# Dynamics and Control Of Spacecraft Astrosat Controller Design

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# Chapter 1

# Kinematics and Dynamics of Astrosat

#### 1.1 Introduction

We are planning to design a preliminary attitude control system for ASTROSAT satellite. Since this satellite is an inertial pointing satellite, we have chosen to stabilize the satellite using zero momentum biased stabilization method with 4 wheel tetrahedron configuration. Star sensors senses and provide the values of roll, pitch and yaw Euler angles along with gyroscopes. Our design also includes the momentum dumping, as and when any of the wheels reach their maximum angular rate capacity.

We have initially derived the kinematic equations of motion using 2-3-1 rotation sequence to get the Euler angles. Euler angles are then converted to quaternions before integration to avoid any singularities like gimbal lock phenomenon. Dynamic equations of motion for inertially pointing satellite, with zero momentum biased system configuration is derived using Euler equations. Gravity gradient torque is also considered as disturbance torque, apart from the disturbance torque given in the problem which is in the order of milli N-m. Since our's is an inertially pointing satellite, our roll, pitch and yaw equations of motion will be decoupled.

We have studied the motion of satellite, in roll, pitch and yaw, found that the solutions are unstable in all the 3 DOF in the presence of disturbances and hence we have concluded to go for active stabilization technique based on Proportional-Derivative (PD) controller using momentum wheels in tetrahedral configuration. The gains for our control system design are chosen in such a way that the maximum allowable steady state error does not exceed 0.005 deg about all the axes (zero momentum biased system).

#### 1.2 Astrosat

It is an inertial pointing spacecraft in a 650km 6 deg inclined circular orbit; 4-wheel tetrahedron wheel system is used for momentum management; Actual MI properties of the s/c after deployment.

$$J_c = \begin{bmatrix} 1763 & -52 & -16 \\ -52 & 1591 & 25 \\ -16 & 25 & 1185 \end{bmatrix} kg - m^2$$

Mass of the s/c = 1542 Kg. [x,y,z] axes are yaw, roll and pitch respectively. Initially we have assumed that the cross product of inertias are negligible and designed the control system. Then once the control design is completed, we have used the actual inertia matrix to check the performance variations. The momentum dumping is achieved by using 60 A-m<sup>2</sup> torque rods about all the three axes. Disturbance torques are  $T_x = T_z = 2*10^{-3}$  Nm and  $T_y = 10^{-4}$  Nm and satellite's orbital angular velocity,  $\omega_o = 1.0741*10^{-3}$  rad/sec

### 1.3 Kinematics

We are choosing 2-3-1  $(\psi, \theta, \phi)$  rotation for our kinematics. The angle rates and angular velocity can be related as below,

$$\begin{bmatrix} \dot{\phi} \\ \dot{\psi} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} 1 & -\cos\phi tan\theta & \sin\phi tan\theta \\ 0 & \cos\phi \sec\theta & -\sin\phi \sec\theta \\ 0 & \sin\phi & \cos\phi \end{bmatrix} \begin{bmatrix} \omega_x \\ \omega_y \\ \omega_z \end{bmatrix}$$
 (1.3.1)

After small angle approximations,

$$\begin{bmatrix} \dot{\phi} \\ \dot{\psi} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \omega_x \\ \omega_y \\ \omega_z \end{bmatrix} \tag{1.3.2}$$

### 1.4 Dynamics

Since we are using a zero momentum biased control system, the following holds true. Where  $\vec{h_i}$  are the wheel angular momentum.

$$\vec{h}_1 + \vec{h}_2 + \vec{h}_3 + \vec{h}_4 = 0 \tag{1.4.1}$$

Also each of XYZ components must be zero.

$$h_{wx} = \frac{h_1}{\sqrt{3}} - \frac{h_2}{\sqrt{3}} - \frac{h_3}{\sqrt{3}} + \frac{h_4}{\sqrt{3}} = 0 \tag{1.4.2}$$

$$h_{wy} = \frac{h_1}{\sqrt{3}} - \frac{h_2}{\sqrt{3}} + \frac{h_3}{\sqrt{3}} - \frac{h_4}{\sqrt{3}} = 0$$
 (1.4.3)

$$h_{wz} = \frac{h_1}{\sqrt{3}} + \frac{h_2}{\sqrt{3}} - \frac{h_3}{\sqrt{3}} - \frac{h_4}{\sqrt{3}} = 0 \tag{1.4.4}$$

The dynamics of the wheels is governed by,

$$\frac{d}{dt}\left(\vec{H}_w\right) = -\vec{T}_c$$

where  $\vec{T}_c$  is the control torque.

