Exercise 2:

A statistics T = T(x) is sufficient statistics for θ if the conditional distribution of x given T is free of θ ; i.e. if the ratio

$$f_{xit}$$
 (xit) = $\frac{f_x(xi\theta)}{f_t(ti\theta)}$

is free of 0. for all xEX. In other words, after conditioning on T, we have removed all information about 0 from samplex.

The joint distribution of the n-order Statistics is

=
$$0.14^{\times}(x10)$$

for $-\infty < x_1 < x_2 < --- < x_n < \infty$. Therefore the natio

$$\frac{f_{x}(x|\theta)}{f_{T}(x|\theta)} = \frac{f_{x}(x|\theta)}{n! f_{x}(x|\theta)} = \frac{1}{n!}$$

Which is free of 0.

So, according to the defination of sufficiency: $T = T(x) = (X_1, X_2, ..., X_n)$ is a Sufficient statistic.

5/5