

# Package ‘SADmoment’

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**Type** Package

**Title** Extrapolate SAD and calculate parameters of best fitting distribution for subareas with several others

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**Description** Extrapolation of SAD and finding parameters of the best fitting distribution for subareas from the study of moments across scales. Moments of fitting distributions across scales by only using their parameters across scales.

**Depends** copula, BB, stats4, VGAM, sads, bbmle, poilog, splines, BBmisc

**License** GPL (>= 2)

**LazyData** true

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SADmoment-package	<i>Extrapolate SAD and calculate parameters of best fitting distribution for subareas with several others</i>
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## Description

Extrapolate SAD and parameters of best fitting distribution for subareas.

## Details

It is implemented by the techniques developed in Alirezazadeh S. (2019) and Alirezazadeh et. al. (2018). The most important functions of the package LLfun and SAD\_Moment. The function SAD\_Moment(X,Y,Splist,ext.rate,dplot) asks for positions (X,Y) of individuals of species Splist in the area of existing sample, an extrapolation rate that is the proportion of area we are interested to extrapolate to by the sample area, and dplot that identify whether the user want to visualise the SAD of the extrapolated area and compare it with the sample data or not. If the dplot=T then after running the function provides the histogram for species abundances of the sample and a line which is the estimation of species abundances of the extrapolated area. Note that the function SAD\_Moment(X,Y,Splist,ext.rate,dplot) returns valuable information regarding the running time, information on the sample and also information regarding the extrapolated area. So, we suggest

to run it as: `name<-SAD_Moment(X,Y,Splist,ext.rate,dplot)`. Also, note that the length of X, Y and Splist must be the same. The function `LLfun(X,splist)`, where X is a data.frame consists of species names and their (X,Y) positions. And splist is the name of existing species in the sample. And by pressing return it requests the user to enter a value for sub-area size and then with respect to the Log-Likelihood, finds the best fitting distribution of data and returns its parameters, see Alirezazadeh et.al. (2018)

### Author(s)

Saeid Alirezazadeh

### References

Alirezazadeh, S., 2019, Improvement on Extrapolation of Species Abundance Distribution Across Scales from Moments Across Scales (Unpublished)

Saeid Alirezazadeh and Luís Borda-de-Água and Paulo Borges and Rosalina Gabriel and F. Miguel Dionisio and Henrique Miguel Pereira and Pedro Cardoso, 2018, Theoretical Approach for how Species Abundance Distributions Change Across Scales, 2018 13th APCA International Conference on Control and Soft Computing (CONTROLO), pp. 131-136.

### Examples

```
# Data from Barro Colorado Island (BCI) is used here for the example,
# within total 50 ha area all the individuals
# with at least 1cm (Diameter at Breast Height) (dbh) are considered.

SAD_Moment(dbci[,3],dbci[,4],dbci[,1],ext.rate=1.1,dplot=TRUE)

# In the following we used all the individuals
# with at least 10cm (Diameter at Breast Height) (dbh) from the BCI data.
#R> name<-SAD_Moment(X,Y,Spnames,ext.rate=1.2,dplot=FALSE)
#R> summary(name)
#           Length Class      Mode
#Data       6      -none-    list
#Initial    4      -none-    list
#Extrapolate 7      -none-    list
#Time       5      proc_time numeric
#R> summary(name$Initial)
#           Length Class      Mode
#Area        1      -none- numeric
#Moments     20      -none- numeric
#XY.Ratio     1      -none- numeric
#Number.of.bins 1      -none- numeric
#R> summary(name$Extrapolate)
#           Length Class      Mode
#Area        1      -none- numeric
#Moments     20      -none- numeric
#Number.of.bins 1      -none- numeric
#Coefficients.of.Tchebychev.Polynomials 49      -none- numeric
#Tchebychev.Polynomials.Values          98      -none- numeric
#Tchebychev.Moments.Values              7      -none- numeric
#Extrapolate.SAD                      12      -none- numeric
#R> summary(name$Time)
# user system elapsed
# 4.632 2.009 6.690
#R> print(name$Data$SAD)
```

```
# [1] 27 11 20 30 29 38 30 21 20 5 4 1
#R> print(name$Extrapolate$Extrapolate.SAD)
# [1] 32 13 15 24 31 33 30 24 17 10 5 2
#
#R> LLfun(X,Splist)
#Enter sub-area size: 9800
#      [,1]
#[1,] "For the sub-area ( 9800 ) the best fitting distribution is : Poisson Gamma"
#[2,] "alpha= 1.2089269105249 and beta= 1.2089269105249"
#R> LLfun(X,Y,Splist)
#Enter sub-area size: 200000
#      [,1]
#[1,] "For the sub-area ( 2e+05 ) the best fitting distribution is : Log-Normal"
#[2,] "mu= 3.51478121939837 and sigma= 2.2582385148143"
#
```

