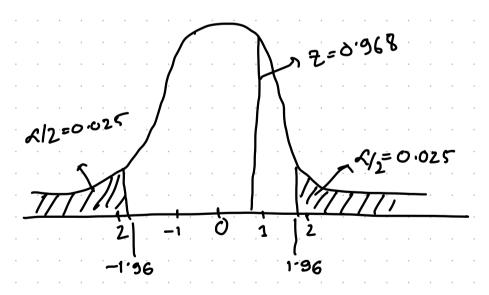
## Problem 1:

Parit 1: 
$$\frac{x-\theta}{\sqrt{n}}$$

here  $\bar{\chi}_{=}1.5$ ,  $\theta=1$ , n=15, and  $\sigma^{2}=4$  = 70=2

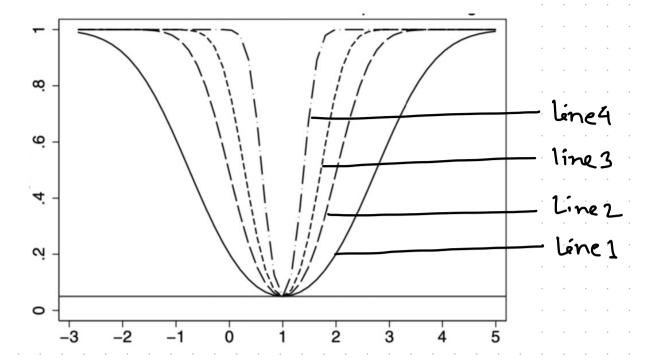
$$\frac{2}{2} = \frac{1.5 - 1}{2/\sqrt{15}}$$

Herre, of= 0.05, two tailed test, %= 0.025 Using 2 table the 2 value of 7 for the two tailed test is 1.96



wè can πeject Ho if 7 <-1.96 oπ if ₹> 1.960 Hene 0.968< 1.960

so, we cannot reject Ho, on the other hand Ho is accepted.



For understanding of mename the line with line 1, lihez, line 3 and line 4.

here when the sample size gets larger, the z value increases therefore we will more likely to reject the null hypothesis; less likely to fail to reject the null hypothesis, thus the power of test increase.

Also when increase the sample size, the sampling distributions are getting narrow.

and when they are getting narmow then

## difficult to reject the null hypothesis.

| Line    |
|---------|
| Line 4  |
| Line 2  |
| Line 1  |
| Line 3. |
|         |

## Part 3:

From Pairt 1 we found that for a=0.05two tabled test the value is ± 1.96

$$\Rightarrow P(-1.96 < \frac{\bar{\chi}-\theta}{\sigma/\bar{\chi}_{h}} < 1.96) = 0.95$$

=) 
$$P(\bar{\chi} - 1.96 \frac{\sigma}{\sqrt{n}} < \theta < \bar{\chi} + 1.96 \frac{\sigma}{\sqrt{m}}) = 0.95$$

So, when errnor probability &=0.05 then the confidence interval of Dis (0.48, 2.52)

## Part 4:

From Part 3 (\*)

$$P(\overline{\chi}-1.96\frac{\sigma}{\overline{m}}<\theta<\overline{\chi}+1.96\frac{\sigma}{\overline{m}})\approx0.95$$

=) 
$$P(1.5 - 1.96 \frac{2}{\sqrt{n}} < 0 < 15 + 1.96 \frac{2}{\sqrt{n}}) \approx 0.95$$

=) 
$$P\left(1.5 - \frac{3.92}{\sqrt{n}} < 0 < 1.5 + \frac{3.92}{\sqrt{n}}\right) \approx 0.95$$

Now, we take some sample size and calculate the corrresponding confidence interval.

| · · · · · · | confidence înterval |  |  |  |  |
|-------------|---------------------|--|--|--|--|
| <b>5</b>    | (-0.25, 3.25)       |  |  |  |  |
| 10          | (0.26, 2.74)        |  |  |  |  |
| 15          | (0.49, 2.51)        |  |  |  |  |
| 20          | (0.62, 2.38)        |  |  |  |  |
| 50          | (0.95, 2.05)        |  |  |  |  |
| 100         | (1.11, 1.892)       |  |  |  |  |

So, when sample size is increasing then
the Lower bound of the interval is
increasing and the upper bound is
decreasing. So, the sampling distribution
are getting narrow, and we have
less area to reject the null hypothesis.

At some big sample size the upper and lower bound will be same.

Confidence interval & Rejection region

8/8