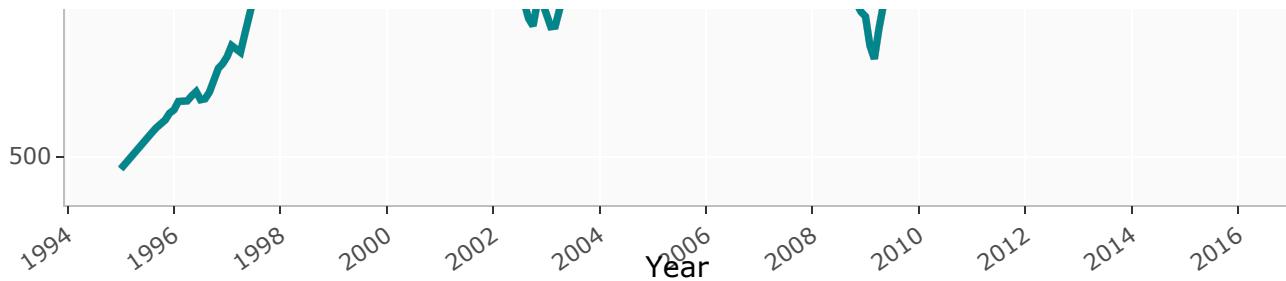


```
ggplotly(s)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

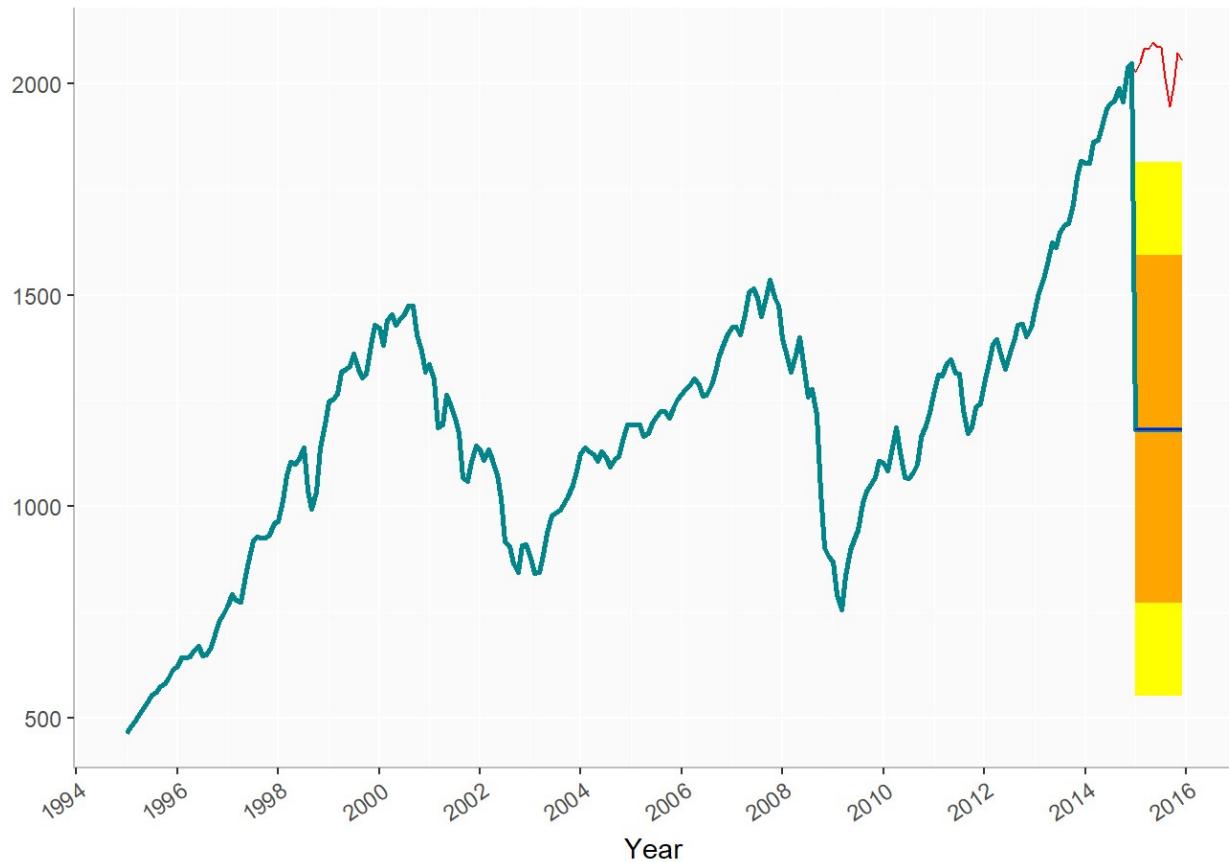
Box-Cox Transformation Forecast Plot of S&P 500





```
# MEAN FORECAST METHOD
fit_meanf <- forecast(meanf(sp500_TS, h = 12))
e <- autoplot(fit_meanf,
              holdout = act_sp500_2015_ts,
              ts_object_name = 'Mean Forecast')
e
```

Mean Forecast Forecast Plot of S&P 500



