

KNAPSACK

$$(H, P, V, M) \begin{cases} 0 & \text{se } H < 0 \text{ o } M < 0 \\ \text{MAX } (V_1, V_2) & \text{se } H > 0 \text{ e } M > 0 \end{cases}$$

$$\rightarrow \text{MAX} = K + \text{MaxValue}((V-K), M - w_K)$$

$$0 \leq K \leq M-1$$

ROD-CUT

$$r_m = \begin{cases} 0 & \text{se } m = 0 \\ r_m = \max_{0 \leq k \leq m} \{P[k] + r_{m-k}\} & \text{se } m \geq 1 \end{cases}$$

MATRIX-CHAIN

$$m[i, j] = \begin{cases} 0 & \text{se } i = j \\ \min_{i < k < j} (m[i, k] + m[k+1, j] + P[i-1]P[k]P[j]) & \text{se } i < j \end{cases}$$

ACTIVITY-SELECTION

$$C[i, j] = \begin{cases} 0 & \text{se } S_{i,j} = \emptyset \\ \text{MAX} \{C(i, k) + C(k+1, j) + 1\} & \end{cases}$$

LCS

$$C[i, j] = \begin{cases} 0 & \text{se } i = 0 \text{ o } j = 0 \\ C[i-1, j-1] + 1 & \text{se } i, j > 0 \text{ e } x_i = y_i \\ \text{MAX}(C[i-1, j], C[i, j-1]) & \text{se } i, j > 0 \text{ e } x_i \neq y_i \end{cases}$$

APSP

$$W = \begin{cases} 0 & \text{se } i=j \\ w(i,j) & \text{se } \exists (i,j) \in E \\ \infty & \text{se } \nexists (i,j) \in E \end{cases}$$

numero di archi usati

$$\downarrow$$

$$D^m[i,j] = \min_{1 \leq k \leq m} (D^{m-1}[i,k] + W[k,j])$$

FLOYD - WARSHALL

D^0 : MATRICE DI ADIACENZA

$$D^k[i,j] = \min_{1 \leq k \leq m} (D^{k-1}[i,j], D^{k-1}[i,k] + D^{k-1}[k,j])$$