The Euler equations for the spacecraft system can be rewritten as below,

$$J_c \dot{\omega} + \omega \times (J_c \omega) = T_c + T_d \tag{1.4.5}$$

$$J_{x}\dot{\omega}_{x} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$-\omega_{z}\left(J_{y}\omega_{y} + \frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} + \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}}\right)$$

$$+\omega_{y}\left(J_{z}\omega_{z} + \frac{I_{w}\omega_{1}}{\sqrt{3}} + \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}}\right) = 0$$
(1.4.6)

$$J_{y}\ddot{\omega}_{y} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$+\omega_{z}\left(J_{x}\omega_{x} + \frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} + \frac{I_{w}\omega_{4}}{\sqrt{3}}\right)$$

$$-\omega_{x}\left(J_{z}\omega_{z} + \frac{I_{w}\omega_{1}}{\sqrt{3}} + \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}}\right) = 0$$

$$J_{z}\ddot{\omega}_{z} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$\left(J_{z}\omega_{1} - J_{w}\omega_{1} - J_{w}\omega_{2} - J_{w}\omega_{3} - J_{w}\omega_{4}\right)$$

$$-\omega_y \left( J_x \omega_x + \frac{I_w \omega_1}{\sqrt{3}} - \frac{I_w \omega_2}{\sqrt{3}} - \frac{I_w \omega_3}{\sqrt{3}} + \frac{I_w \omega_4}{\sqrt{3}} \right)$$

$$+\omega_x \left( J_y \omega_y + \frac{I_w \omega_1}{\sqrt{3}} - \frac{I_w \omega_2}{\sqrt{3}} + \frac{I_w \omega_3}{\sqrt{3}} - \frac{I_w \omega_4}{\sqrt{3}} \right) = 0$$

$$(1.4.8)$$

After doing small angle approximations the euler equations can be written as follows,

$$J_{x}\ddot{\phi} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$-\dot{\theta} \left( \frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} + \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}} \right)$$

$$+\dot{\psi} \left( \frac{I_{w}\omega_{1}}{\sqrt{3}} + \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}} \right) = 0$$

$$J_{y}\ddot{\psi} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$J_{y}\ddot{\psi} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$+\dot{\theta} \left( \frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} + \frac{I_{w}\omega_{4}}{\sqrt{3}} \right)$$

$$-\dot{\phi} \left( \frac{I_{w}\omega_{1}}{\sqrt{3}} + \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}} \right) = 0$$
(1.4.10)

$$J_{z}\ddot{\theta} + \frac{I_{w}\dot{\omega}_{1}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{2}}{\sqrt{3}} - \frac{I_{w}\dot{\omega}_{3}}{\sqrt{3}} + \frac{I_{w}\dot{\omega}_{4}}{\sqrt{3}}$$

$$-\dot{\psi}\left(\frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} - \frac{I_{w}\omega_{3}}{\sqrt{3}} + \frac{I_{w}\omega_{4}}{\sqrt{3}}\right)$$

$$+\dot{\phi}\left(\frac{I_{w}\omega_{1}}{\sqrt{3}} - \frac{I_{w}\omega_{2}}{\sqrt{3}} + \frac{I_{w}\omega_{3}}{\sqrt{3}} - \frac{I_{w}\omega_{4}}{\sqrt{3}}\right) = 0$$
(1.4.11)

# Chapter 2

# Controller Design

We will be using the modified Proportional Derivative (PD) controller.