---

alffinder	<i>Parameter alpha in the fitting with a Gamma distribution</i>
-----------	---

---

### Description

Finds parameter alpha in the case of fitting with a Gamma distribution

### Usage

```
alffinder(res, slope, ro, c, z, A)
```

### Arguments

res	intercept of first moments across area
slope	slope of first moments across area
ro	slope of number of individuals across area
c	parameter c in the power-law species area relationship
z	parameter z in the power-law species area relationship
A	total area of consideration

---

BellB	<i>Bell function</i>
-------	----------------------

---

### Description

Returns the values of Bell function

### Usage

```
BellB(n, k, x)
```

### Arguments

n	total elements of the sets
k	number of partitions
x	specific element(s) of the set

---

bet.f	<i>bet.f</i>
-------	--------------

---

**Description**

returns beta(n,N) as a part of finding values of Tchebychev polynomials.

**Usage**

```
bet.f(n, N)
```

**Arguments**

n	order of polynomial
N	number of bins

---

betfinder	<i>Parameter beta in the fitting with a Gamma distribution</i>
-----------	--

---

**Description**

Finds parameter beta in the case of fitting with a Gamma distribution

**Usage**

```
betfinder(res, slope, ro, c, z, A)
```

**Arguments**

res	slope of first moments across area
slope	slope of first moments across area
ro	slope of number of individuals across area
c	parameter c in the power-law species area relationship
z	parameter z in the power-law species area relationship
A	total area of consideration

---

calcalpha	<i>Logseries parameter</i>
-----------	----------------------------

---

**Description**

Finds the parameter alpha in the case of fitting with a log-series distribution

**Usage**

```
calcalpha(n.orig, s.orig)
```

**Arguments**

n.orig	number of individuals
s.orig	number of species

---

cmoment	<i>moment calculator, first step in the Log-Normal, values need to be transformed</i>
---------	---

---

**Description**

First step for calculating moments of log-normal, will be used in another function for transformation.

**Usage**

```
cmoment(mu, sig, k)
```

**Arguments**

mu	the parameter mu in the log-normal
sig	the parameter sigma in the log-normal
k	maximum order of moments

---

cmul	<i>symbolic constant multiplication</i>
------	---

---

**Description**

symbolic multiplication with a constant

**Usage**

```
cmul(u, c)
```

**Arguments**

u	matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients
c	a constant

---

Coef.Tcheb.pol.2nd	<i>Coefficients of the Tchebychev polynomials up to a certain degree</i>
--------------------	--

---

**Description**

Coefficients of the Tchebychev polynomials up to a certain degree as a matrix

**Usage**

Coef.Tcheb.pol.2nd(N, no.m)

**Arguments**

N	Number of bins
no.m	maximum order of polynomials

---

data_read	<i>get values from keyboard for future use.</i>
-----------	---

---

**Description**

Take a value from keyboard for future use. It is a part of LLfun which is to find the best fitting distribution for a smaller sub-areas.

**Usage**

data\_read()

---

datfun	<i>average number of species and individuals</i>
--------	--

---

**Description**

Returns average number of species and individuals in a given sub-area, by randomly sampling that sub-area size from the total area.

**Usage**

datfun(df, x, spp, n, ratio)

**Arguments**

df	data frame, name of species, position over X and Y axis
x	sub-section size over Y axis
spp	list of all species
n	number of random sampling
ratio	ratio of X by Y

---

dbfact	<i>double factorial</i>
--------	-------------------------

---

**Description**

Finds the value of double factorial value.

**Usage**

```
dbfact(i)
```

**Arguments**

i	an integer
---	------------

---

Dist_Moment	<i>Moments of the most common fitting distributions</i>
-------------	---

---

**Description**

Returns the moments up to degree 20 of the fitting distribution of data across scales.

