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Phase transition detection without order parameters

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Abstract

Phase transitions are critical points in the thermodynamic behavior of many physical systems. Detecting phase transitions accurately is important for understanding and predicting the behavior of such systems. However, it is not always possible to obtain the order parameter for a given system, especially near the phase boundary. In this report, we propose 13 nachine learning approach for phase transition detection, which can be applied to study the second order phase transition for the 2d Ising model without the being provided an order parameter, by employing a convolutional neural network.

1 Introduction

Traditionally, phase transitions are detected by analyzing the thermodynamic properties of a system, such as its specific heat, susceptibility, or magnetization. However, this approach can be challenging for complex systems with high-dimensional thermodynamic properties. In recent years, machine ning has shown great promise in analyzing complex bystems and detecting phase transitions. Machine learning approaches have been used to analyze the spin configurations of the Ising model and the XY model 3.

In this project, we propose a machine learning approach for phase 9 nsition detection that can be applied to a wide range of physical systems. Specifically, we employ a convolutional neural network 11 N) to classify the phases of a given system based on its thermodynamic properties. We simulated the 2D ising model using Metropolis Hastings algorithm, and run a CNN algorithm using tensorflow to detect order in the system and predict on which side of T_c the system lies.

2 Theory

2.1 Ising Model

The mo 5 consists of a lattice of spins, where each spin can be either up or down. The energy of the system is given by the Hamiltonian

$$H = -J\sum_{\langle i,j\rangle} s_i s_j - h\sum_i s_i,\tag{1}$$

where s_i is the spin at site i, J is the interaction strength between 7 ighboring spins, $\langle i,j \rangle$ denotes the sum over neighboring sites, and h is an external magnetic field. The Ising model exhibits a phase transition between a ferromagnetic phase, where all spins are aligned, and a paramagnetic phase, where the spins are randomly oriented. The magnetisation is given as:

$$M = \frac{1}{N} \sum_{i=1}^{N} s_i \tag{2}$$

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from where we can get the critical temperature T_c as:

$$\frac{kT_c}{J} = \frac{2}{\ln(1+\sqrt{2})}\tag{3}$$

2.2 Metropolis Algorithm

We initialize a two-dimensional lattice of spins, with each spin randomly oriented up or down. We then choose a spin at random and propose a new orientation for that spin. We compute the change in energy ΔE resulting from the proposed change in orientation, and use the Metropolis acceptance thereion to decide whether to accept or reject the proposed change.

The acceptance probability for a proposed spin flip is given by:

$$P_{\text{accept}} = \min \left(1, e^{-\Delta E/T} \right)$$

where ΔE is the change in energy resulting from the proposed spin flip, and T is the temperature 2 the system. If the change in energy ΔE is negative, indicating that the proposed change lowers the energy of the system, then the spin 2 p is accepted. If the change in energy ΔE is positive, indicating that the proposed change raises the energy of the system, then the spin flip is accepted with a probability proportional to $e^{-\Delta E/T}$ and continue the process till equilibrium is reached.

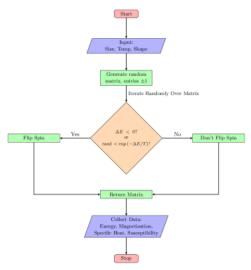


Figure 1: Flowchart depicting the metropolis algorithm [2]

3 Study of a few related works

We were interested in studying phase transitions using machine learning after being in 1 duced to 5, where neural networks were seen to be able to identify phase transitions occurring for systems where the Hamiltonian and the order parameters were not kn 1 m. In this work, two different CNNs were used to identify the occurrence of two different types of quantum phase transitions in case of ultracold quantum gases. The first set of experiments, we have the Haldane model on the honeycomb lattice, where based on the shaking frequency (ω) and the shaking plus (ϕ) , we get an order parameter known as the Chern number C which can be equal to 0 and ± 1 . There is no physical model to obtain the this quantity from single images. The CNN is trained on a dataset consisting of images taken far away from phase boundaries. The full two-dimens (44) 12 se diagram for the Haldane model was successfully mapped out this way. Similarly, in case of the superfluid-to-Mott-insulator transition, the superfluid phase probability (P_{SF}) acts as an order parameter as the lattice depth is varied. However, here the order parameter is seen to vary smoothly across the phase boundary. This leads to questions about what exactly leads a CNN to deduce the presence of a phase transition and a phase boundary.

In [6], a CNN was implemented to study the correlation between the tempe 4 ure and the spin configuration in case of the 2d Ising model. It was seen that their CNN was able to identify the defining feature of a phase transition for this case, i.e., the order parameter. Along with this, they also came up with a weight matrix that acted in a manner analogous to the order parameter, obtaining the critical temperature (as per the standard statistical mechanics calculation) very accurately. They contrasted the performance of fully-connected neural networks (FNNs) and CNNs and found that FNNs did reasonably well. However, the dataset used for training consisted of data produced at temperatures ranging across the phase boundary.

4 Baseline

We ran a sequential CNN (Tensorflow 2.11 11) to check the presence of a phase transition on snapshots for the 2d Ising 3 odel, when the CNN is trained on snapshots away from the phase boundary. The CNN model consists of two convolutional layers with 32 and 64 filters, respectively, followed by max poo 9 g layers, a flatten layer, and two fully connected layers with 64 neurons and 1 neuron respectively. The output layer uses sigmoid activation to output a probability of the system being in the ordered phase. We compile the model with binary crossentropy loss and Adam optimizer, and train it for 10 epochs with 20% of the data used for validation.