```
ggplotly(e)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Mean Forecast Forecast Plot of S&P 500



```
# NAIVE METHOD
fit_naive <- forecast(naive(sp500_TS, h = 12))
f <- autoplot(fit_naive,
              holdout = act_sp500_2015_ts,
              ts_object_name = "Naive Forecast")
f
```

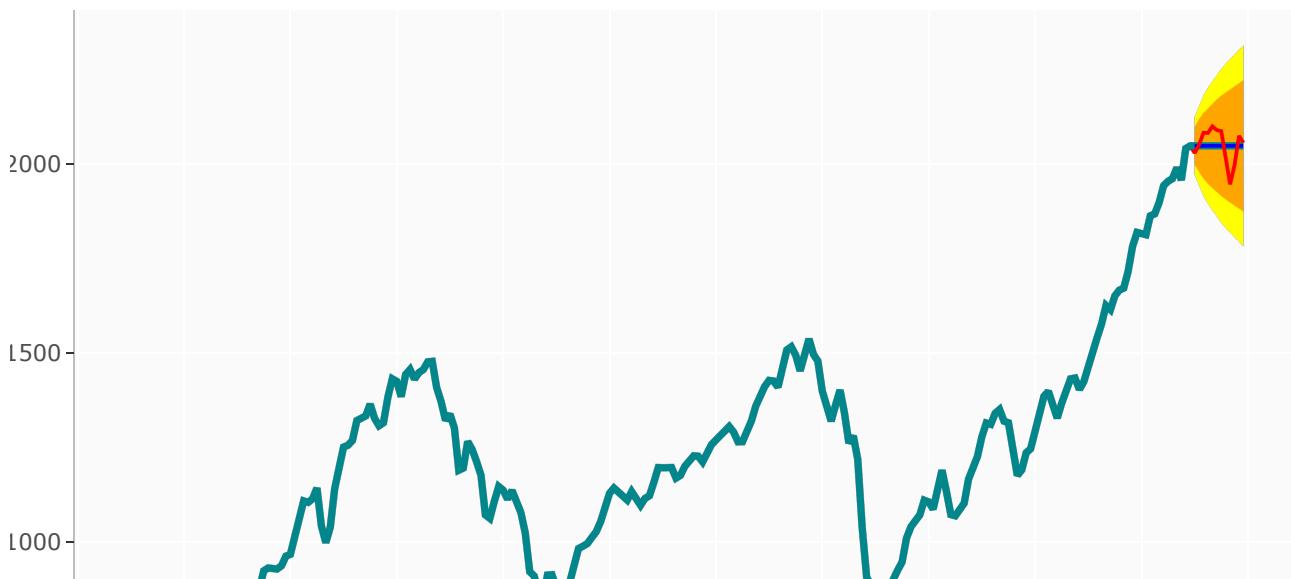
Naive Forecast Forecast Plot of S&P 500

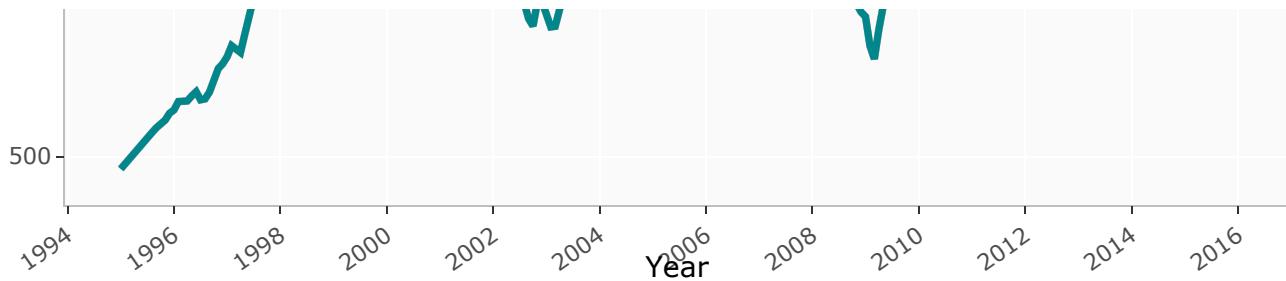


```
ggplotly(f)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Naive Forecast Forecast Plot of S&P 500





