

### What is Intelligence?

- □ Physics:
  - Branch of science concerned with the nature and properties of matter and energy.
- □ Chemistry:
  - Branch of science concerned with the substances of which matter is composed, the investigation of their properties and reactions, and the use of such reactions to form new substances.
- □ Intelligence:
  - \* Capacity to learn and solve problems Webster dictionary
  - To learn, reason, understand and similar form of mental activity
  - The ability to act rationally
- $\hfill \square$  Hmm... Not so easy to define

4/4/2024



Homo sapiens— "human the wise"

pra-sâmi

### How do we think...

- □ Ever understood "how we think..."
  - How a mere handful of matter can perceive, understand, predict, and manipulate a world far larger and more complicated than itself
  - Is it possible for machines to act intelligently in the way that people do?
  - Would such machines have real, conscious minds?
  - Still a big question...
- Add couple of more questions
  - \* What are the ethical implications of intelligent machines in day to-day use?
  - Should machines be allowed to decide to kill humans?
  - Can algorithms be fair and unbiased?
  - What will humans do if machines can do all kinds of work?
  - Should machines become more intelligent than us, how do we control them?
- □ Al attempts not just to understand but also to build intelligent entities

Philosophy and Computer Science

pra-sâmi

### Computer Science and Philosophy "I don't see that human intelligence is something that humans can never understand." - John McCarthy, March 1989 □ Computer Science and Philosophy are coming together ❖ Artificial intelligence (AI), Logic, \* Robotics, Virtual reality, etc. ☐ Two disciplines share a broad focus on \* The representation of information and rational inference, Embracing common interests in > Algorithms, ➤ Cognition, > Intelligence, ➤ Language, > Models, > Proof and Verification 4/4/2024 pra-sâmi

### Computer Science and Philosophy

- □ Philosophy of a Science
  - Philosopher analyze a concept
  - \* Comment on concepts being coherent or not!
- ☐ AI has closer connection with philosophy compared to any other science
- □ Shared concepts are:
  - Action
  - Consciousness
  - Epistemology
  - Free will
- □ Al Point of view
  - Use the philosophical theories without precluding human level AI
  - Do not obstruct development

*pra-sâmi* 

### Think about a computer(Read AI System)!

- □ Epistemology:
  - What can we know about a Computer?
  - How can we justify our beliefs about Computer?
  - \* Can a Computer have Knowledge?
- Metaphysics:
  - \* What kind of thing a Computer is?
  - ❖ Does it have free will?
  - How does it relates to its parts?
  - ❖ Is it necessary or contingent?

- □ Ethics:
  - Is Computer Good or bad?
  - How can we use a Computer for good or bad?
- □ Philosophy of Mind:
  - Does Computer have consciousness?
- □ Philosophy of Art
  - ❖ Is it beautiful?
  - ❖ Is it sublime?

### Philosophical Criticisms of Al

- ☐ Two categories of criticism:
  - \* It cannot be done because ...
  - It cannot be done the way you are trying to do it...

Generative Pre-trained Transformer (GPTs) have arrived, would become better over time

- ☐ The danger of "can't be done" arguments...
  - Philosophers are forever telling scientists what they can't do, what they can't say, what they can't know, and so on and so forth
- In 1844 the philosopher August Compte said that if there was one thing man would never know it would be the composition of the distant stars and planets
- But three years after Compte died physicists discovered that an object's composition can be determined by its spectrum no matter how far off the object happens to be
- Simon Newcomb, who in October 1903 wrote "aerial flight is one of the great class of problems with which man can never cope"
  - Two months later, the Wright brothers' flew an aircraft at Kitty Hawk
- ☐ Air Travel arrived in 1903, of course took time to perfect it

pra-sâmi

10



.1

### Computer Science and Philosophy

- ☐ When it comes to philosophy of mind, AI offers advice to philosophers
- □ Key problem is `Common Sense`
- ☐ How to take decision in absence of complete picture
  - · Without having access to full observation or
  - \* For ill-defined problems

4/4/2024

pra-sâmi

12

### Computer Science and Philosophy

- □ The study of Philosophy develops analytical, critical and logical rigor, and the ability to think through the consequences of novel ideas and speculations
- □ It stretches the mind by considering a wide range of thought on subjects as fundamental as the limits of knowledge, the nature of reality and our place in it, and the basis of morality
- □ Philosophers need to understand a world increasingly shaped by technology, in which a whole new range of enquiry has opened up, from the philosophy of AI, to the ethics of privacy and intellectual property
- □ Some of the greatest thinkers of the past including Aristotle, Hobbes and Turing dreamed of automating reasoning and what this might achieve
- Computer scientists need to be able to reflect critically and philosophically, as they push forward into novel domains
- □ The computer has now made it a reality, providing a wonderful tool for extending our speculation and understanding

4/4/2024

Do no Harm!

Limits of AI

### Limits of Al

- □ The argument from informality
  - \* Human behavior is far too complex to be captured by any formal set of rules
  - Humans must be using some informal guidelines that could never be captured in a formal set of rules
  - Thus could never be codified in a computer program
  - It turns out that argument was aimed against the simple reflex agent
- □ The argument from disability
  - ❖ A machine can never do a few things such as:
    - > Be kind, resourceful, beautiful, friendly, have initiative, have a sense of humor, tell right from wrong, make mistakes, fall in love, enjoy Vada Pav, make someone fall in love with it, learn from experience, use words properly, be the subject of its own thought, have as much diversity of behavior as man, do something really new.
  - Today's machines can do a few of stuff
    - > The one thing that it is clear they can't do is be exactly human

### Limits of AI

- □ The mathematical objection
  - Turing and Gödel proved that certain mathematical questions are in principle unanswerable by particular formal systems. Gödel's incompleteness theorem is the most famous example of this.
- □ Briefly, for any formal axiomatic framework powerful enough to do arithmetic, it is possible to construct a so-called Gödel sentence with the following properties:
  - > G(F) is a sentence of F, but cannot be proved within G(F)
  - Imagine there is a village with a strict law against not shaving
    - > The village has only one barber and only barber can shave another villager
    - > The village barber must shave all men if they are incapable of shaving themselves
    - > So who shaves the barber?
    - > Barber cannot shave himself because barber is authorized to shave only people who do not shave themselves
    - > But barber can shave himself
- □ A complete formal system of mathematics is not possible!

4/4/2024

pra-sâmi

16

### Limits of Al

- □ Lack of Common Sense:
  - \* All systems generate responses based on patterns in the data they were trained on,
  - Don't truly understand the context or have the ability to think critically.
- □ Data Dependency:
  - Require vast amounts of data to train effectively. Do not perform well on tasks or domains where sufficient training data is not available.
- Bias and Fairness:
  - Inherit biases present in their training data. Leads to biased and unfair outcomes, especially in applications like hiring, lending, and law enforcement.
- Lack of Creativity:
  - Creativity is often limited to patterns it has learned from training data. It cannot truly innovate or have genuine creative insights.
- Ethical Concerns:
  - \* All can be used unethically, such as in deepfake creation or for malicious purposes.
- □ Interpretability:
  - \* Al models are "black boxes", Challenging to understand how they arrive at their decisions.