#### 2.0.1 Modified PD controller

#### Control Torque

For a general moment of inertia matrix, after including control torques, disturbance torques and the gravity gradient torques, the dynamic equations become:

$$I_{xx}\dot{\omega}_x + I_{xy}\dot{\omega}_y + I_{xz}\dot{\omega}_z +$$

$$\omega_y \left( I_{zx}\omega_x + I_{zy}\omega_y + I_{zz}\omega_z \right)$$

$$-\omega_z \left( I_{yx}\omega_x + I_{yy}\omega_y + I_{yz}\omega_z \right) = T_{cx} + T_{dx} + T_{gx}$$
(2.0.1)

$$I_{yx}\dot{\omega}_x + I_{yy}\dot{\omega}_y + I_{yz}\dot{\omega}_z +$$

$$\omega_z \left( I_{xx}\omega_x + I_{xy}\omega_y + I_{xz}\omega_z \right)$$

$$-\omega_x \left( I_{zx}\omega_x + I_{zy}\omega_y + I_{zz}\omega_z \right) = T_{cy} + T_{dy} + T_{gy}$$
(2.0.2)

$$I_{zx}\dot{\omega}_x + I_{zy}\dot{\omega}_y + I_{zz}\dot{\omega}_z +$$

$$\omega_x \left( I_{yx}\omega_x + I_{yy}\omega_y + I_{yz}\omega_z \right)$$

$$-\omega_y \left( I_{xx}\omega_x + I_{xy}\omega_y + I_{xz}\omega_z \right) = T_{cz} + T_{dz} + T_{gz}$$
(2.0.3)

$$T_c = -\begin{bmatrix} K_{px}(\phi - R_{\phi}) + K_{dx}\dot{\phi} \\ K_{py}(\psi - R_{\psi}) + K_{dy}\dot{\psi} \\ K_{pz}(\theta - R_{\theta}) + K_{dz}\dot{\theta} \end{bmatrix}$$

$$(2.0.4)$$

#### 2.0.1.1 Gravity Gradient torque:

$$r_{b} = C_{bo}r$$

$$= \begin{bmatrix} 1 & \theta & -\psi \\ -\theta & 1 & \phi \\ \psi & -\phi & 1 \end{bmatrix} \begin{bmatrix} -r \\ 0 \\ 0 \end{bmatrix}$$

$$= \begin{bmatrix} -r \\ \theta r \\ -\psi r \end{bmatrix}$$

$$(2.0.5)$$

$$T_{g} = \frac{3\mu}{r^{5}} r_{b}^{x} I r_{b}$$

$$= \frac{3\mu}{r^{5}} \begin{bmatrix} 0 & \psi r & \theta r \\ -\psi r & 0 & r \\ -\theta r & -r & 0 \end{bmatrix} I \begin{bmatrix} -r \\ \theta r \\ -\psi r \end{bmatrix}$$

$$= \frac{3\mu}{r^{3}} \begin{bmatrix} 0 \\ (I_{x} - I_{z}) \psi \\ (I_{x} - I_{y}) \theta \end{bmatrix}$$

$$= 3\omega_{0}^{2} \begin{bmatrix} 0 \\ (I_{x} - I_{z}) \psi \\ (I_{x} - I_{y}) \theta \end{bmatrix}$$

$$(2.0.8)$$

#### 2.0.2 Wheel Dynamics

The individual wheel torques are:

$$T_1 = \frac{1}{4} \left( \sqrt{3} T_{cx} + \sqrt{3} T_{cy} + \sqrt{3} T_{cz} \right) \tag{2.0.9}$$

$$T_2 = \frac{1}{4} \left( -\sqrt{3}T_{cx} - \sqrt{3}T_{cy} + \sqrt{3}T_{cz} \right) \tag{2.0.10}$$

$$T_3 = \frac{1}{4} \left( -\sqrt{3}T_{cx} + \sqrt{3}T_{cy} - \sqrt{3}T_{cz} \right) \tag{2.0.11}$$

$$T_4 = \frac{1}{4} \left( \sqrt{3} T_{cx} - \sqrt{3} T_{cx} - \sqrt{3} T_{cx} \right) \tag{2.0.12}$$

The dynamics of wheel **i** are described by the equations below:

$$I\dot{\omega}_i = T_i \tag{2.0.13}$$

$$I\dot{\omega}_i + IC_{w_ib}\dot{\omega} + (\omega_i + C_{w_ib}\omega) \times (I\omega_i + IC_{w_ib}\omega) = T_i$$

$$I\dot{\omega}_i = T_i - IC_{w_ib}\dot{\omega} - (\omega_i + C_{w_ib}\omega) \times (I\omega_i + IC_{w_ib}\omega)$$
(2.0.14)

where I is the moment of inertia of the whole spacecraft.