```
# SEASONAL NAIVE METHOD
fit_snaive <- forecast(snaive(sp500_TS, h = 12))
g <- autoplot(fit_snaive,
              holdout = act_sp500_2015_ts,
              ts_object_name = "Seasonal Naive")
g
```

Seasonal Naive Forecast Plot of S&P 500

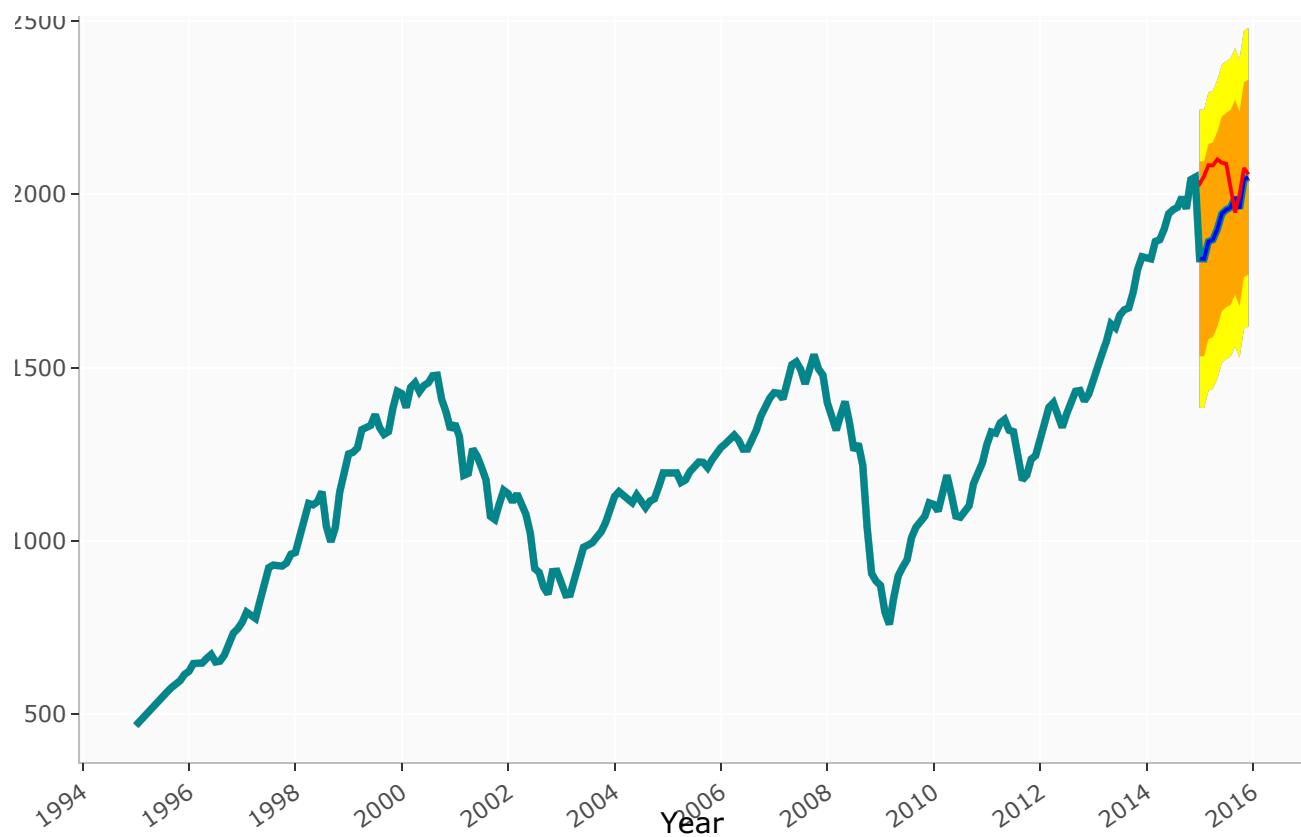


```
ggplotly(g)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Seasonal Naive Forecast Plot of S&P 500