4/4/2024

### Limits of AI

- Resource Intensive:
  - \* Training and running AI models can be computationally expensive and energy-intensive
- Security Risks:
  - Can be vulnerable to attacks, including adversarial attacks where malicious inputs can fool the system into making incorrect decisions
- Scalability and Generalization:
  - While AI models can perform well in specific tasks they were trained on, they may struggle to generalize to new, unseen situations or tasks
- □ Human-AI Collaboration:
  - Al is often seen as a replacement for human jobs, but it can also create job displacement and challenges in integrating Al systems with human workers
- □ Legal and Regulatory Challenges:
  - The rapid development of AI has posed legal and regulatory challenges, including questions about liability and accountability when AI systems make errors or cause harm

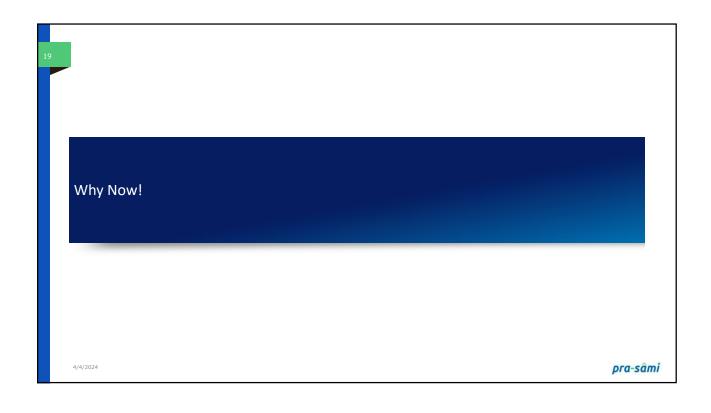
pra-sâmi

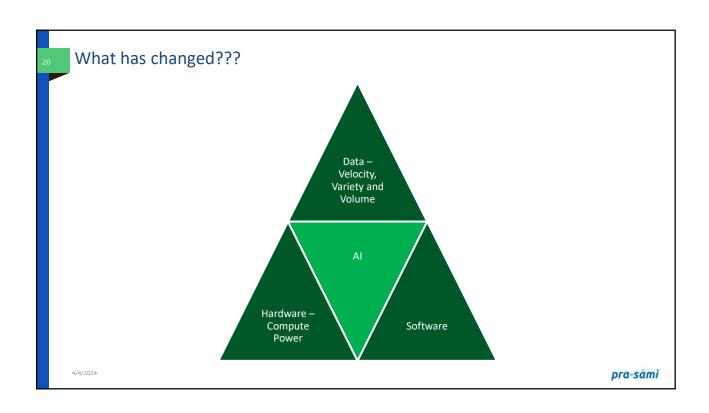
18

### Objections to the Al

- ☐ The Theological Objection
  - "Thinking is a function of man's immortal soul. God has given an immortal soul to every man and woman, but not to any other animal or to machine. Hence no animal or machine can think."
- ☐ The "Head in the Sand" Objection
  - "The consequences of machines thinking are too dreadful to think about."
- ☐ The Argument for Consciousness
  - "A machine cannot write a sonnet or compose a concerto because of thoughts or emotions felt."
- Robotic Limitations:
  - . Physical robots have limitations in terms of mobility, dexterity, and interaction with the physical world.
  - Still far from matching human capabilities in many real-world scenarios.

4/4/2024





### **Cambrian Explosion**

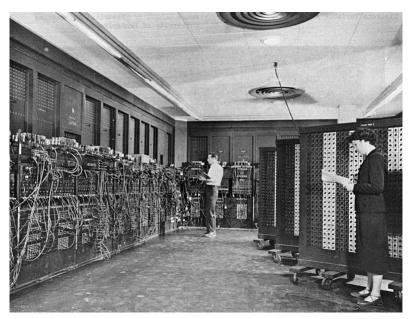
- Current period of fervent innovation
- □ Range of innovative AI hardware-accelerator architectures continues to expand.
  - ❖ GPU is not the only one
- □ New Al-optimized chipset architectures:
  - ❖ New generations of GPUs
  - Neural network processing units (NNPUs)
  - Field programmable gate arrays (FPGAs),
  - \* Application-specific integrated circuits (ASICs), and
  - Various related approaches that go by the collective name of neurosynaptic architectures.

4/4/2024

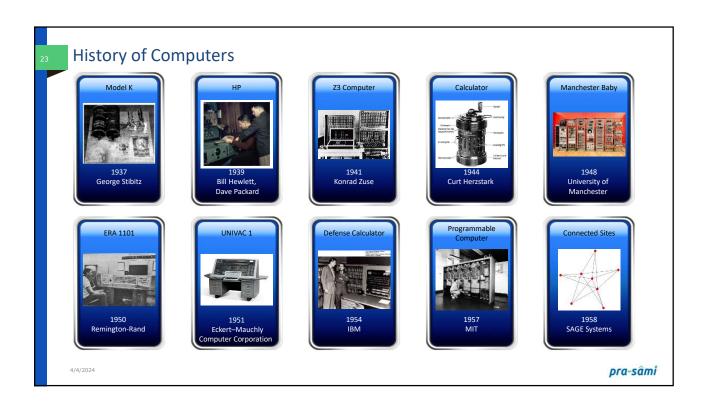
pra-sâmi

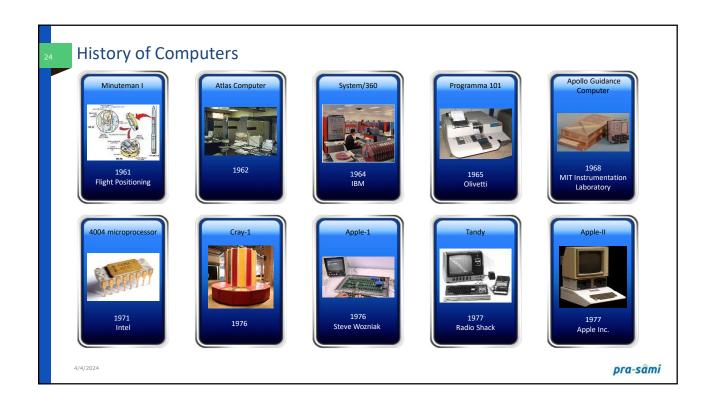
2

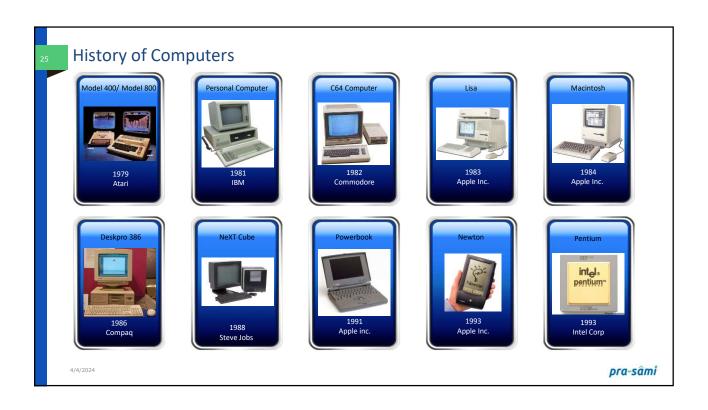
### **ENIAC** - Electronic Numerical Integrator and Computer



