The probability mass function of the multinomial distribution is:

$$P(X_{1}=X_{2}, X_{2}=X_{2}, ..., X_{K}=X_{K}) = \frac{n_{1}}{x_{1}! x_{2}! ... x_{K}!} \times P_{1}^{X_{2}} \times P_{2}^{X_{2}} \times P_{K}^{X_{K}}$$
Here,
$$N = \sum_{i=1}^{K} X_{i}$$
and
$$\sum_{k=1}^{K} P_{i} = 1.$$
use unitarounal

The likelihood function is:

$$\left(\frac{3}{5}\right)^{\times} p^{2\xi}.$$

coefficient

Taking log-likelihood is given by

Log 
$$(P(x, y, z|p)) = log \left[ {x + y + z \choose x} \times (1-p)^{2x} \times {y + z \choose x} \times (2p(1-p))^{y} \times {y \choose z} \times p^{2z} \right]$$

= 
$$2n \log(1-P) + \log(\frac{x+y+z}{x}) + y \log(2P) + y \log(1-P) + \log(y+z) + 2z \log(P) + \log(\frac{z}{z})$$

Taking the derivative witht P

$$\frac{\partial (\log (P(x_1 \forall 1, 2|P)))}{\partial P} = -\frac{2x}{1-P} + \frac{y}{ZP} \cdot 2 - \frac{y}{1-P} + \frac{2z}{P}$$

$$= \frac{y}{1-P} - \frac{y}{1-P} = \frac{2z}{1-P}$$

Set the delivative equal to 0.

$$\frac{3+2\frac{2}{P}}{P} - \frac{y+2x}{1-P} = 0$$

$$\frac{y+2z-yp-2pz-yp-2xp}{P(1-P)} = 0$$

=) 
$$3+2z - P(2y+2x+2z) = 0$$
  
::  $P_{MLE} = \frac{y+2z}{2x+2z+2z}$ 

Taking 2nd devisive,

which is <0, because here x, y, z are positive and the value of p is O<P<1.

So, PMLE maximizes the likelihood.

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