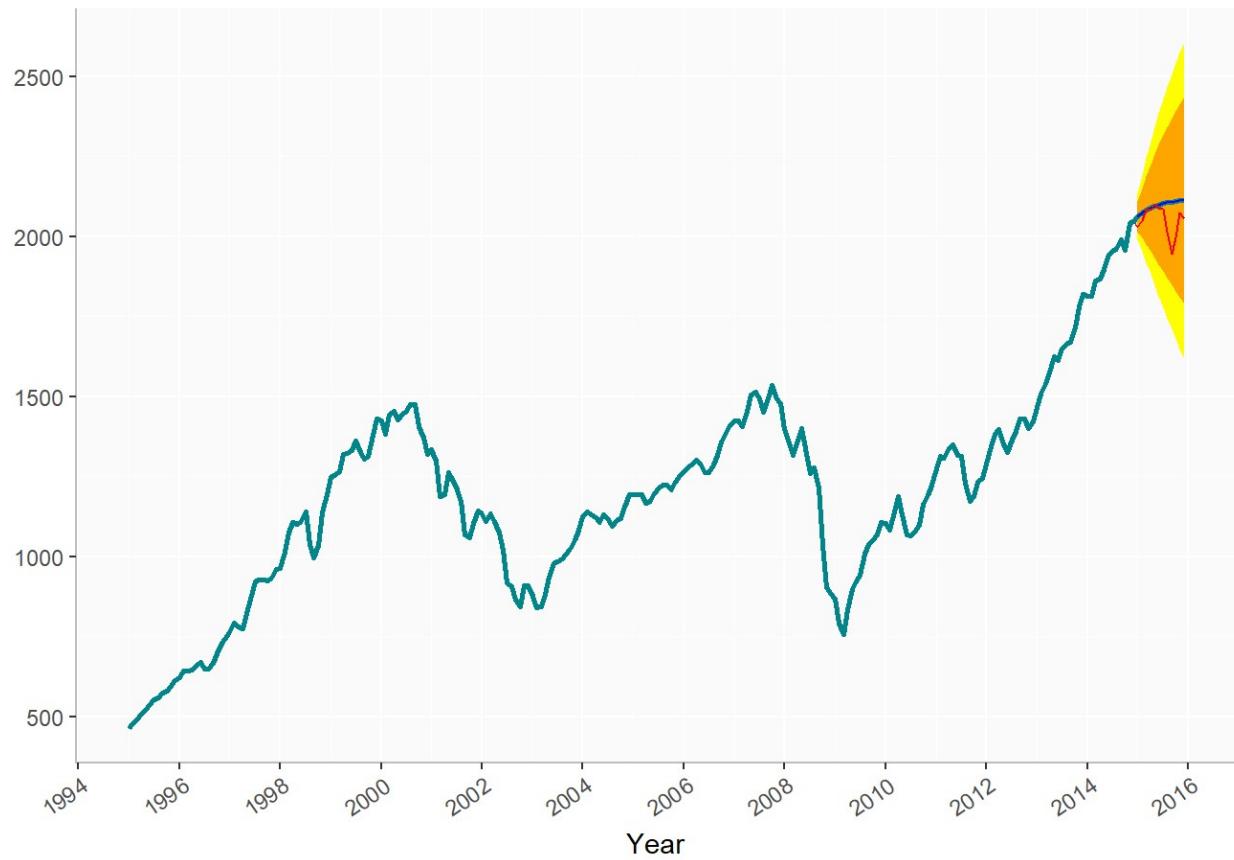
... |



```
# EXPONENTIAL SMOOTHING METHOD
fit_ets <- forecast(ets(sp500_TS), h = 12)
h <- autoplot(fit_ets,
              holdout=act_sp500_2015_ts,
              ts_object_name = "Exponential Smoothing")
```

```
h
```

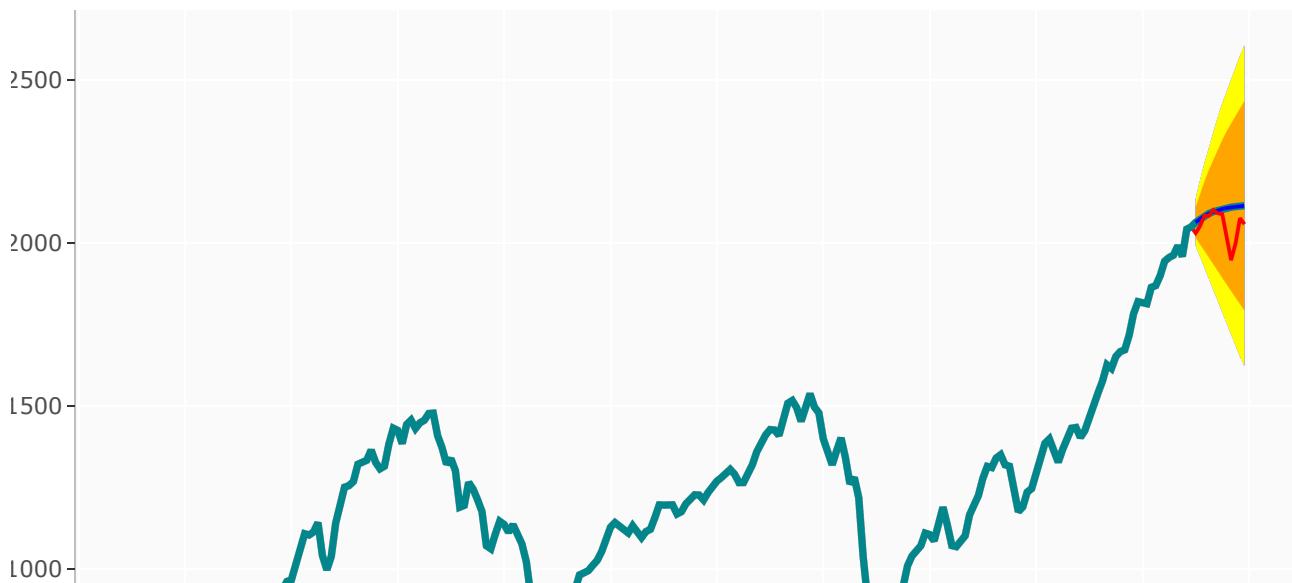
Exponential Smoothing Forecast Plot of S&P 500