4/4/2024









## History of Computers







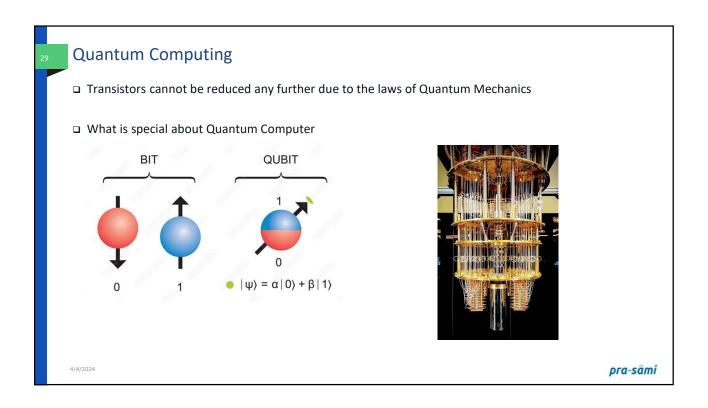


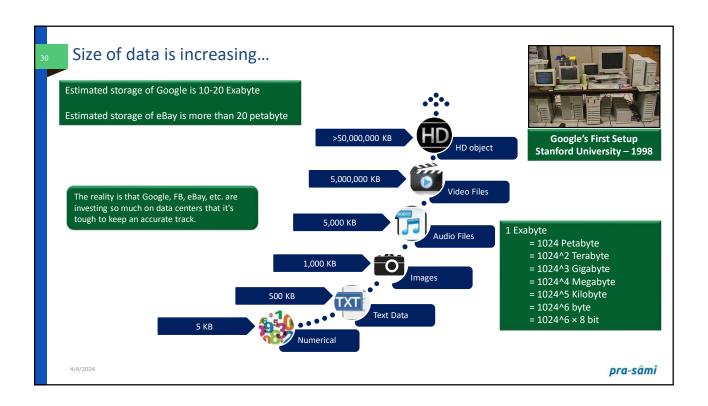


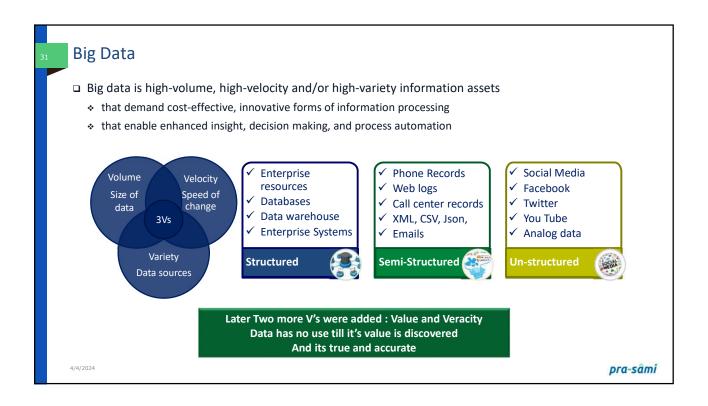
pra-sâmi

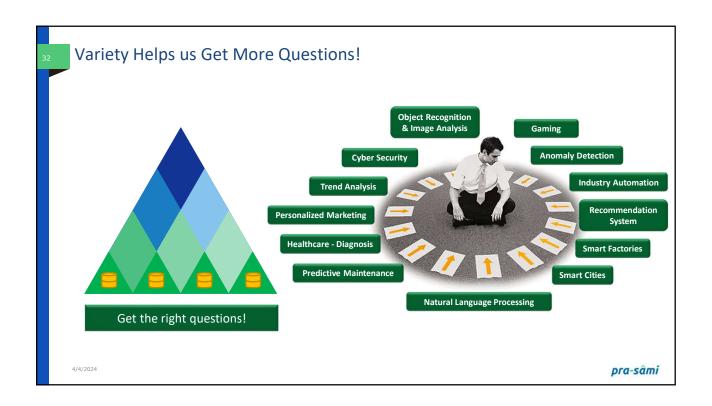
### Better and Better Hardware

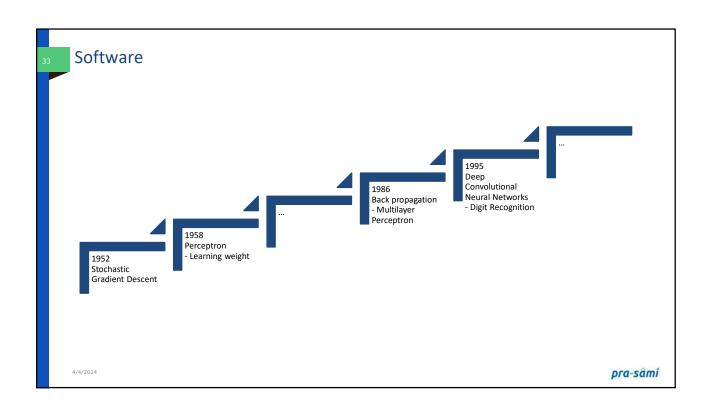
- ☐ Graphic processing units (GPU), in 2007, NVIDIA launched CUDA It is Massively Parallelized
- □ Between 1990 and 2010, off-the-shelf CPU's became approx. 5000 times faster
- ☐ Around 2011, some researchers began to write CUDA implementations of neural nets
- □ NVIDIA TITAN X , a gaming GPU can deliver a peak of 6.6 TFLOPS in single precision: 6.6 trillion float32 operations per second.
  - 350 times more than what you can get out of a modern lap-top
- □ Beyond GPU → TPU: specially designed hardware for neural networks about 10 times faster than GPU.
- □ 2016: The first reprogrammable quantum computer was created
- 2017: The Defense Advanced Research Projects Agency (DARPA) is developing a new "Molecular Informatics" program that uses molecules as computers



