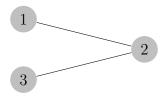


## 10. Problem sheet for Statistical Data Analysis

## Exercise 1 (8 Points)

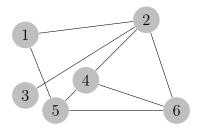
For the following graph compute the Laplacian matrix and its eigenvalues and eigenvectors.  $^{1}$ 



Find (by hand) a bisection of this graph such that RatioCut is minimal and one such that NCut is minimal.

## Exercise 2 (8 Points)

Given is the following graph



- (i) Construct its corresponding Laplacian matrix.
- (ii) From the previous exercise sheet we know that  $\{1, 2, 3\}, \{4, 5, 6\}$  is (one of) the best partition(s) into two classes. Construct the corresponding vector f.
  - Verify the equation

$$f^{\top}Lf = |V| \cdot RatioCut(A, \bar{A}) \tag{1}$$

for this particular choice of f.

• Show that f is orthogonal to the all-one-vector and that  $||f||^2 = n$  holds.

<sup>&</sup>lt;sup>1</sup>Use Sarrus' scheme to compute the determinant.