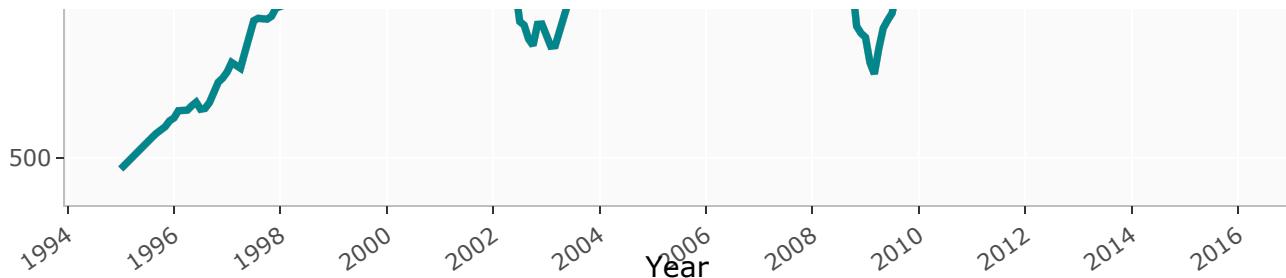


```
ggplotly(h)
```

```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Exponential Smoothing Forecast Plot of S&P 500





```
# COMPARE FORECAST ACCURACIES ACROSS DIFFERENT METHODS USED
accuracy(fit_arima)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.00911296 33.85289 24.84955 -0.00840343 2.141218 0.1310854
##                         ACF1
## Training set -0.01137429
```

```
accuracy(fit_BC)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 6.808873 39.28348 30.16598 0.282006 2.567669 0.1591304
##                         ACF1
## Training set 0.4091459
```

```
accuracy(fit_meanf)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -9.668655e-15 319.3598 244.9373 -9.110565 24.74398 1.292084
##                         ACF1
## Training set 0.9666459
```

```
accuracy(fit_naive)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 6.624059 39.30052 30.14866 0.5581768 2.66548 0.1590391
##                         ACF1
## Training set 0.4170651
```

```
accuracy(fit_snaive)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 73.06769 219.6302 189.5676 4.738094 16.6731      1 0.9647997
```

```
accuracy(fit_ets)
```

```

##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 2.648054 36.65711 27.74495 0.2519063 2.409392 0.1463591
##               ACF1
## Training set 0.1592457

```

```

# CONCLUSIONS
# The model with the best diagnostics is our ARIMA Model

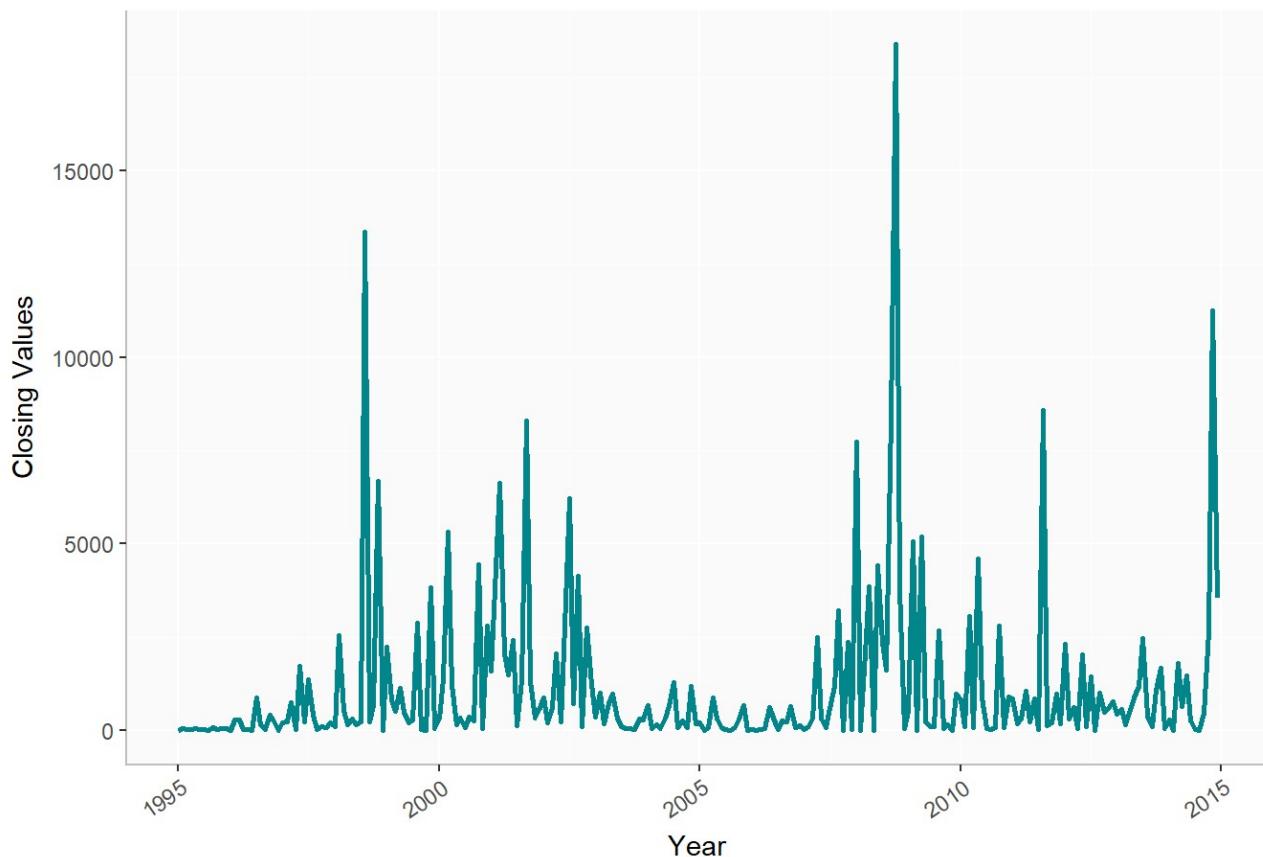
# ARCH Modeling
# Here we first square the residuals and plot the time series/ACF/PACF
# to see if there is correlation within the residuals.
# If there is we can continue adding on to our ARIMA model with a gARCH
# aspect that helps in the volatility of our data.
squared_res_fit <- fit$residuals^2