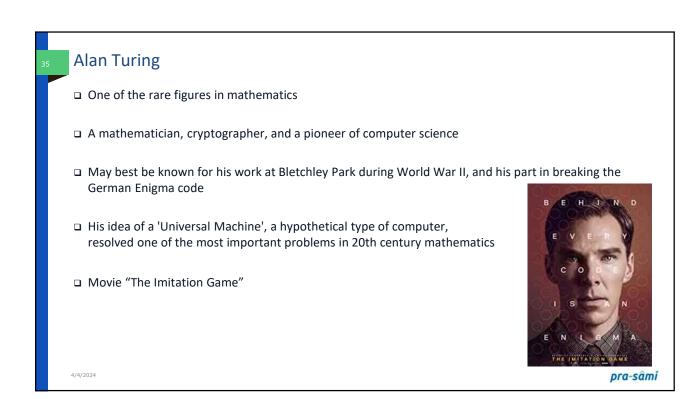


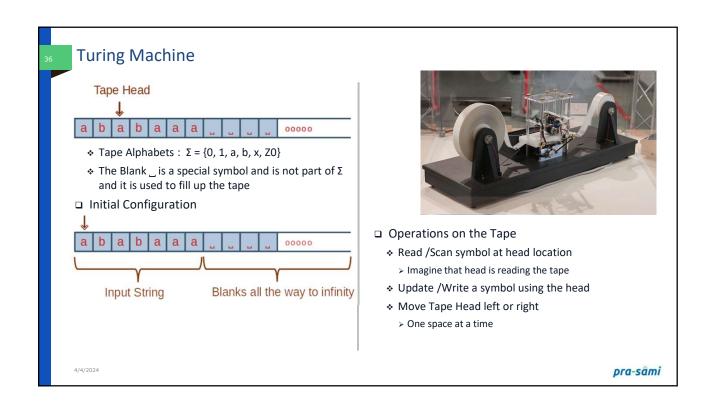


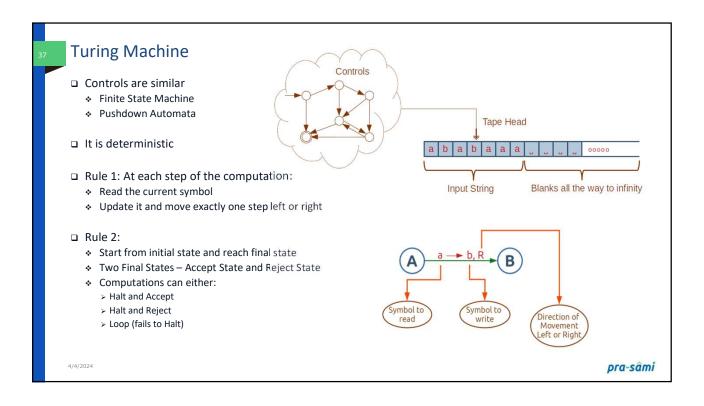




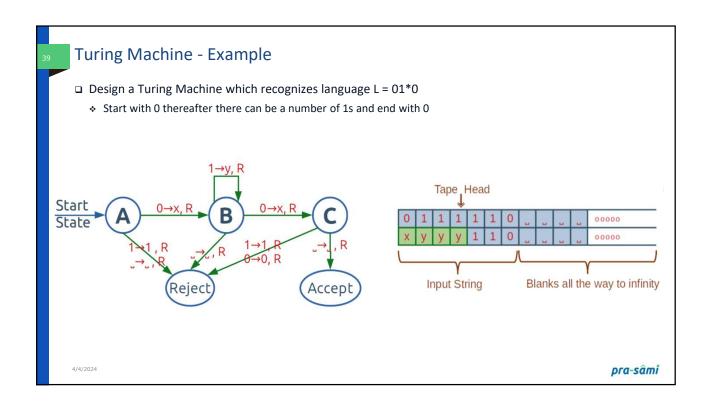


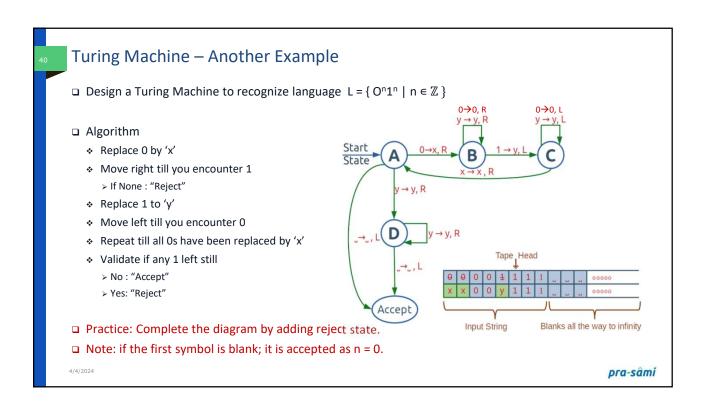






## Turing Machine - Defined a Turing Machine can be defined as a tuple of seven The tuple is $(Q, \Sigma, \Gamma, \delta, q_0, b, F)$ , where $Q: A \text{ finite set of States - Non-empty only } \{A, B, C, D, ...\},$ $\Sigma(\text{sigma}): A \text{ finite set of non-empty Symbols } \{1, 0, x, y, ...\}$ $\Gamma(\text{gamma}): A \text{ finite Tape Symbols}$ $\delta(\text{delta}): \text{The transition Function, } Q \times \Sigma \to \Gamma \times (L/R) \times Q$ $q_0: \text{Initial State,}$ b: Blank Symbol, F: set of Final State (Accept or Reject)Production Rule can be written as: $\delta(q_0, \alpha) \to (q_1, \gamma, R)$





### **Turing Thesis**

- □ Turing's Thesis states that any computation that can be carried out by mechanical means can be performed by some Turing Machine
- Explanation
  - \* Anything that can be done on existing digital computer can also be done by Turing Machine
  - No one has yet been able to suggest a problem solvable by what we consider an algorithm, for which a Turing Machine Program cannot be written

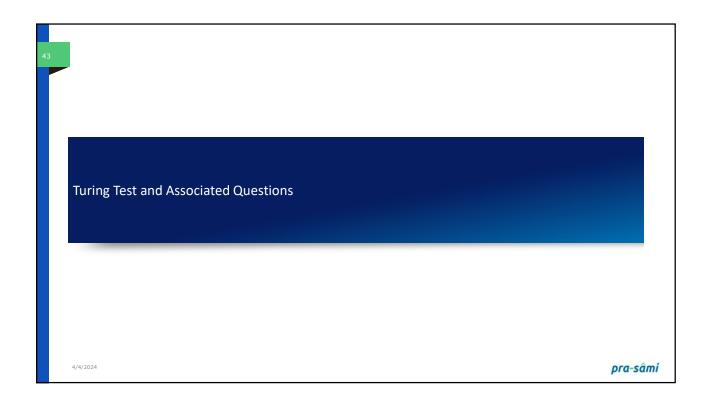
pra-sâmi

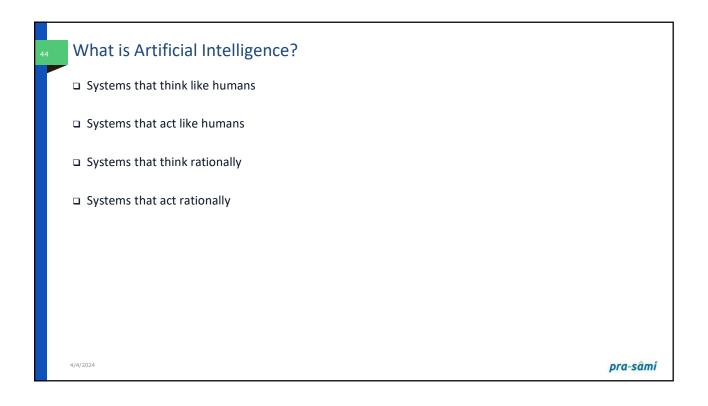
12

### PA\_FAI\_01: Construct a Turing Machine

- □ Construct a Turing Machine for the language  $L = \{0^n1^n2^n\}$  where  $n \ge 1$
- Answer to include
  - \* Algorithm
  - Representative transition diagram
  - ❖ Initial Tape and Final Tape
  - Similar to what you saw in slides 29 and 30
- Submission:
  - PDF or Image to be uploaded in the shared drive
  - Upload file Name: PRN\_
    last 4 digits of PRN>\_.

4/4/2024



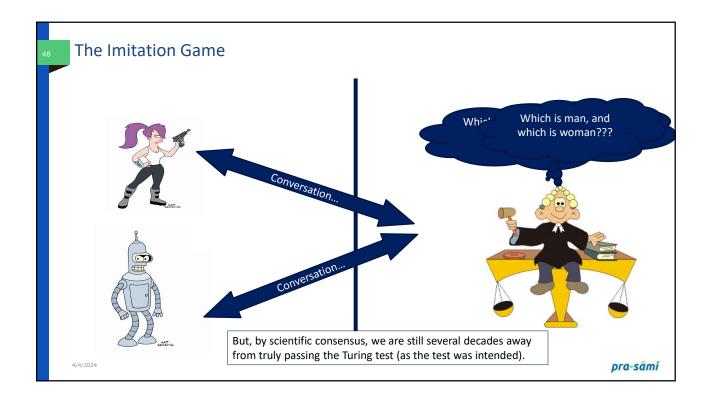


### What is AI? □ Views of AI fall into four different perspectives --- two dimensions: Thinking versus Acting Human versus Rational "Ideal" Intelligent/ **Human-like Pure Rationality** Intelligence Thought/ Reasoning 2. Thinking Humanly 3. Thinking Rationally ("modeling thought" "brain") **Behavior/Actions** "behaviorism", "mimics 1. Acting Humanly 4. Acting Rationally behavior" 4/4/2024 pra-sâmi

Acting Humanly  Views of AI fall into four d  Thinking versus Acting  Human versus Rational	ifferent perspectives two dir	mensions:	
	Human-like Intelligence	"Ideal" Intelligent/ Pure Rationality	
Thought/ Reasoning ("modeling thought" "brain")	2. Thinking Humanly	3. Thinking Rationally	
Behavior/Actions "behaviorism", "mimics behavior"	1. Acting Humanly	4. Acting Rationally	
4/4/2024			pra-sâmi

### Acting Humanly: The Turing Test

- □ Turing (1950) "Computing machinery and intelligence"
  - "Can machines think?"; "Can machines behave intelligently?"
  - \* Operational test for intelligent behavior: the Imitation Game