### 2.0.3 Estimates for $K_d$ and $K_p$

The system can be represented as a transfer function:

$$G_p(s) = \frac{1}{Is^2 + K_d s} (2.0.15)$$

Assuming a critically damped system,

$$\xi = 1$$

$$K_d^2 = 4IK_p (2.0.16)$$

Closed loop system pole:

$$1 + G_c(s) = 0$$

$$1 + \frac{K_p}{Is^2 + K_d s} = 0$$

$$Is^2 + K_d s + K_p = 0$$

So our spacecraft is a Type 1 system.

$$s^2 + \frac{K_d}{I}s + \frac{K_p}{I} = 0 (2.0.17)$$

$$s^2 + 2\xi\omega_n s + \omega_n^2 = 0 (2.0.18)$$

From this equation, since we know that damping and frequency are positive,  $K_p$  and  $K_d$  are positive. This is also verified using Routh's stability criterion.

$$\omega_n^2 = \frac{K_p}{I} \tag{2.0.19}$$

$$2\xi\omega_n = \frac{K_d}{I}$$

$$\xi = \frac{K_d}{2\omega_n I} \tag{2.0.20}$$

$$\xi^2 = \frac{K_d^2}{4\frac{K_p}{I}I^2} = \frac{K_d^2}{4K_pI}$$

#### 2.0.4 Steady State errors

Without consideration of disturbance torque, the steady state error is given by,

$$lim_{s\to 0} \frac{sR(s)}{1 + G_0(s)}$$

$$\lim_{s \to 0} \frac{sR(s)}{1 + \left(\frac{1}{Is^2 + K_d s}\right) G_c(s)} = \lim_{s \to 0} \frac{s(Is^2 + K_d s)}{Is^2 + K_d s + G_c(s)} R(s)$$
$$= \lim_{s \to 0} \frac{Is + K_d}{I + \frac{K_d}{s} + \frac{G_c(s)}{s^2}} R(s)$$

Test signals  $R(s) = \frac{1}{s}$ ,  $R(s) = \frac{1}{s^2}$ ,  $R(s) = \frac{1}{s^3}$ ,

#### 2.0.4.1 Step Input

$$\lim_{s \to 0} \frac{Is + K_d}{I + \frac{K_d}{s} + \frac{G_c(s)}{s^2}} \frac{1}{s} = \lim_{s \to 0} \frac{Is + K_d}{Is + K_d + \frac{G_c(s)}{s}}$$

$$= \lim_{s \to 0} \frac{Is + K_d}{Is + K_d + \frac{K_p}{s}}$$

$$= 0$$

#### 2.0.4.2 Ramp Input

$$\begin{split} \lim_{s \to 0} \frac{Is + K_d}{I + \frac{K_d}{s} + \frac{G_c(s)}{s^2}} \frac{1}{s^2} &= \lim_{s \to 0} \frac{Is + K_d}{Is^2 + K_ds + K_p} \\ &= \frac{K_d}{K_p} \end{split}$$

#### 2.0.4.3 Accelerating Input

$$\lim_{s\to 0} \frac{Is + K_d}{I + \frac{K_d}{s} + \frac{G_c(s)}{s^2}} \frac{1}{s^3} = \lim_{s\to 0} \frac{Is + K_d}{Is^3 + K_ds^2 + sK_p}$$

$$= K_d$$

### 2.1 Momentum dumping

There is a maximum capacity that each of the wheel is designed for. If by applying control torques multiple times over the operation period, this capacity is reached, the wheel cannot be used and thus, requires the momentum of the entire spacecraft to be dumped using thrusters in order to restore the wheel to working configuration.

#### • Criteria 1: Maximum cap on angular rate in the wheel frame.

Consider the wheel torque on a wheel i. In the wheel frame, the moment of inertia of the entire spacecraft is  $I_t$ .

$$T_i = I_t \frac{d\omega_t}{dt}$$

$$\omega_t = \omega_i + C_{w_i b} \omega$$

$$I_{t} \frac{d\omega_{tw}}{dt} = I_{t} \frac{d\omega_{t}}{dt} + \omega_{t} \times I_{t}\omega_{t}$$

$$= I_{t} \left( \dot{\omega}_{i} + C_{w_{i}b}\dot{\omega}_{b} + \dot{C}_{w_{i}b}\omega_{b} \right)$$

$$+ (\omega_{i} + C_{wb}\omega_{b}) \times \left[ I_{t} \left( \omega_{i} + C_{wb}\omega_{b} \right) \right]$$

$$= I_{t}\dot{\omega}_{i} + I_{t}C_{w_{i}b}\dot{\omega}_{b} + \omega_{i} \times I_{t} \left( \omega_{i} + C_{wb}\omega_{b} \right)$$

$$+ C_{wb}\omega_{b} \times I_{t} \left( \omega_{i} + C_{wb}\omega_{b} \right)$$

All quantities quantities on RHS can be known at any instant from the dynamics. The dumping is done if the angular rate so obtained exceeds the cutoff.

