$$f(t) = \begin{cases} 1/20J_{\pm} \exp(-J_{0}) & \text{fontso} \\ 0, & \text{fontso} \end{cases}$$

$$L(t; \theta) = \prod_{i=1}^{n} f(t_i; \theta)$$

$$= \prod_{i=1}^{n} \frac{1}{2\theta \sqrt{t_i}} exp(-\frac{\sqrt{t_i}}{\theta})$$

$$= \prod_{i=1}^{n} \frac{1}{2\theta \sqrt{t_i}} exp(-\frac{\sqrt{t_i}}{\theta})$$

Taking lug

$$L(t;\theta) = log \left(\frac{1}{1-1} \frac{1}{2\theta \sqrt{t}} exp - \frac{\sqrt{t}}{\theta} \right)$$

$$= log \left(\frac{\Sigma}{1-1} \frac{1}{2\theta \sqrt{t}} \right) - \frac{\Sigma}{1-2} \sqrt{t} \frac{1}{\theta}$$

$$= \frac{\Sigma}{1-2} \left(log(1) - log (20\sqrt{t}) \right) - \frac{\Sigma}{1-2} \sqrt{t} \frac{1}{\theta}$$

$$= -\frac{\Sigma}{1-2} log 20\sqrt{t} \frac{1}{1-2} - \frac{\Sigma}{1-2} \sqrt{t} \frac{1}{\theta}$$

$$= -\frac{\Sigma}{1-2} log 20 - \frac{\Sigma}{1-2} \sqrt{t} \frac{1}{\theta}$$

Differentiating w. 17. to. 0.

$$\frac{\partial L(t;\theta)}{\partial \theta} = \frac{\sqrt{2}}{\sqrt{2}\theta} - \sum_{i=1}^{\infty} \frac{1}{2\theta} \cdot 2 - 0 + \sum_{i=1}^{\infty} \frac{\sqrt{2}}{\theta^2}$$

$$= -\sum_{i=1}^{\infty} \frac{1}{\theta} + \sum_{i=1}^{\infty} \frac{\sqrt{2}}{\theta^2}$$

$$= -\frac{n}{\theta} + \sum_{i=1}^{\infty} \frac{\sqrt{2}}{\theta^2}$$

To find the MLE of 0, Q, we solve $-\frac{n}{0} + \frac{\sum_{i=1}^{n} J_{\pm i}}{0} = 0$

$$= \sum_{i=1}^{\infty} \sqrt{E_i} = 0$$

$$=) \quad \hat{\Theta}_{MLE} = \frac{1}{m} \sum_{i=1}^{m} \sqrt{E_i}$$

For Sample, t1, t2, t3, t4 4 t5.

$$= 2\sqrt{370}$$
.

Using method of moments,

here, = 11300 + 3000 + 4300 + 8500 + 7900

$$=$$
 7400
So, $6mom = \sqrt{\frac{7400}{2}} = 10\sqrt{37}$.