### Acting Humanly: The Turing Test

- □ "Imitation Game"
  - Method
    - > Three people play (man, woman, and interrogator)
    - > Interrogator determines which of the other two is a woman by asking questions
      - Example: How long is your hair?
    - > Questions and responses are typewritten or repeated by an intermediary
    - > Turing Test: Machine takes the part of the man
  - \* Al system passes if interrogator cannot tell which one is the machine.
  - \* No computer vision or robotics or physical presence required!
  - Predicted that by 2000, a machine might have a 30% chance of fooling a lay person for 5 minutes

4/4/2024

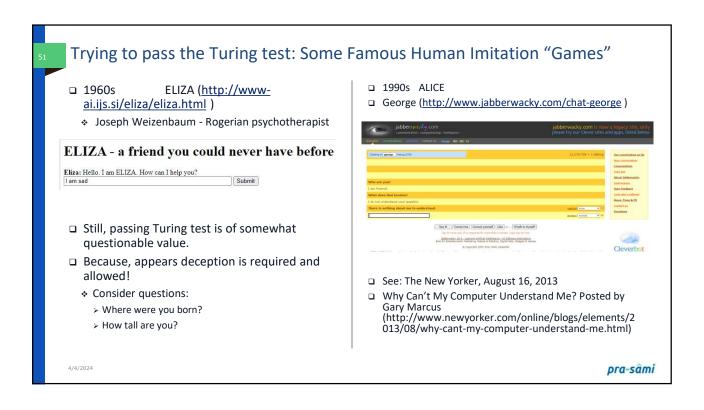
pra-sâmi

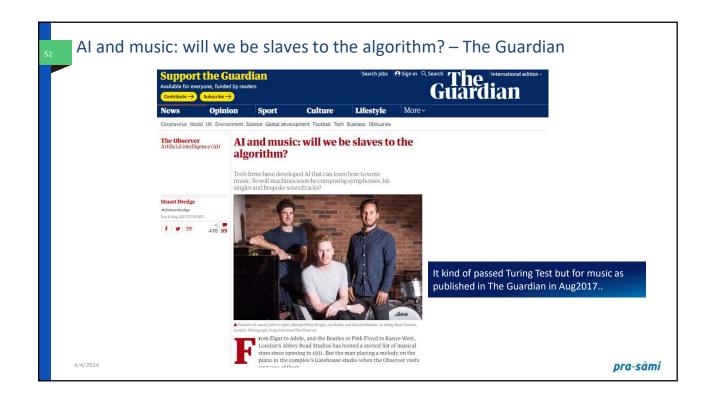
50

### **Predictions**

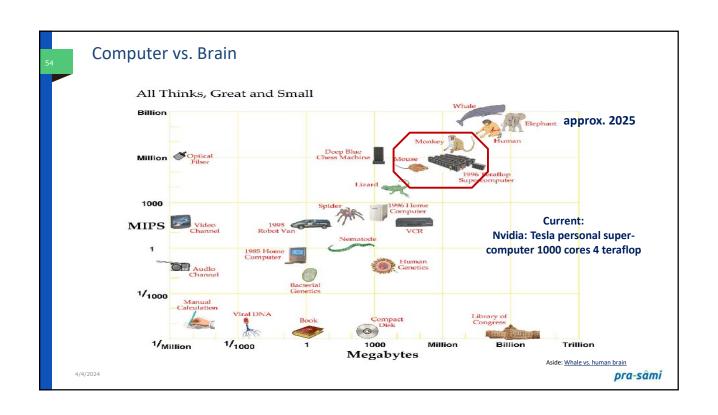
- □ In 1950, Turing predicted that 50 years later it will be possible to program a computer with ~100 Mb memory to pass TT 70% of the time, with 5 minute conversations.
- □ It will be natural to speak of computers 'thinking'.
- □ "[The machine] may be used to help in making up its own programs, or to predict the effect of alterations in its own structure."
- □ "We may hope that machines will eventually compete with men in all purely intellectual fields."

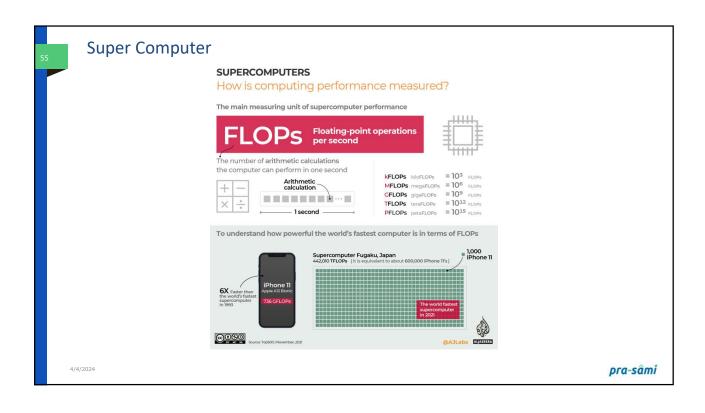
4/4/2024





	Human-like Intelligence	"Ideal" Intelligent/ Pure Rati	onality
Thought/ Reasoning ("modeling thought" "brain")	2. Thinking humanly <ul><li>Cognitive Modeling</li></ul>	3. Thinking Rationally	
Behavior/Actions "behaviorism", "mimics behavior"	1. Acting Humanly	4. Acting Rationally	
☐ Requires scientific theories	s of internal activities of the br	ain.	
<ul><li>Cognitive Science (top-dov</li><li>Predicting and testing beh</li></ul>		mental techniques from psycho	logy
□ Cognitive Neuroscience (b	ottom-up): Direct identification	on from neurological data	
Cog	nitive Science and Cognitive Neurosci Cognitive Neuroscience has beco		
		MSR / Facebook AI Lab efforts.)	





## Super Computers

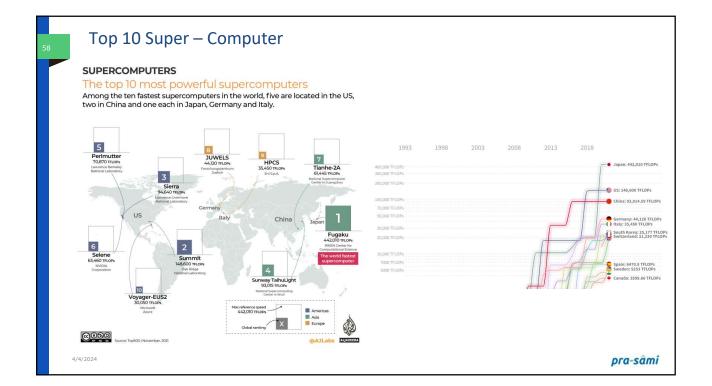
- □ The US has retaken the top spot in the race to build the world's fastest supercomputer
- □ 'Frontier' is capable of more than a billion billion operations a second, making it the first exascale supercomputer.
- □ Supercomputers have been used to discover more about diseases including COVID-19 and cancer.
- □ Fun fact: there might be faster supercomputers out there whose operators didn't submit their systems to be ranked.