#### • Criteria 2: Maximum cap on Torque

From our wheel dynamics, for a given control torque, each of the component torques given to every wheel is known. If it exceeds the maximum allowable torque rating of the wheel, momentum dumping is done.

#### • Criteria 2: Maximum cap on wheel angular momentum

Again, from our wheel dynamics, the applied wheel torque changes the angular speed of the wheel which has a maximum capacity. The resulting angular speed from a given torque must be estimated beforehand to see if it exceeds the capacity. If it is so, dumping of momentum is done.

#### 2.2 Results

#### **Excluding Gravity Gradient**

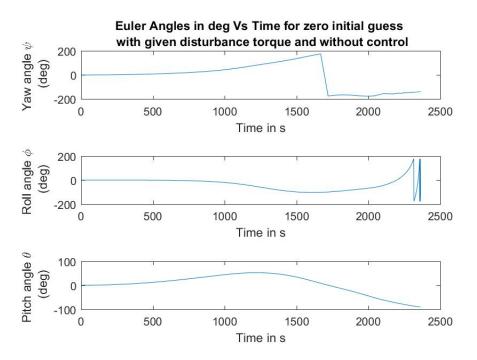


Figure 2.2.1:

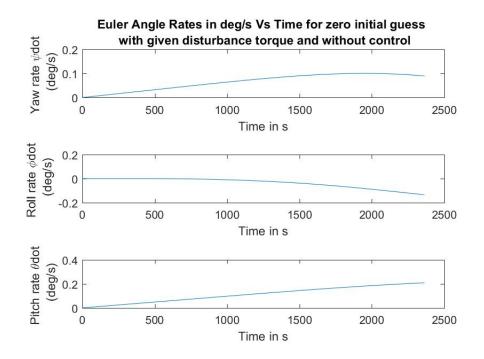


Figure 2.2.2:

Without the application of control torques, in the presence of disturbances, the Euler angles and Euler rates keep diverging. Hence active control system is required for Inertial pointing spacecrafts.

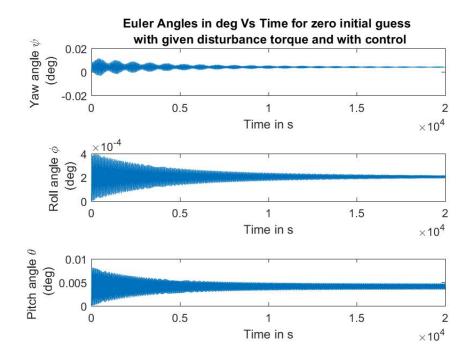


Figure 2.2.3:

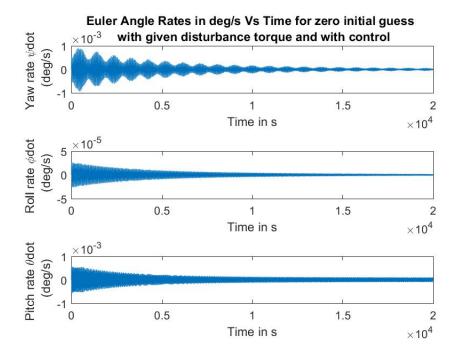


Figure 2.2.4:

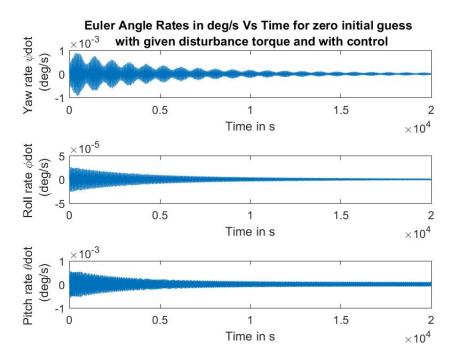


Figure 2.2.5:

As th control torques are applied in x,y and z directions, it is evident from the plots that the Euler angle and Euler rates settle down, such that the steady state error and error rates are well within 0.005 deg and 0.005 deg/sec, as per the requirement of the problem. The values of Kp and Kd are chosen as 28 and 0.95 after several analysis, for all the axes, to achieve the required steady state error.