**Usage**

```
Dist_Moment(xpos, ypos, splist, DIST = "LS")
```

**Arguments**

xpos	position of individuals of species by X-axis
ypos	position of individuals of species by Y-axis
splist	Respective name of the species in the position (X,Y)
DIST	The fitting distribution under consideration ("LS", "LN", "PG", "PLN")

---

expnd	<i>symbolic expansion</i>
-------	---------------------------

---

**Description**

expand symbolic polynomials to higher degree

**Usage**

```
expnd(u, n)
```

**Arguments**

u	matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients
n	numeric value that we need to expand the polynomial.



---

extpfun	<i>extrapolation of moments across scales</i>
---------	---

---

**Description**

extrapolate moments.

**Usage**

```
extpfun(dat, m)
```

**Arguments**

dat	list of values (the list must have almost linear pattern).
m	the corresponding numeric index in the list that we try to extrapolate to.

---

extrapolation.dist	<i>extrapolate distribution moments across scales</i>
--------------------	---

---

**Description**

Returns the values of extrapolations of moments of different orders of the distribution moments

**Usage**

```
extrapolation.dist(momraw, momdist, ext.rate, momr)
```

**Arguments**

momraw	raw moments values
momdist	distribution moments values
ext.rate	extrapolation rate.
momr	values of extrapolation of raw moments to that rate.

---

extrapolation.raw	<i>extrapolate raw moments across scales</i>
-------------------	--

---

### Description

Returns the values of extrapolations of moments of different orders of the raw moments

### Usage

```
extrapolation.raw(momraw, ratio, ba, bba)
```

### Arguments

momraw	values of raw moments
ratio	the ration of x by y.
ba	total area we try to extrapolate to.
bba	total area that we have informations.

---

f	<i>individuals in a given positions</i>
---	---

---

### Description

Lista of individuals exist in a given sub-area.

### Usage

```
f(df, xcoor, ycoor, x, ratio)
```

### Arguments

df	data frame, name of species, position over X and Y axis
xcoor	initial X-coordinate inside total area
ycoor	initial Y-coordinate inside total area
x	sub-section size over Y axis
ratio	ratio of X by Y

---

fg	<i>list of number individuals of all species</i>
----	--

---

**Description**

Returns the abundances of species of interest from a given list of individuals.

**Usage**

```
fg(g, sppnames)
```

**Arguments**

g	list of all individuals in a sub-area
sppnames	list of all species

---

fo	<i>fo</i>
----	-----------

---

**Description**

used as part of method to evaluate the parameter of log-series across scales

**Usage**

```
fo(a, n, s)
```

**Arguments**

a	area
n	number of individual
s	number of species

---

fprime	<i>first derivative of funtion fo, as a part of the function calculate the parameter of log-series</i>
--------	--

---

**Description**

first derivative of the fo function used for the Newton's method to find the parameter of log-series

**Usage**

```
fprime(a, n, s)
```

**Arguments**

a	area
n	numero of individuals
s	number of species

---

LLfun	<i>Parameters of the best fitting distribution</i>
-------	--

---

**Description**

Returns the parameters of the best fitting distribution with respect to the log-likelihoods.

**Usage**

```
LLfun(Y, spp)
```

**Arguments**

Y	A matrix consists of x,y and species names respect all individuals in the community
spp	list of all species in the community

---

LNmom	<i>Moments of log-normal</i>
-------	------------------------------

---

**Description**

Returns moments up to degree k of the log-normal distribution.

**Usage**

```
LNmom(mu, sig, k)
```

**Arguments**

mu	mu value in the log-normal distribution
sig	sigma value in the log-normal distribution
k	the order of moment.

---

LSmom	<i>Moments of the log-series distribution.</i>
-------	--

---

**Description**

Returns moments up to degree k of the log-normal distribution.

**Usage**

```
LSmom(x, n)
```

**Arguments**

x	the parameter of log-series
n	order of moment

---

M1	<i>M1, theoretical average</i>
----	--------------------------------

---

**Description**

Returns average number of individuals (Theoretical)

**Usage**

```
M1(ro, c, z, A)
```

**Arguments**

ro	parameter ro in $N=ro \cdot A$
c	parameter c in $S=c \cdot A^z$
z	parameter z in $S=c \cdot A^z$
A	area or scale

---

manage_data	<i>data across scales, number of individuals of species across scales</i>
-------------	---

---

**Description**

returns number of individuals of all species and number of species across scales.