4/4/2024

### **Super Computers**

- □ Frontier: Built by Hewlett Packard Enterprise (HPE) and housed at the Oak Ridge National Laboratory (ORNL) in Tennessee, USA
- Fugaku: Previously held the top spot, is installed at the Riken Center for Computational Science in Kobe, Japan. It is three times faster than the next supercomputer in the top 10
- □ LUMI: New number 3, crunching the numbers in Finland
- □ Summit (IBM): is also at ORNL in Tennessee
- Sierra: Installed at the Lawrence Livermore National Laboratory in California, which is used for testing and maintaining the reliability of nuclear weapons
- Sunway TaihuLight: A system developed by the National Research Center of Parallel Computer Engineering and Technology and installed in Wuxi, Jiangsu
- □ Perlmutter: another top 10 entry based on HPE technology
- Selene : currently running at AI multinational NVIDIA in the US
- u Tianhe-2A : developed by China's National University of Defence Technology and installed at the National Supercomputer Center in Guangzhou
- □ France's Adastra is the second-fastest system in Europe and has been built using HPE and AMD technology

4/4/2024



Super Computers - India



### □ AIRAWAT

- \* Ranked 75th in the Top 500 Global Supercomputing List. The rankings were announced at the 61st edition of the International Supercomputing Conference (ISC 2023) held in Germany.
- Speed of 13,170 teraflops (Rpeak). The AI system was installed as part of the government's National Program on Artificial Intelligence

4/4/2024 **pra-sâmi** 

Three More - Super Computers India

- □ PARAM Siddhi-Al supercomputer which has been ranked 131st on the list is Installed at the C-DAC, Pune.
- □ The Pratyush supercomputer at the Indian Institute of Tropical Meteorology has secured the 169th position
- ☐ Mihir supercomputer at the National Centre for Medium-Range Weather Forecasting has been ranked 316th on the list







pra-sâmi

4/4/2024

### Super Computers - India



PARAM Utkarsh is a High Performance Computing System setup at C-DAC, Bangalore under the National Supercomputing Mission (NSM), Government of India.

- This system offers Artificial Intelligence over Machine Learning & Deep Learning frameworks, Compute and Storage as a cloud service.
- This leads to reduced turnaround time to market of MSMEs and Startup India, thereby increasing their innovation potential.
- PARAM Utkarsh is based on Intel Cascade Lake processor and NVIDIA Tesla V100 GPU with 100Gbps infiniband nonblocking interconnect.
- Equipped with 50,000+ compute cores (CPU & GPU) and liquid cooling system for efficient PUE, PARAM Utkarsh offers peak computing power of 838 Teraflops.

pra-sâmi

### Safe to assume

- □ In near future, we can have computers with as many processing elements as our brain, but:
  - Far fewer interconnections (wires or synapses)
  - Then again, much faster updates
- □ Fundamentally different hardware may be require → fundamentally different algorithms!
  - Still an open question.
  - Neural net research Can a digital computer simulate our brain?

Likely: Church-Turing Thesis
(But, might we need quantum computing?)
(Penrose; consciousness; free will)



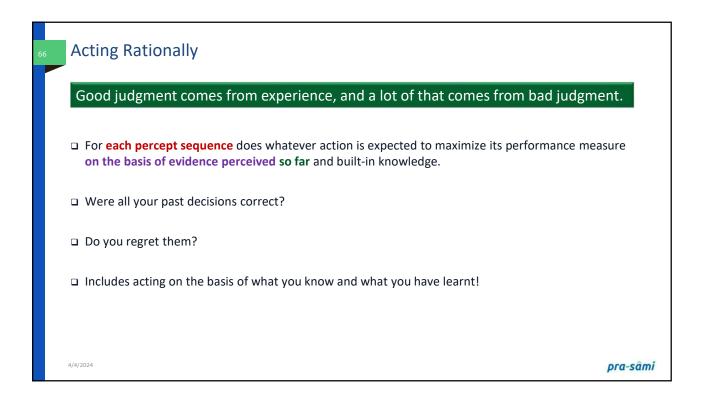
pra-sâmi

4/4/2024

Thinking Rationally **Human-like Intelligence** "Ideal" Intelligent/ Pure Rationality 3. Thinking Rationally Thought/ Reasoning 2. Thinking humanly formalizing "Laws of ("modeling thought" "brain") Thought" **Behavior/Actions** "behaviorism", "mimics 1. Acting Humanly 4. Acting Rationally behavior" □ Logic: Making the right inferences! \* Remarkably effective in science, math, and engineering. □ Several Greek schools developed various forms of logic: notation and rules of derivation for thoughts. ☐ Aristotle: what are correct arguments/thought processes? (characterization of "right thinking"). ❖ Socrates is a man, All men are mortal → Therefore, Socrates is mortal Can we mechanize it? (syntactic; strip interpretation) Use: legal cases, diplomacy, ethics etc. (?) 4/4/2024 pra-sâmi

	Human-like Intelligence	"Ideal" Intelligent/ Pure Rationality
Thought/ Reasoning "modeling thought" "brain")	2. Thinking humanly	3. Thinking Rationally
Behavior/Actions 'behaviorism" "mimics behavior"	1. Acting Humanly	4. Acting Rationally
	perceives and acts in the world out or software robot (e.g. an el	(i.e. an "autonomous system" (e.g. self- ectronic trading system))
Current focus of AI is about	ut designing rational agents	
☐ For any given class of envi performance	ronments and tasks, we seek th	e agent (or class of agents) with the bes
Caveat: computational limitations	may make perfect rationality unachieva "Limited rationality"	ble design best program for given machine resourc

# Focus I Building exact models of human cognition view from psychology, cognitive science, and neuroscience But, Focus I often provides inspiration for Focus II. Also, Neural Nets blur the separation.



### Turing Test – Loebner prize

## Loebner Prize Judges Could Easily Identify Chatbots

Written by Sue Gee Friday, 18 May 2012 08:36

The 2012 Loebner Prize for the best chatbot has been awarded to <a href="Chip">Chip</a> Vivant, created by Mohan Embar, a software consultant based in Milwaukee.

There were four contestants in the final round of this competition which took place at Bletchley Park on May 15, 2012 and none of them were likely to fool the judges into mistaking them for a human as required to win the Loebner Prize Gold Medal. So instead the Bronze Medal and \$5,000

Now where to the critical with the most impressive



Alan Turing depicted on the Loebner Prize Gold Medal

ni

pra-sâmi

4/4/2024

4/4/2024

### What is AI? □ Views of AI fall into four different perspectives --- two dimensions: Thinking versus Acting · Human versus Rational Human-like "Ideal" Intelligent/ Intelligence **Pure Rationality** Thought/ Reasoning 2. Thinking humanly 3. Thinking Rationally ("modeling thought" "brain") Seems to be a Good Idea **Behavior/Actions** "behaviorism" "mimics 4. Acting Rationally 1. Acting Humanly behavior"

### **Rational Agent**

- An agent should strive to do right thing,
  - Based on what it can perceive and the actions it can perform
- ☐ Right action is one which makes agent to be most successful
- Performance measure: An objective criterion for success of an agents behavior
- ☐ Imagine you are trying to design a vacuum-cleaner
  - · Amount of dirt gathered
  - Time taken in doing so
  - Electricity consumed
  - Noise generated
  - etc...

We will circle back to Agents later...

pra-sâmi

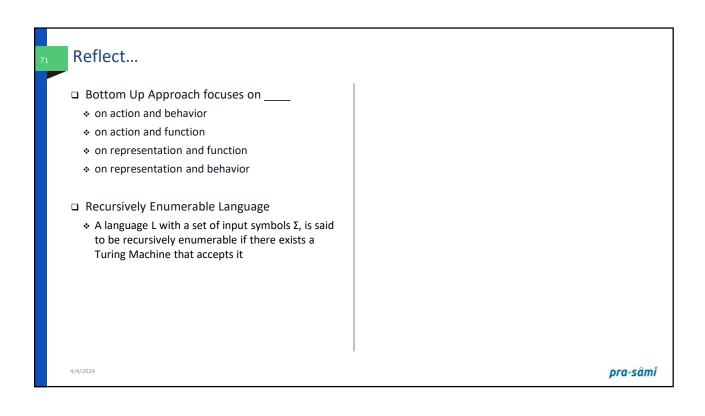
4/4/2024

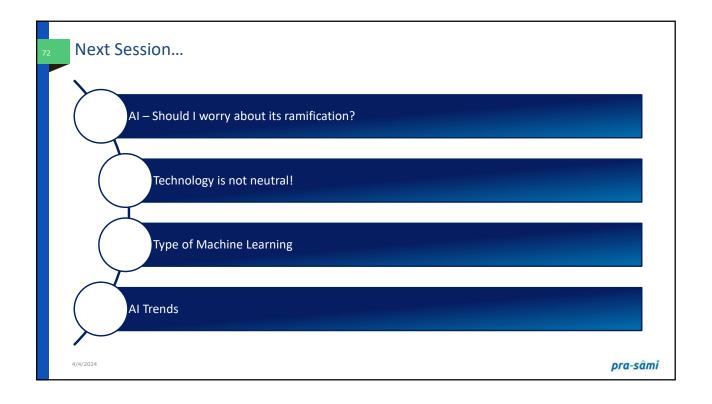
Reflect...

