



INDIAN INSTITUTE OF INFORMATION TECHNOLOGY SONEPAT

भारतीय सूचना प्रौद्योगिकी संस्थान सोनीपत

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Mid Sem-I
Branch: CSE & IT

Subject: AFL
M.M.-15 marks

Roll no
Time- 60 mint.

Note: All questions are compulsory.

Q.[1] (a) Construct right-and left-linear grammars for the language $L = \{a^n b^m : n \geq 2, m \geq 3\}$ 1.5

Q.[1] (b) Obtain the production rules for CFG g for the given language generated as 1.5

(a) $L(G) = \{w \mid w \in \{a, b\}^*, n_a(w) = n_b(w)\}$

(b) $L(G) = \{w \mid w \in \{a, b\}, n_a(w) = 2 n_b(w)\}$

(c) $L(G) = \{w \mid w \in \{a, b\}, n_a(w) = 3 n_b(w)\}$

Q.[2](a) Obtain the language generated by each of the following production rules. 2

(a) $A \rightarrow a$
 $A \rightarrow aB$
 $A \rightarrow \epsilon$

(b) $S \rightarrow aS$
 $S \rightarrow \epsilon$

(c) $A \rightarrow a$
 $A \rightarrow aB$
 $A \rightarrow \epsilon$

(d) $A \rightarrow aS$
 $S \rightarrow bS$
 $S \rightarrow \epsilon$

(e) $S \rightarrow aS$
 $S \rightarrow bS$
 $S \rightarrow a$

(f) $S \rightarrow ab$
 $S \rightarrow bs$
 $S \rightarrow a$
 $S \rightarrow b$

Q.[2](b) Convert the following PDA into an equivalent CFG. 2

$\delta(q_0, a, z_0) \rightarrow (q_1, z_1 z_0)$

$\delta(q_0, b, z_0) \rightarrow (q_1, z_2 z_0)$

$\delta(q_1, a, z_1) \rightarrow (q_1, z_1 z_1)$

$\delta(q_1, b, z_1) \rightarrow (q_1, \lambda)$

$\delta(q_1, b, z_2) \rightarrow (q_1, z_2 z_2)$

$\delta(q_1, a, z_2) \rightarrow (q_1, \lambda)$

$\delta(q_1, \lambda, z_0) \rightarrow (q_1, \lambda)$ // accepted by the empty stack

Q.[3](a) Convert the following CFG in Chomsky Normal Form (CNF) 2

$S \rightarrow aA/bB$

$A \rightarrow aBB/bS/b$

$B \rightarrow bAA/aS/a$

Q.[3](b) Convert the following CFG into GNF. 2

$S \rightarrow XY$

$X \rightarrow YS/b$

$Y \rightarrow SX/a$

Q.[4](a) Given $L = \{a^n b^m \mid n < m\}$. 2

Derive (i) a context-free grammar that accepts L

(ii) a PDA accepting L by empty store

(iii) a PDA accepting L by final state.

Q.[4](b) Construct an equivalent PDA for the following context-free grammar. 2

$S \rightarrow aAB/bBA$

$A \rightarrow bS/a$

$B \rightarrow aS/b$

Show an ID for the string ***abbbaabbbbab*** for the PDA generated with stack description.