sq_res <- plot_time_series(squared_res_fit, "Squared Residuals")

sq_res

```

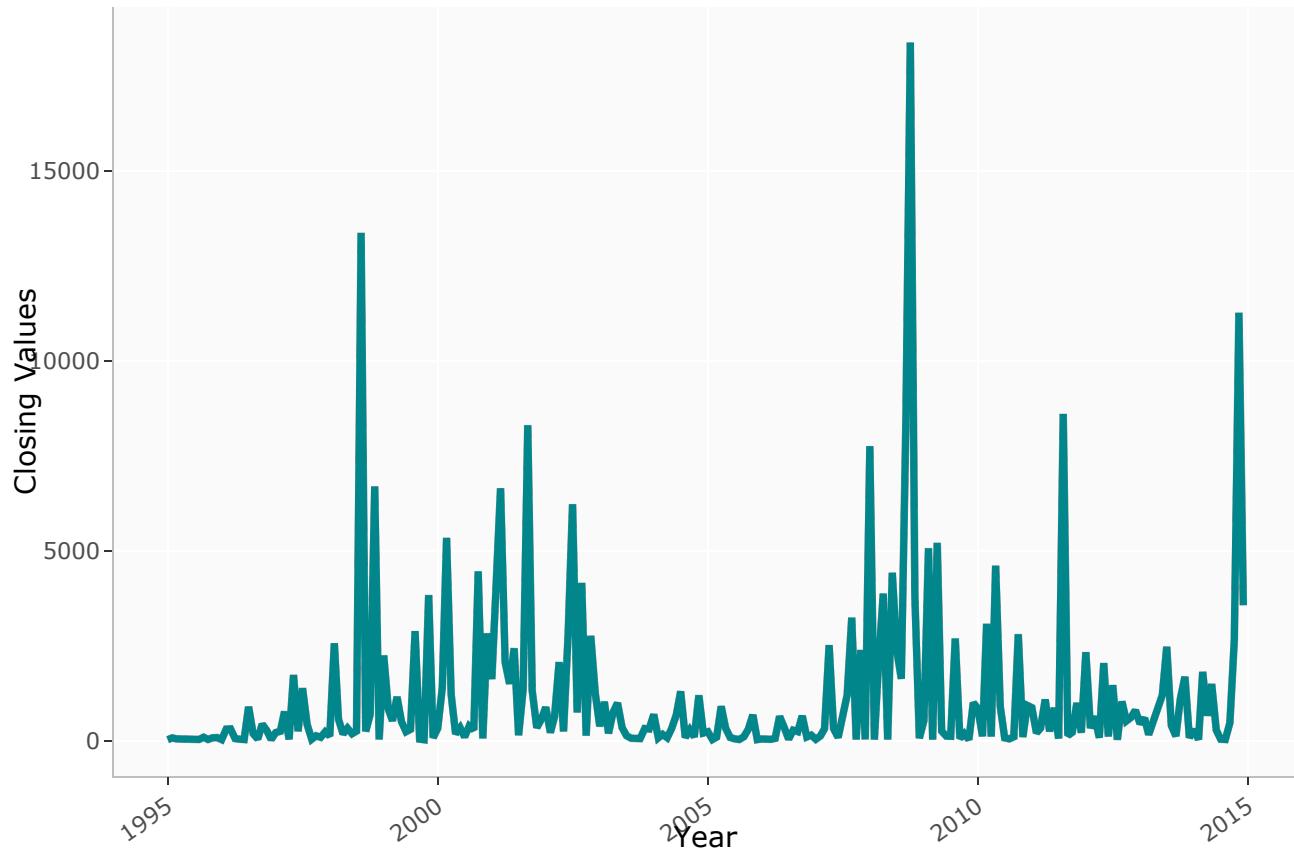
Plot of Squared Residuals Time Series (1995 - 2014)