5 Experiments

5.1 GitHub

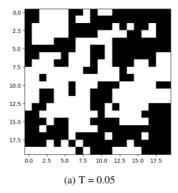
The dataset and the code is available on this repository

5.2 Description

We wanted to train the CNN on a dataset where the snapshots were taken away from the phase boundary in order to see how well it performs for snapshots that were taken near the phase boundary. The training and testing datasets were prepared accordingly.

5.3 Dataset

We produced 41,000 snapshots from Ising model simulations. 20,000 of these were produced below the critical temperature ($T_c \approx 2.27$), between T = 0.05 and T = 1.00 (see 2a and 2b). 21,000 of these were produced above T_c , between T = 3.00 and T = 4.00 (see 3a and 3b). The first set of snapshots were labelled to be in the ordered phase while the second was labelled as disordered.



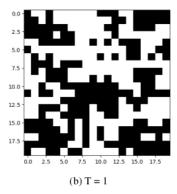
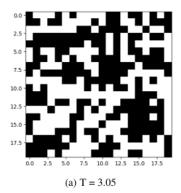


Figure 2: Snapshots of 2d ising model below T_c showing ordered states

In the ordered phase, one can see formation of larger islands of homogeneous spins, whereas in the disordered phase, noise appears to dominate.



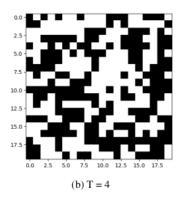


Figure 3: Snapshots of 2d ising model above T_c showing disordered phase

5.4 Training

Training accuracy and loss follows a clear trend (increasing and decreasing respectively). Final training accuracy was 97.46%. Final training loss was 0.0665 However, validation accuracy and loss were not as consistent in terms of showing a trend (see 4a and 4b)

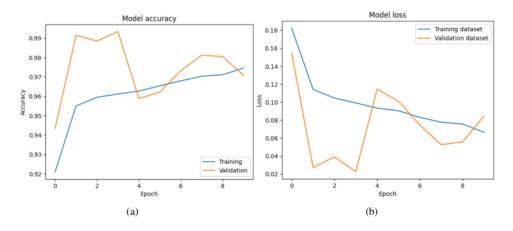


Figure 4: Model accuracy and model loss for the sequential CNN

5.5 Testing

The baseline model was able to distinguish between ordered and disordered phase snapshots with an accuracy of 100% when tested on snapshots within the temperature ranges the CNN was trained on (50 samples). For temperature ranges much closer to Tc, the model was accurate 76% of the time (50 samples). For a second order transition, there is a bit of smoothness to the change in magnetisation with respect to temperature, hence some confusion is expected near T_c .

6 Further plans

- 1. To obtain the weight matrix as a function of temperature as seen in [6]
- 2. To study difference in results for a long range spin interaction case
- 3. Attempt to train the code on variations of the Ising model (XY model, Potts and triangular)
- 4. Running the data on experimental data from the Ultracold Gas at SPS

References

- [1] M. Abadi, A. Agarwal, P. Barham, E. Brevdo, Z. Chen, C. Citro, G. S. Corrado, A. Davis, J. Dean, M. Devin, S. Ghemawat, I. Goodfellow, A. Harp, G. Irving, M. Isard, Y. Jia, R. Jozefowicz, L. Kaiser, M. Kudlur, J. Levenberg, D. Mané, R. Monga, S. Moore, D. Murray, C. Olah, M. Schuster, J. Shlens, B. Steiner, I. Sutskever, K. Talwar, P. Tucker, V. Vanhoucke, V. Vasudevan, F. Viégas, O. Vinyals, P. Warden, M. Wattenberg, M. Wicke, Y. Yu, and X. Zheng. Tensor-Flow: Large-scale machine learning on heterogeneous systems, 2015. Software available from tensorflow.org.
- [2] D. Bennett. Numerical solutions to the ising model using the metropolis algorithm. 2016.
- [3] P. Broecker, J. Carrasquilla, R. G. Melko, and S. Trebst. Machine learning quantum phases of matter beyond the fermion sign problem. *Scientific Reports*, 7(1):8823, Aug. 2017.
- [4] J. Carrasquilla and R. G. Melko. Machine learning phases of matter. *Nature Physics*, 13(5):431–434, feb 2017.
- [5] B. S. Rem, N. Käming, M. Tarnowski, L. Asteria, N. Fläschner, C. Becker, K. Sengstock, and C. Weitenberg. Identifying quantum phase transitions using artificial neural networks on experimental data. *Nature Physics*, 15(9):917–920, Sept. 2019. Number: 9 Publisher: Nature Publishing Group.
- [6] A. Tanaka and A. Tomiya. Detection of Phase Transition via Convolutional Neural Networks. Journal of the Physical Society of Japan, 86(6):063001, June 2017. Publisher: The Physical Society of Japan.

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PRIMARY SOURCES

- Benno S. Rem, Niklas Käming, Matthias Tarnowski, Luca Asteria et al. "Identifying quantum phase transitions using artificial neural networks on experimental data", Nature Physics, 2019
- S. W. Sides. "Kinetic Ising system in an oscillating external field: Stochastic resonance and residence-time distributions", Journal of Applied Physics, 1997 $_{\text{Crossref}}$
- $\frac{\text{www.teses.usp.br}}{\text{Internet}} 23 \, \text{words} 2\%$
- Akinori Tanaka, Akio Tomiya. "Detection of Phase Transition via Convolutional Neural Networks",

 Journal of the Physical Society of Japan, 2017

 Crossref
- Vladimir V. Kornyak. "Chapter 19 Symmetries and Dynamics of Discrete Systems", Springer Science and Business Media LLC, 2007
- deepai.org
 Internet

 18 words 1 %
- Julian Arnold, Frank Schäfer. "Replacing Neural Networks by Optimal Analytical Predictors for the 16 words 1%

Detection of Phase Transitions", Physical Review X, 2022

Crossref

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