**Usage**

```
manage_data(df, spp, n, x, ratio)
```

**Arguments**

df	data frame, name of species, position over X and Y axis
spp	list of all species
n	number of random sampling over Y axis
x	sub-section size over Y axis
ratio	ratio of X by Y

---

mmoment	<i>first step for finding moment of Poisson-Gamma, the values needed to be transformed</i>
---------	--

---

### Description

the values from this function is used as the first step to calculate the moments of Poisson-Gamma distribution and need to be transformed

### Usage

```
mmoment(al, bet, k)
```

### Arguments

al	parameter alpha in the gamma distribution
bet	parameter beta in the gamma distribution
k	maximum order of moments

---

mo2nd	<i>2nd moment across scales</i>
-------	---------------------------------

---

### Description

consider the linear pattern for the 2nd moment across scales.

### Usage

```
mo2nd(res, slope, A)
```

### Arguments

res	residual of second moment across scales
slope	slope of second moment across scales
A	area or scale

---

moment1	<i>moment of log-series number of individuals are not log-transformed</i>
---------	---

---

### Description

return moments of different orders of log-series but in the case where the number of individuals are not log-transformed

### Usage

```
moment1(x, n)
```

### Arguments

x	parameter of log-series
n	maximum moment order

---

momfun	<i>raw, distribution, and linear moments</i>
--------	--

---

### Description

all moments are calculated here. linear moments is when we do not log transform the number of individuals.

### Usage

```
momfun(df, x, spp, n, no.m, ratio)
```

### Arguments

df	data frame consists of name of species together with positions over X and Y axis
x	subsection size over Y axis
spp	list of all species
n	number of randomize sampling in the total area
no.m	maximum order of moments
ratio	ratio of X by Y

---

mufinderLN	<i>mean finder for the Log-Normal</i>
------------	---------------------------------------

---

**Description**

find the parameter mu in a log-normal

**Usage**

```
mufinderLN(res, slope, A)
```

**Arguments**

res	residual of the first raw moment across scales
slope	slope of the first raw moment across scales
A	area or scale

---

---

mufinderPLN	<i>mean finder for the Poisson log-normal</i>
-------------	---

---

**Description**

returns the parameter of mu in the Poisson log-normal.

**Usage**

```
mufinderPLN(res, slope, A)
```

**Arguments**

res	residual of the first moment across scales
slope	slope of the first moment across scales
A	area or scale

---

---

numsum	<i>weighted sum</i>
--------	---------------------

---

**Description**

Calculate the weighted sum for given weight and a list

**Usage**

```
numsum(n, x, k)
```

**Arguments**

n	maximum degree
x	a numeric parameter
k	a numeric value for the weight



---

PGmom	<i>Moments of the Poisson Gamma</i>
-------	-------------------------------------

---

**Description**

Returns moments up to degree k of the Poisson Gamma distribution.

**Usage**

```
PGmom(al, bet, k)
```

**Arguments**

al	parameter alpha of poisson gamma distribution
bet	parameter beta of poisson gamma distribution
k	order of moment

---

PLNmom	<i>Moments of the Poisson log-normal distribution.</i>
--------	--

---

**Description**

Returns moments up to degree k of the Poisson log-normal distribution.

**Usage**

```
PLNmom(mu, sig, k)
```

**Arguments**

mu	parameter mu of the distribution
sig	parameter sigma of the distribution
k	order of moment

---

provide_info	<i>provide some info</i>
--------------	--------------------------

---

**Description**

inside function to print some information from LLfun function.

**Usage**

```
provide_info(L)
```

**Arguments**

L	A list of information provided by the LLfun function.
---	---

---

ptransform	<i>polylog transformation</i>
------------	-------------------------------

---

**Description**

Polylog transformation used to calculate moments of log-series where number individuals are log transformed

**Usage**

```
ptransform(x, k)
```

**Arguments**

x	parameter for log series
k	integer as degree of the polylog function to expand to.