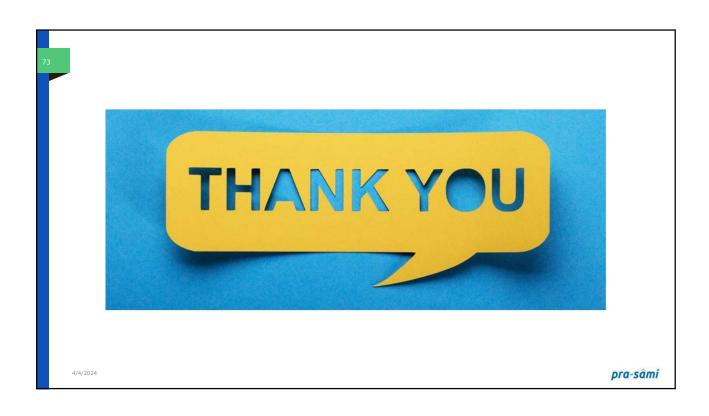
- □ Fine-tuned model from one field may not work in other field
  - ❖ True
  - ❖ False
  - ❖ Don't know
- A.M. Turing developed a technique for determining whether a computer could or could not demonstrate the artificial Intelligence, Presently, this technique is called
  - Turing Test
  - Algorithm
  - \* Boolean Algebra
  - ❖ Logarithm

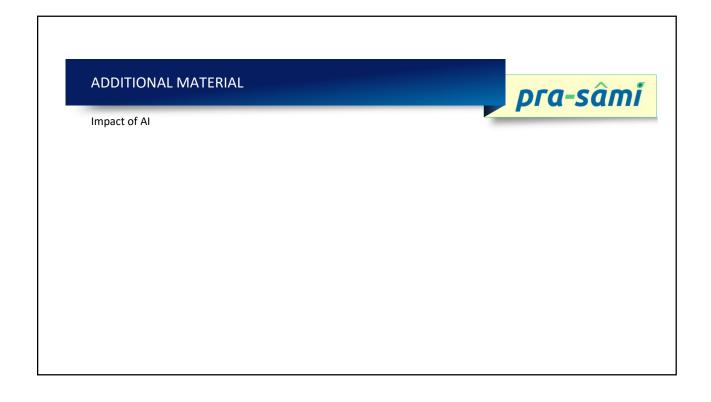
- □ What was originally called the "imitation game" by its creator?
  - ❖ The Turing Test
  - ❖ LISP
  - The Logic Theorist
  - Cybernetics
- □ Which programming language is most used for Al?
  - Python
  - Java
  - Lisp
  - ❖ R
  - ❖ Prolog

4/4/2024





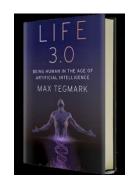




'5

# Impact of Al

- ☐ How will Artificial Intelligence affect
  - Crime, war, justice, jobs, society
  - And our very sense of being human?
- ☐ The rise of AI has the potential to transform our future more than any other technology?
- □ Life 3.0
  - Written by Swedish-American cosmologist Max Tegmark from MIT.
  - Discusses Artificial Intelligence (AI) and its impact on the future of life on Earth and beyond
  - Discusses a variety of societal implications, what can be done to Maximize
    - > the chances of a positive outcome
    - > Potential futures for humanity, technology and combinations thereof



4/4/2024

pra-sâmi

6

# How job Scenario will change?

- □ How can we grow our prosperity through automation without leaving people lacking income or purpose?
- □ What career advice should we give today?



4/4/2024

77

### Where we are!

- ☐ First phase of Life biological origins,
- Second Phase cultural developments in humanity,
  - Customs, cultures, social norms
- □ This is technical age of humans
- □ Emerging technology such as artificial general intelligence that may someday, in addition to being able to learn, be able to also redesign its own hardware and internal structure
- □ Short-term effects of the development of advanced technology
  - Technological unemployment,
  - Al weapons,
  - \* Quest for human-level AGI (Artificial General Intelligence).
- Examples
  - . Deepmind and OpenAI, self-driving cars, and AI players that can defeat humans in Chess, Jeopardy and Go.

4/4/2024

pra-sâmi

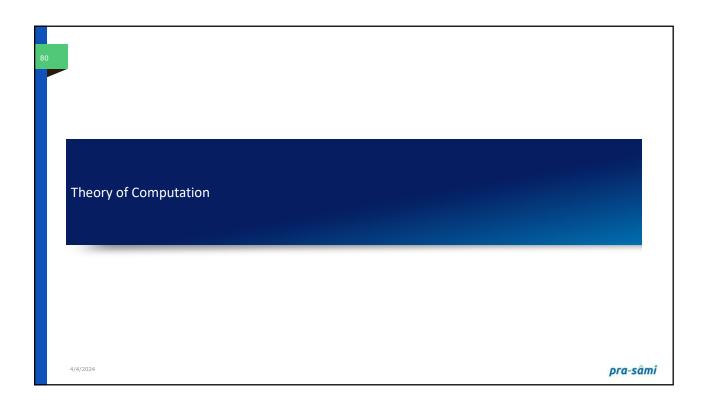
78

### Limitations

- □ Not all intelligent behavior is mediated by logical deliberation (much appears not...)
- □ (Logical) representation of knowledge underlying intelligence is quite non-trivial.
- □ Studied in the area of "knowledge representation."
- □ Also brings in probabilistic representations. E.g. Bayesian networks and graphical models.
- □ What is the purpose of thinking?
- □ What thoughts should I have?
- ☐ Seems to require some connection to "acting in the world."
- □ We ("agents") want/need to affect our environment (in part for survival)

4/4/2024

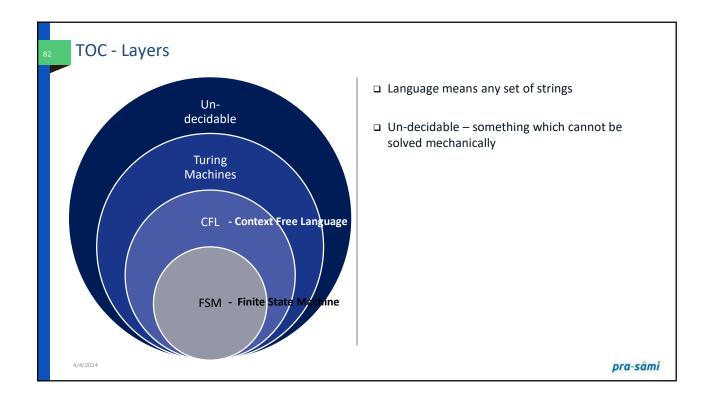
Computer Science		Philosophy	
Functional programming	Object-oriented programming	General philosophy	Ethics
Probability & Algorithms	Computational complexity	Elements of deductive logic	Philosophical logic
Imperative programming	Computer-aided verification	Turing on computability and intelligence	Philosophy of cognitive science
Discrete mathematics	Knowledge representation and reasoning		
		Knowledge and reality	Philosophy of mathematics
Models of computation	Advanced security	Early Modern philosophy	Philosophy of logic and language and many others
Compilers	Computational game theory		
Concurrent programming	Concurrent algorithms and data structures	Philosophy of science	Advanced options in Philosophy
Databases	Computational Learning Theory	Philosophy of mind	Computers in society
Intelligent systems	Quantum Computer Science		
Machine learning			