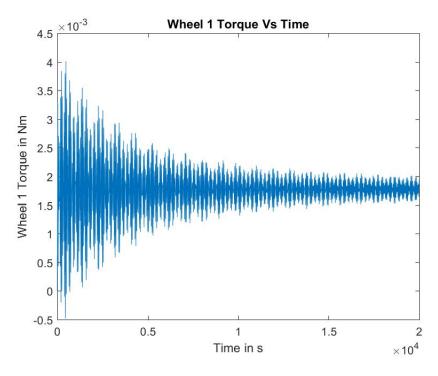


Figure 2.2.6:

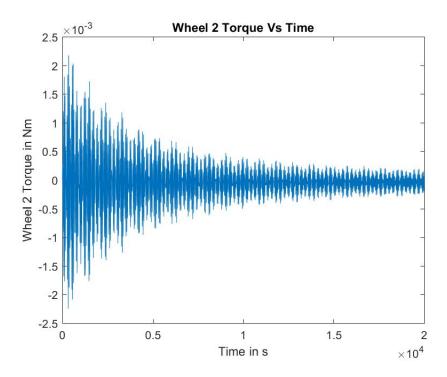


Figure 2.2.7:

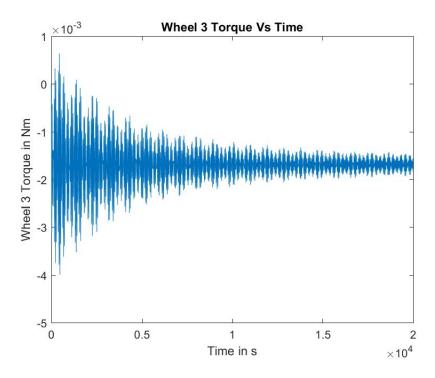


Figure 2.2.8:

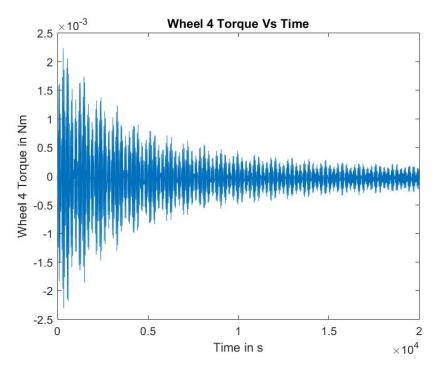


Figure 2.2.9:

All the above plots indicate the variation of Control Toruqe applied with time. As the control torque operate on the error dynamics of the system, eventually as the error reduces over time, the torque reaches zero, but the wheels will have change in angular speed and settle in new angular speed.

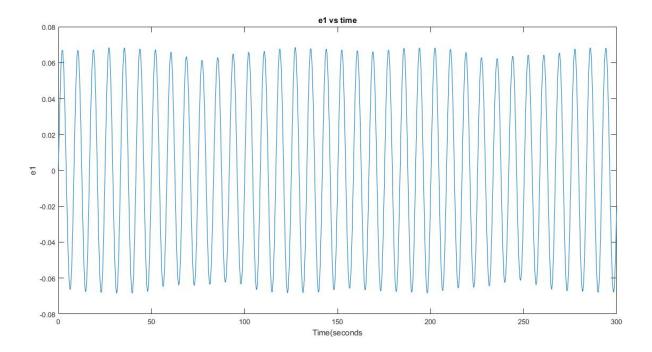


Figure 2.2.10:

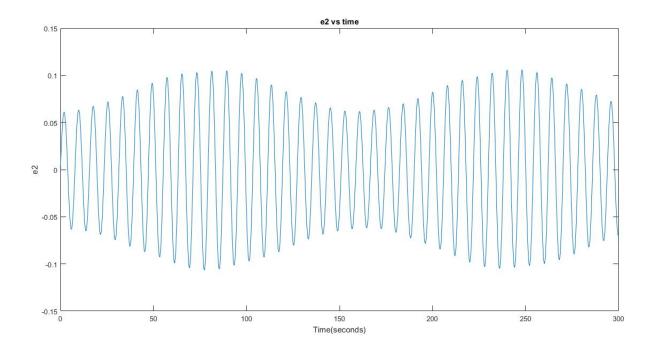


Figure 2.2.11:

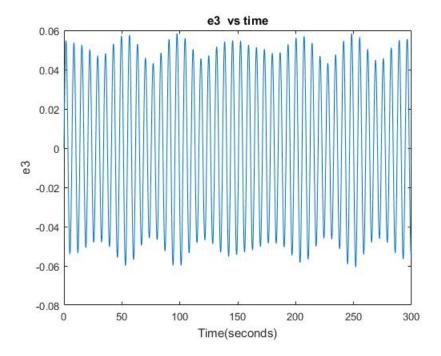


Figure 2.2.12:

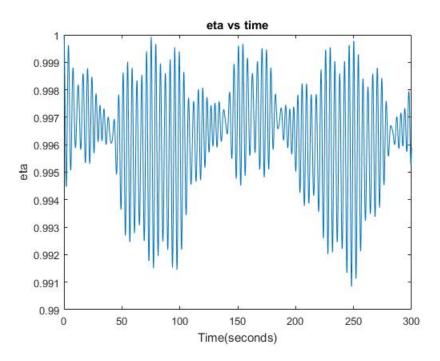


Figure 2.2.13:

The above plots show variation of quaternion in time without including gravity gradient. It can be clearly seen they reach a stable value.

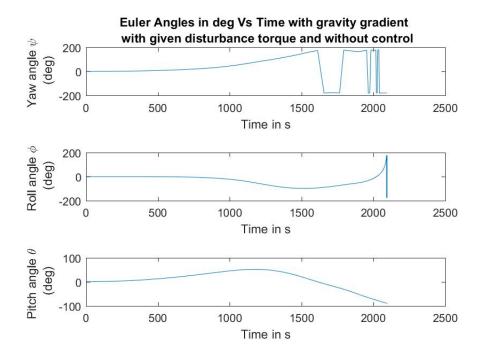
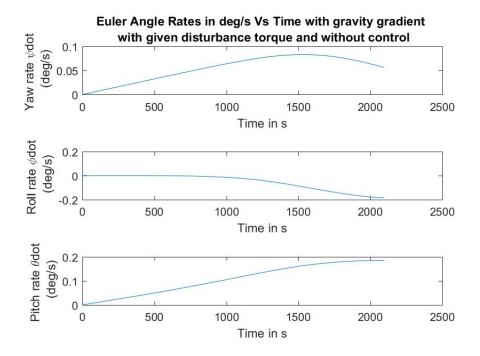


Figure 2.2.14:



 $\mathrm{Figure}_{1} \underline{2}.2.15 :$ 

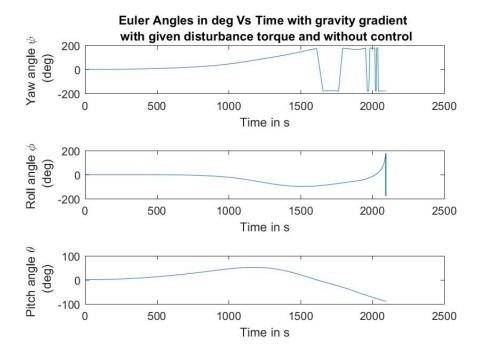


Figure 2.2.16:

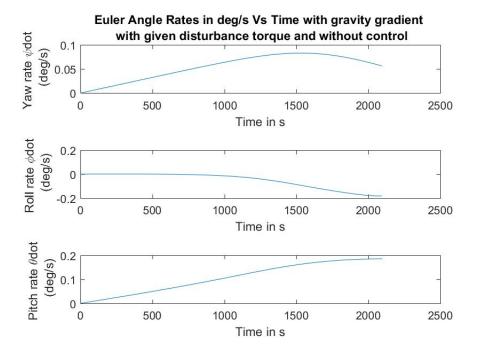


Figure 2.2.17:

As the gravity gradient torques are applied along with the given disturbances, euler angles and rates both diverge with time as indicated by above plots.

