

Logical Equivalences Involving Conditional Statements

$$p \rightarrow q \equiv \neg p \vee q$$

$$\boxed{p \rightarrow q \equiv \neg q \rightarrow \neg p} \text{ Contrapositive}$$

$$p \vee q \equiv \neg p \rightarrow q$$

$$p \wedge q \equiv \neg(p \rightarrow \neg q)$$

$$\neg(p \rightarrow q) \equiv p \wedge \neg q$$

$$(p \rightarrow q) \wedge (p \rightarrow r) \equiv p \rightarrow (q \wedge r)$$

$$(p \rightarrow q) \wedge (q \rightarrow r) \equiv (p \vee q) \rightarrow r$$

$$(p \rightarrow q) \vee (p \rightarrow r) \equiv p \rightarrow (q \vee r)$$

$$(p \rightarrow r) \vee (q \rightarrow r) \equiv (p \wedge q) \rightarrow r$$

$$p \rightarrow q \text{ is } q \rightarrow p \text{ Converse}$$

$$p \rightarrow q \text{ is } \neg p \rightarrow \neg q \text{ Inverse}$$

$$\boxed{p \leftrightarrow q \equiv p \rightarrow q \wedge q \rightarrow p}$$