Improving Group Fairness in Knowledge Distillation via Laplace Approximation of Early Exits

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CS 769 Optimization in Machine Learning

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Overview

1. Recap from Seminar

2. Experiments And Results

3. Analysis And Future Work

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 Knowledge Distillation as an effective way to distill knowledge from teacher to student

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- DEDIER loss

$$\mathcal{L}_{ extit{student}} = \sum_{D_{ extit{w}}} (1 - \lambda) \cdot \emph{l}_{ extit{ce}} + \lambda \cdot exttt{wt} \cdot \emph{l}_{ extit{kd}}$$

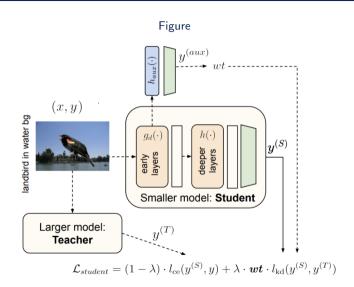
where $\mathbf{wt} = \exp^{\beta.\mathbf{cm}.\alpha}$ and $\mathbf{cm}(\mathbf{p}) = \mathbf{p_{max}} - \max_{\mathbf{p_k} \in \mathbf{p} - \mathbf{p_{max}}} \mathbf{p_k}$

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- Experiment: Laplace Approximation based uncertainity estimate to reweight both the losses.



Figure



(blond, male)



(blond, female)



(landbird, land bg) (waterbird, land bg)





S1: oh uh-huh well no they wouldn't would they no S2: No, they wouldn't go there.

Group: (contradiction X, has negation words)

Sentence: You sound like a terrorist Group: (Toxic ... mention of identity .X.)

\$1: Do you think Mrs. Inglethorp made a will leaving all her money to Miss Howard? I asked in a low voice, with some curiosity. S2: I yelled at the top of my lungs. Group: (contradiction ... has negation words

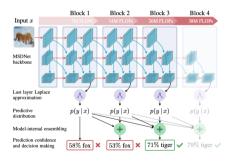
Sentence: She hates men because that's what her mother taught her Group: (Toxic ... mention of identity ...)

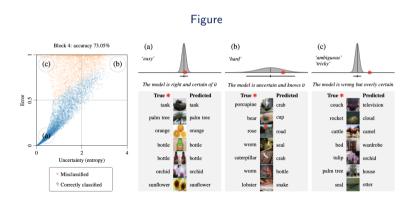
S1: so i have to find a way to supplement that S2: I need a way to add something extra. Group: (contradiction X has negation words X) Sentence: I doubt that anyone cares whether you believe it or not Group: (Toxic X, mention of identity X)



CivilComments-WILDS MultiNLI CelebA Waterbirds







• Bayesian treatment of parameters

$$p(\boldsymbol{\theta} \mid \mathcal{D}_{\mathsf{train}}) = \frac{p(\mathcal{D}_{\mathsf{train}} \mid \boldsymbol{\theta}) \, p(\boldsymbol{\theta})}{\int_{\boldsymbol{\theta}} p(\mathcal{D}_{\mathsf{train}}, \boldsymbol{\theta}) \, d\boldsymbol{\theta}} = \frac{[\mathsf{likelihood}] \times [\mathsf{prior}]}{[\mathsf{model evidence}]}$$

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MAP estimate can be found by maximising the unnormalised posterior:

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Gaussian distribution via laplace approximation

$$p(\hat{\mathbf{z}}_i \mid \mathbf{x}_i) = \mathcal{N}(\hat{\mathbf{W}}_{MAP}^{\top} \hat{\boldsymbol{\phi}}_i, (\hat{\boldsymbol{\phi}}_i^{\top} \mathbf{V} \hat{\boldsymbol{\phi}}_i) \mathbf{U})$$

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Samples

$$\hat{\mathbf{z}}_{i}^{(I)} = \hat{\mathbf{W}}_{\mathsf{MAP}}^{\top} \hat{\boldsymbol{\phi}}_{i} + (\hat{\boldsymbol{\phi}}_{i}^{\top} \mathbf{V} \hat{\boldsymbol{\phi}}_{i})^{\frac{1}{2}} (\mathsf{Lg}^{(I)})$$

 $\mathbf{g}^{(\prime)} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ and \mathbf{L} is the Cholesky factor of \mathbf{U}



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- The MultiNLI dataset [Williams et al., 2018] was used.
- Determine if premise entails, contradicts, or is neutral given a hypothesis.
- Major Diffrences with DEDIER: The auxiliary reweighting is done in every layer, as student trained for five epochs.
- The auxiliary network used is a simple, single layer network.
- Models Used
 - Teacher model: bert-base-uncased (12-layer BERT, hidden size 768)
 - Student model: distilbert-base-uncased (6-layer DistilBERT, hidden size 768)
 - Auxiliary network: One-layer linear classifier trained on the students third layer.

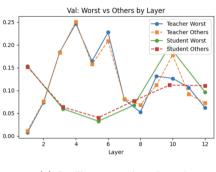
- Hyperparameters
 - Teacher fine-tuning
 - Epochs: $E_T = 3$
 - Learning rate: 2×10^{-5}
 - Optimizer: AdamW
 - Student training
 - Epochs: $E_S = 5$
 - Learning rate: 2×10^{-5}
 - Optimizer: AdamW
 - Distillation temperature: $\tau = 2.0$
- Training and Evaluation
 - Batch size: 16
 - Dataset: MultiNLI (via HuggingFace datasets)
 - Evaluation: Accuracy and per-group performance (negation vs. non-negation)
 - Tokenization: bert-base-uncased tokenizer with padding and truncation
 - Learning rate scheduler: Linear schedule with warm-up

Metric	Teacher	Student (Aux layer 3)	Student (Aux layer 6)	Group
Average Accuracy	0.845	0.835	0.832	All

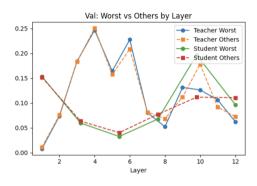
Table: Results of Dedier with Laplace

Metric	Teacher	Student
Final Test Accuracy	0.841	0.830

Table: Original DEDIER performance with same teacher

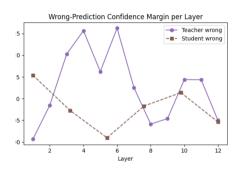


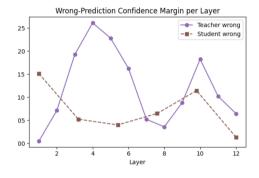




(b) Auxiliary network on layer 6 (last layer)

Figure: Confidence margins per layer on worst group predictions and all predictions





(a) Auxiliary network on layer 3 (b) Auxiliary network on layer 6 (last layer)

Figure: Confidence margins in student and teacher on the predictions that were wrong

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Analysis And Future Work

- Minor improvement in accuracy of the student model by the proposed approach over DEDIER on MultiNLI
- Still more testing needed, on varied datasets and teacher models for justifying its use.
- The confidence margins are generally lower than one used in DEDIER work.
- Need to study effects of increasing layers of Aux network
- Hyperparameter tuning

Conclusion

- Cheap, effective uncertainty via Laplace in early exits.
- Uncertainty reweights KD loss in student models.
- Reduces reliance on simple features.

References



Meronen, L., Trapp, M., Pilzer, A., Yang, L., and Solin, A. (2023). Fixing Overconfidence in Dynamic Neural Networks.

Version Number: 4.

Williams, A., Nangia, N., and Bowman, S. R. (2018).

A broad-coverage challenge corpus for sentence understanding through inference.

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