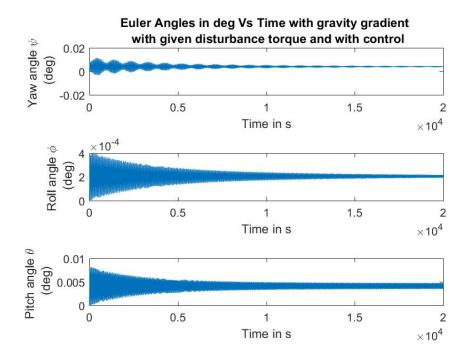


Figure 2.2.18:

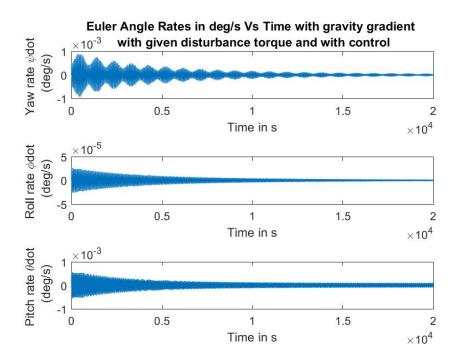


Figure 2.2.19:

Even in the presence of gravity gradient torque and external disturbances, the steady state errors of Euler angles and Rates are well within  $0.005 \, \deg$  and  $0.005 \, \deg/s$ .

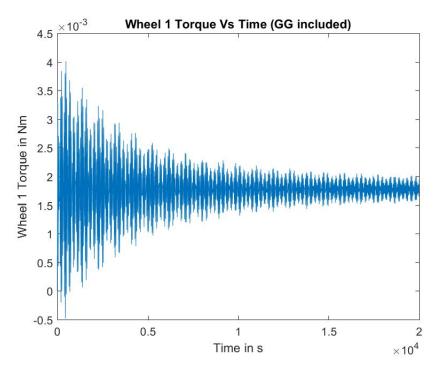


Figure 2.2.20:

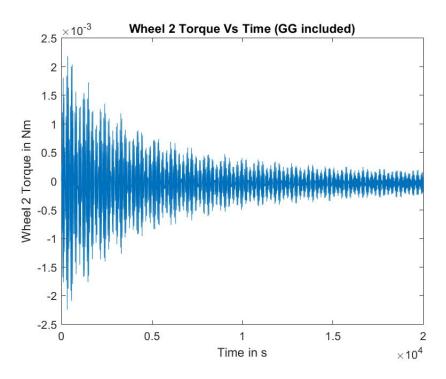


Figure 2.2.21:

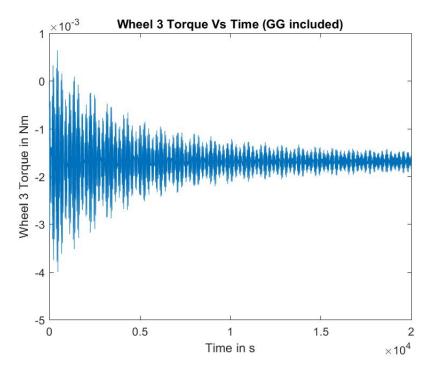


Figure 2.2.22:

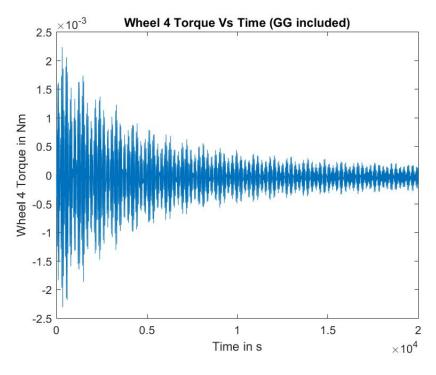


Figure 2.2.23:

From the above plots it is very clear that the torque level for none of the wheels reached 0.5 Nm, hence there is no requirement of momentum dumping even in the presence of gravity gradient torques and external disturbances.

### 2.3 Conclusion

A modified PD controller was used to control Astrosat to make it stable given a small disturbance. The gains  $K_p$  and  $K_d$  were set so that the steady state errors in the euler angles do not exceed 0.005 degrees. Quaternions and momentum dumping strategies are also addressed in this report apart from Euler angles approach.

# Bibliography

- [1] Spacecraft Dynamics and Control Marcel J.Sidis
- [2] Spacecraft Dynamics and Control Anton de Ruiter, Christopher Dameren, James Forbes