```
ggplotly(sq_res)
```

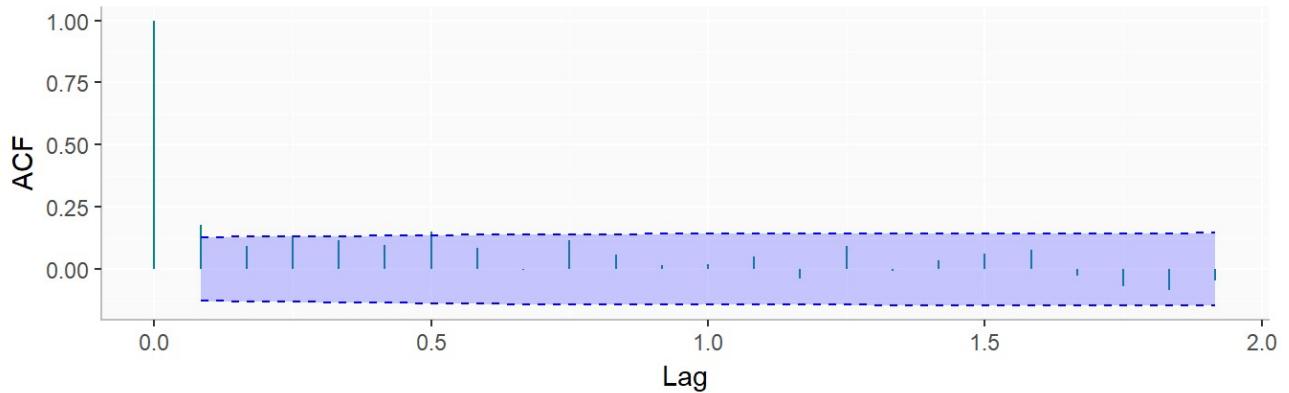
```
## We recommend that you use the dev version of ggplot2 with `ggplotly()`  
## Install it with: `devtools::install_github('hadley/ggplot2')`
```

Plot of Squared Residuals Time Series (1995 - 2014)

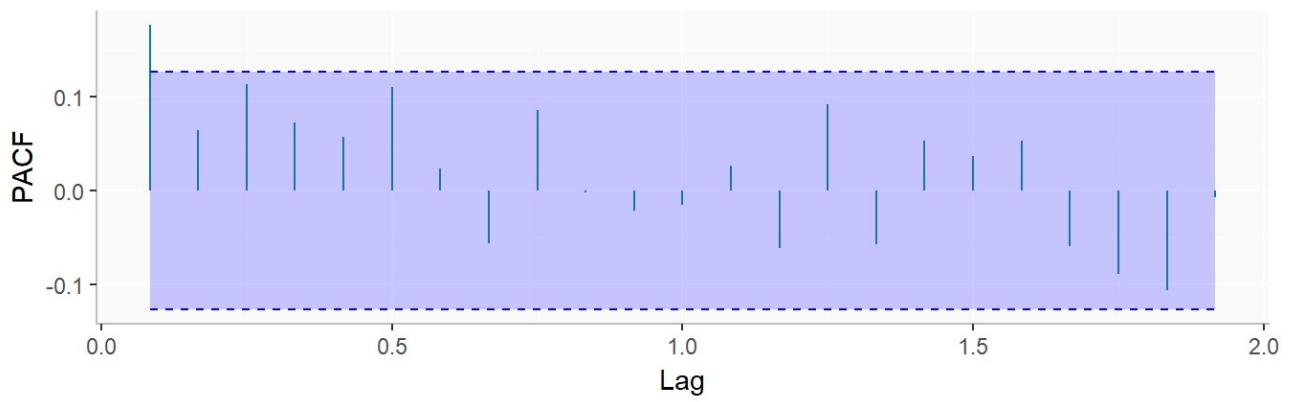


```
# ACF AND PACF PLOT FOR SQUARED RESIDUALS  
plot_acf_pacf(squared_res_fit, 'S&P 500 Residuals^2')
```

ACF plot of S&P 500 Residuals^{^2}



PACF plot of S&P 500 Residuals^{^2}



```
# The acf plot shows one significant lag, as does the pacf,  
# but that isn't enough to suggest we need GARCH modeling  
gfit <- garch(fit$residuals, order = c(1,1), trace = TRUE)
```