---

r.mom	<i>raw moments</i>
-------	--------------------

---

**Description**

calculate raw moments

**Usage**

```
r.mom(dat, no.m)
```

**Arguments**

dat	data list of number of individuals of species
no.m	maximum order of moments

---

relpwave	<i>wave function</i>
----------	----------------------

---

**Description**

fit wave function and use it for extrapolation

**Usage**

```
relpwave(l, t, ba)
```

**Arguments**

l	list of values that is considered to be wave
t	the larger scale we need to extrapolate to
ba	area or scale

---

ro.c.z	<i>parameter finder</i>
--------	-------------------------

---

**Description**

returns theoretical parameter ro, c, and z in  $N=ro A$  and  $S=cA^z$

**Usage**

```
ro.c.z(No.Sp, No.Id, bba)
```

**Arguments**

No.Sp	number of species across scales
No.Id	number of individuals across scales
bba	area or scales

---

SAD_Moment	<i>Extrapolate Species Abundance Distribution</i>
------------	---

---

**Description**

Extrapolates SAD by extrapolating of moments.

**Usage**

```
SAD_Moment(xpos = NULL, ypos = NULL, splist = NULL, ext.rate = 1, dplot = T)
```

**Arguments**

xpos	List of position of individuals over X-axis
ypos	List of position of individuals over Y-axis
splist	Name of species where its individual is in place (X,Y)
ext.rate	extrapolation rate( $\geq 1$ )
dplot	Values (T or F) respectively to inform whether the plot of the extrapolation should appears or not.

---

shrt	<i>Symbolic shortenning</i>
------	-----------------------------

---

### Description

Shorten a polynomial with symbolic calculation

### Usage

shrt(u)

### Arguments

u                      matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients

---

sigfinderLN	<i>standard deviation finder for Log Normal across scales</i>
-------------	---

---

### Description

returns the parameter sigma in the Log-normal Distribution.

### Usage

sigfinderLN(res, slope, ro, c, z, A)

### Arguments

res                      residual for the change of the first raw moments across scales  
slope                      slope of the change of the first raw moments across scales  
ro                          the parameter ro in the formula  $N=ro \cdot A$ , number of individuals across scales  
c                           the parameter c in  $S=cA^z$   
z                           the parameter z in  $S=cA^z$   
A                           area or scale

---

sigfinderPLN	<i>standard deviation finder for Poisson Log Normal across scales</i>
--------------	---

---

**Description**

returns the parameter sigma in a Poisson log-normal.

**Usage**

```
sigfinderPLN(res1, slope1, res2, slope2, A)
```

**Arguments**

res1	residual for the change of means across scales
slope1	slope of the change of means across scales
res2	residual for the change of moments of second order across scales
slope2	slope of the change of moments of second order across scales
A	area or scale

---

smom	<i>Log-normal moments</i>
------	---------------------------

---

**Description**

moments of log-normal of different orders are calculate here

**Usage**

```
smom(mu, sig, k)
```

**Arguments**

mu	mean
sig	standard deviation
k	maximum order of moment

---

st2k	<i>Sterling number of second kind</i>
------	---------------------------------------

---

**Description**

Returns the Sterling number of second kind

**Usage**

st2k(n, k)

**Arguments**

n	number of elements of the set
k	number of partitions of the set

---

summ	<i>symbolic addition</i>
------	--------------------------

---

**Description**

Adding polynomials symbolically

**Usage**

summ(u1, u2)

**Arguments**

u1	matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients
u2	matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients

---

Tcheb.pol.2nd	<i>Values of Tchebychev polynomials up to certain degree at each bin.</i>
---------------	---

---

**Description**

Returns values of the Tchebychev polynomials up to a certain degree and by considering a certain number of bins.

**Usage**

Tcheb.pol.2nd(N, no.m)

**Arguments**

N	number of bins
no.m	maximum order of polynomials

---

tn	<i>Thebychev polynomials recursive formula</i>
----	--

---

**Description**

calculate recursively the Tchebychev polynomials up to given degree and in different bins

**Usage**

tn(n, N)

**Arguments**

n	maximum degree of polynomial
N	maximum number of bins

---

xmul	<i>symbolic multiplication</i>
------	--------------------------------

---

**Description**

Returns the symbolic multiplications of a polynomial by its variable

**Usage**

xmul(u)

**Arguments**

u	matrix with two rows and second row consists of 1 to number of columns (represent powers) and first row is the coefficients
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