

Assignment –I

Practice Exercises

In Exercises 1–18, use the definition of continuity to determine whether f is continuous at a .

1. $f(x) = 2x + 5$
 $a = 1$
2. $f(x) = 3x + 4$
 $a = 1$
3. $f(x) = x^2 - 3x + 7$
 $a = 4$
4. $f(x) = x^2 - 5x + 6$
 $a = 4$
5. $f(x) = \frac{x^2 + 4}{x - 2}$
 $a = 3$
6. $f(x) = \frac{x^2 + 6}{x - 5}$
 $a = 6$
7. $f(x) = \frac{x + 5}{x - 5}$
 $a = 5$
8. $f(x) = \frac{x + 7}{x - 7}$
 $a = 7$
9. $f(x) = \frac{x - 5}{x + 5}$
 $a = 5$
10. $f(x) = \frac{x - 7}{x + 7}$
 $a = 7$
11. $f(x) = \frac{x^2 + 5x}{x^2 - 5x}$
 $a = 0$
12. $f(x) = \frac{x^2 + 8x}{x^2 - 8x}$
 $a = 0$
13. $f(x) = \begin{cases} \frac{x^2 - 4}{x - 2} & \text{if } x \neq 2 \\ 5 & \text{if } x = 2 \end{cases}$
 $a = 2$
14. $f(x) = \begin{cases} \frac{x^2 - 36}{x - 6} & \text{if } x \neq 6 \\ 13 & \text{if } x = 6 \end{cases}$
 $a = 6$
15. $f(x) = \begin{cases} x - 5 & \text{if } x \leq 0 \\ x^2 + x - 5 & \text{if } x > 0 \end{cases}$
 $a = 0$
16. $f(x) = \begin{cases} x - 4 & \text{if } x \leq 0 \\ x^2 + x - 4 & \text{if } x > 0 \end{cases}$

$$27. f(x) = \begin{cases} x - 1 & \text{if } x \leq 1 \\ x^2 & \text{if } x > 1 \end{cases} \quad 28. f(x) = \begin{cases} x - 2 & \text{if } x \leq 2 \\ x^2 - 1 & \text{if } x > 2 \end{cases}$$

$$29. f(x) = \begin{cases} \frac{x^2 - 1}{x - 1} & \text{if } x \neq 1 \\ 2 & \text{if } x = 1 \end{cases}$$

$$30. f(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & \text{if } x \neq 3 \\ 6 & \text{if } x = 3 \end{cases}$$

$$31. f(x) = \begin{cases} x + 6 & \text{if } x \leq 0 \\ 6 & \text{if } 0 < x \leq 2 \\ x^2 + 1 & \text{if } x > 2 \end{cases}$$

$$32. f(x) = \begin{cases} x + 7 & \text{if } x \leq 0 \\ 7 & \text{if } 0 < x \leq 3 \\ x^2 - 1 & \text{if } x > 3 \end{cases}$$

$$33. f(x) = \begin{cases} 5x & \text{if } x < 4 \\ 21 & \text{if } x = 4 \\ x^2 + 4 & \text{if } x > 4 \end{cases}$$

$$34. f(x) = \begin{cases} 7x & \text{if } x < 6 \\ 41 & \text{if } x = 6 \\ x^2 + 6 & \text{if } x > 6 \end{cases}$$

in 31: first put $x=0$ in $y=x+6$ and in $y=6$ then compare them, after that put $x=2$ in both $y=6$ and $y=x^2+1$ and then compare them if the limit of $y=x+6$ is equal to $y=6$ and the limit of $y=6$ is equal to the $y=x^2+1$'s limit then the limit exist.

Practice Plus

In Exercises 35–38, graph each function. Then determine for what numbers, if any, the function is discontinuous.

$$35. f(x) = \begin{cases} \sin x & \text{if } -\pi \leq x < 0 \\ -\sin x & \text{if } 0 \leq x < \pi \\ \cos x & \text{if } \pi \leq x \leq 2\pi \end{cases}$$

$$36. f(x) = \begin{cases} -\cos x & \text{if } -\pi \leq x < 0 \\ -\sin x & \text{if } 0 \leq x < \pi \\ \sin x & \text{if } \pi \leq x \leq 2\pi \end{cases}$$

$$37. f(x) = \begin{cases} -1 & \text{if } x \text{ is an integer.} \\ 1 & \text{if } x \text{ is not an integer.} \end{cases}$$

$$a = 0$$

$$16. f(x) = \begin{cases} x - 4 & \text{if } x \leq 0 \\ x^2 + x - 4 & \text{if } x > 0 \end{cases}$$

$$a = 0$$

$$17. f(x) = \begin{cases} 1 - x & \text{if } x < 1 \\ 0 & \text{if } x = 1 \\ x^2 - 1 & \text{if } x > 1 \end{cases}$$

$$a = 1$$

$$18. f(x) = \begin{cases} 2 - x & \text{if } x < 1 \\ 1 & \text{if } x = 1 \\ x^2 & \text{if } x > 1 \end{cases}$$

$$a = 1$$

In Exercises 19–34, determine for what numbers, if any, the given function is discontinuous.

$$19. f(x) = x^2 + 4x - 6 \qquad 20. f(x) = x^2 + 8x - 10$$

$$21. f(x) = \frac{x + 1}{(x + 1)(x - 4)} \qquad 22. f(x) = \frac{x + 2}{(x + 2)(x - 5)}$$

$$23. f(x) = \frac{\sin x}{x} \qquad 24. f(x) = \frac{1 - \cos x}{x}$$

$$25. f(x) = \pi \qquad 26. f(x) = c$$

$$\left(\begin{array}{l} \sin x \\ \sin x \end{array} \right) \quad \text{if } n \leq x \leq 2n$$

$$37. f(x) = \begin{cases} -1 & \text{if } x \text{ is an integer.} \\ 1 & \text{if } x \text{ is not an integer.} \end{cases}$$

$$38. f(x) = \begin{cases} 2 & \text{if } x \text{ is an odd integer.} \\ -2 & \text{if } x \text{ is not an odd integer.} \end{cases}$$

In Exercises 39–42, determine for what numbers, if any, the function is discontinuous. Construct a table to find any required limits.

$$39. f(x) = \begin{cases} \frac{\sin 2x}{x} & \text{if } x \neq 0 \\ 2 & \text{if } x = 0 \end{cases}$$

$$40. f(x) = \begin{cases} \frac{\sin 3x}{x} & \text{if } x \neq 0 \\ 3 & \text{if } x = 0 \end{cases}$$

$$41. f(x) = \begin{cases} \frac{\cos x}{x - \frac{\pi}{2}} & \text{if } x \neq \frac{\pi}{2} \\ 1 & \text{if } x = \frac{\pi}{2} \end{cases}$$

$$42. f(x) = \begin{cases} \frac{\sin x}{x - \pi} & \text{if } x \neq \pi \\ 1 & \text{if } x = \pi \end{cases}$$