```

##  

## ***** ESTIMATION WITH ANALYTICAL GRADIENT *****  

##  

##  

##      I      INITIAL X(I)          D(I)  

##  

##      1      1.035732e+03      1.000e+00  

##      2      5.000000e-02      1.000e+00  

##      3      5.000000e-02      1.000e+00  

##  

##      IT      NF      F          RELDF      PRELDF      RELDX      STPPAR      D*STEP      NPRELDF  

##      0      1      9.591e+02  

##      1      3      9.578e+02      1.28e-03      3.40e-03      4.8e-05      3.3e+02      1.0e-01      5.55e-01  

##      2      5      9.577e+02      8.70e-05      9.35e-05      4.8e-06      2.7e+01      1.0e-02      4.23e-02  

##      3      7      9.576e+02      1.26e-04      1.26e-04      9.6e-06      2.0e+00      2.0e-02      6.79e-04  

##      4      9      9.576e+02      1.83e-05      1.83e-05      1.9e-06      1.0e+01      4.0e-03      3.90e-04  

##      5      11     9.576e+02      3.00e-05      3.01e-05      3.8e-06      2.0e+00      8.0e-03      1.40e-04  

##      6      13     9.576e+02      4.99e-06      4.99e-06      7.4e-07      1.7e+01      1.6e-03      8.28e-05  

##      7      16     9.576e+02      9.64e-08      9.64e-08      1.5e-08      7.2e+02      3.2e-05      4.99e-05  

##      8      18     9.576e+02      1.92e-07      1.92e-07      3.0e-08      9.1e+01      6.4e-05      4.68e-05  

##      9      20     9.576e+02      3.83e-07      3.83e-07      5.9e-08      4.6e+01      1.3e-04      4.65e-05  

##      10     23     9.576e+02      7.64e-09      7.64e-09      1.2e-09      8.9e+03      2.6e-06      4.60e-05  

##      11     25     9.576e+02      1.53e-08      1.53e-08      2.4e-09      1.1e+03      5.1e-06      4.58e-05  

##      12     27     9.576e+02      3.06e-08      3.06e-08      4.7e-09      5.6e+02      1.0e-05      4.57e-05  

##      13     29     9.576e+02      6.11e-09      6.11e-09      9.4e-10      1.1e+04      2.0e-06      4.57e-05  

##      14     31     9.576e+02      1.22e-09      1.22e-09      1.9e-10      5.6e+04      4.1e-07      4.57e-05  

##      15     33     9.576e+02      2.44e-09      2.44e-09      3.8e-10      7.0e+03      8.2e-07      4.57e-05  

##      16     35     9.576e+02      4.89e-10      4.89e-10      7.6e-11      1.4e+05      1.6e-07      4.57e-05  

##      17     37     9.576e+02      9.77e-10      9.77e-10      1.5e-10      1.7e+04      3.3e-07      4.57e-05  

##      18     39     9.576e+02      1.95e-10      1.95e-10      3.0e-11      3.5e+05      6.6e-08      4.57e-05  

##      19     41     9.576e+02      3.91e-10      3.91e-10      6.0e-11      4.4e+04      1.3e-07      4.57e-05  

##      20     43     9.576e+02      7.82e-10      7.82e-10      1.2e-10      2.2e+04      2.6e-07      4.57e-05  

##      21     45     9.576e+02      1.56e-10      1.56e-10      2.4e-11      4.4e+05      5.2e-08      4.57e-05  

##      22     47     9.576e+02      3.13e-11      3.13e-11      4.8e-12      2.2e+06      1.0e-08      4.57e-05  

##      23     49     9.576e+02      6.25e-12      6.25e-12      9.7e-13      1.1e+07      2.1e-09      4.57e-05  

##      24     51     9.576e+02      1.25e-12      1.25e-12      1.9e-13      5.4e+07      4.2e-10      4.57e-05  

##      25     53     9.576e+02      2.50e-12      2.50e-12      3.9e-13      6.8e+06      8.4e-10      4.57e-05  

##      26     55     9.576e+02      5.00e-13      5.00e-13      7.7e-14      1.4e+08      1.7e-10      4.57e-05  

##      27     57     9.576e+02      1.00e-12      1.00e-12      1.5e-13      1.7e+07      3.4e-10      4.57e-05  

##      28     59     9.576e+02      2.00e-13      2.00e-13      3.1e-14      3.4e+08      6.7e-11      4.57e-05  

##      29     62     9.576e+02      1.60e-12      1.60e-12      2.5e-13      1.1e+07      5.4e-10      4.57e-05  

##      30     65     9.576e+02      3.30e-14      3.20e-14      5.0e-15      2.1e+09      1.1e-11      4.57e-05  

##      31     67     9.576e+02      6.36e-14      6.40e-14      9.9e-15      2.7e+08      2.1e-11      4.57e-05  

##      32     68     9.576e+02      -1.04e+07      1.28e-13      2.0e-14      5.3e+08      4.3e-11      4.57e-05  

##  

## ***** FALSE CONVERGENCE *****  

##  

##      FUNCTION      9.575700e+02      RELDX      1.980e-14  

##      FUNC. EVALS      68      GRAD. EVALS      32  

##      PRELDF      1.281e-13      NPRELDF      4.565e-05

```

```
##  
##      I      FINAL X(I)      D(I)      G(I)  
##  
##      1      1.035732e+03      1.000e+00      6.818e-03  
##      2      1.505576e-01      1.000e+00      -8.455e-01  
##      3      7.106407e-12      1.000e+00      2.728e+00
```

```
print ("end of script.")
```

```
## [1] "end of script."
```