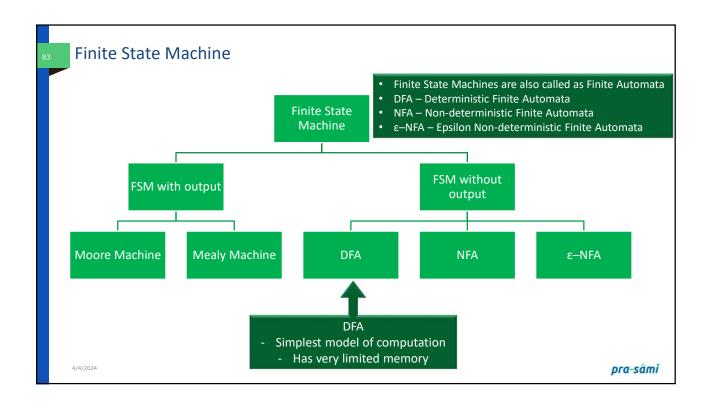


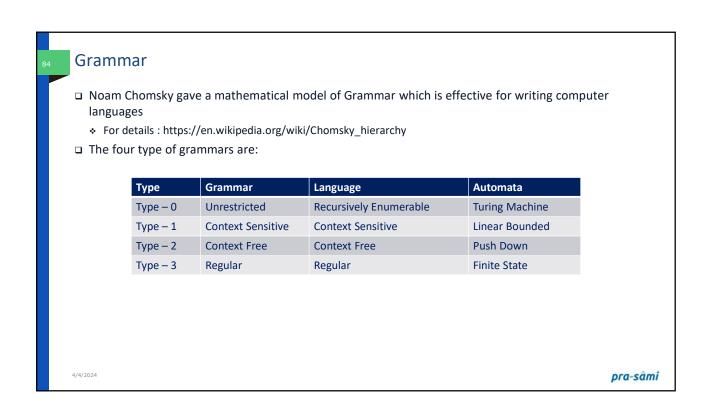
# Introduction to Theory of Computation

- □ Fundamentals of computer science
- □ What can be computed mechanically and how much space will it take
- □ There are computations that computers can do!
  - Does given binary string ends with 0?
  - Is it a valid Python script?
- □ There will always be tasks computers will not be able to perform
  - Will this code run forever (infinite loop)?

4/4/2024 **pra-sâmi** 







# Some definitions!

### Power of Sigma (Σ)

- $\Sigma^1 = \{0,1\}$

 $\Box$  For sigma ( $\Sigma$ ) = { 0, 1}

- $\Sigma^3 = \{000,001,010,100,011,101,110,111\}$
- $\Sigma^n = \{00 \dots n \text{ times}, \dots 2n \text{ terms}\} =$ Set of strings of length n

### Cardinality

- $\square$   $\Sigma^0 \rightarrow Cardinality = 1 = 2^0$
- $\square$   $\Sigma^1 \rightarrow Cardinality = 2 = 2^1$
- $\square$   $\Sigma^2 \rightarrow Cardinality = 4 = 2^2$
- $\square$   $\Sigma^3 \rightarrow Cardinality = 8 = 2^3$
- $\square$   $\Sigma^n \rightarrow Cardinality = 2^n$

4/4/2024

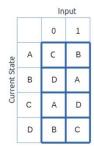
pra-sâmi

# Finite State Machine (Finite Automata)

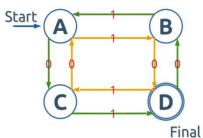
- □ Q : Set of all states = {A, B, C, D},
- □ Σ: inputs = {0, 1},

4/4/2024

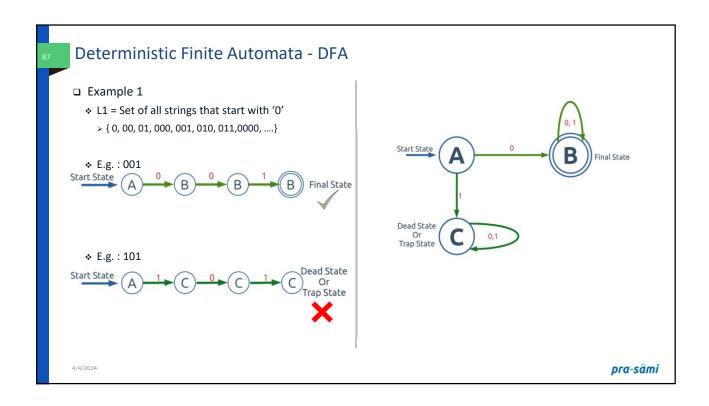
- □ q<sub>0</sub>: Start State / Initial State= A,
- □ F: Final State(s) = {D},
- $\Box$   $\delta$  = transition function from  $Q \times \Sigma \rightarrow Q$

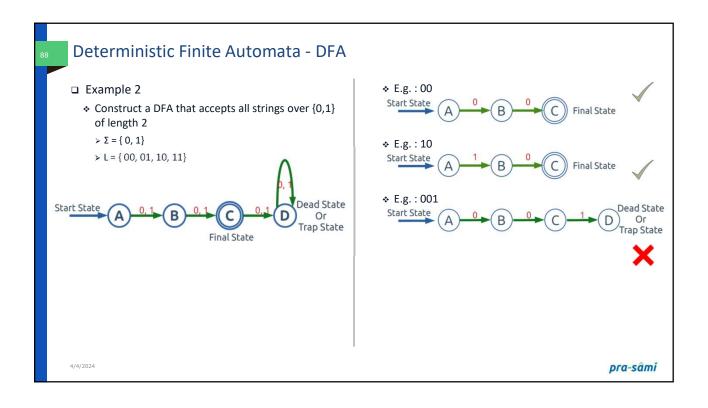


State Transition Diagram



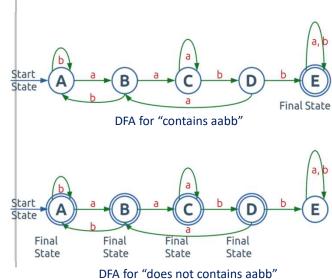
Finite state machine is defined by a tuple  $(Q, \Sigma, q_0, F, \delta)$ 





## Deterministic Finite Automata - DFA

- □ Example 3
  - Construct a DFA that accepts all strings over { a, b } that does not contain 'aabb' in it.
  - It will be simpler to construct a DFA that contains 'aabb'!
    - $> \Sigma = \{ a, b \}$
  - Thereafter, flip the DFA to represent 'Does not contain' condition
  - Final stage becomes non-final and non-final stages become final stage



4/4/2024

# **Regular Languages**

- □ A language is said to be REGULAR LANGUAGE if and only if some Finite State Machine recognizes it
- □ Irregular languages (read set of strings)???
- □ The languages which
  - Are not recognized by FSM
  - Require memory
- ☐ Memory of FSM is very limited
  - It cannot store or count strings
- □ E.g.: ababbababb
- $\Box$  E.g.:  $a^nb^n \rightarrow for n = 3$ , it becomes 'aaabbb' and for n = 5, it is 'aaaaabbbbb'
  - ❖ We need to keep count of how many times 'a' has appeared and compare it with count of 'b'

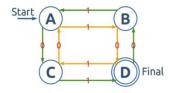
4/4/2024

pra-sâmi

### NFA - Nondeterministic Finite Automata

### **Deterministic Finite Automata**

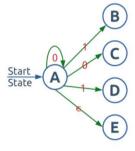
- $\hfill \Box$  Given the current state and input, next state is fixed
- □ It has only one unique next state
- ☐ It has no choices or randomness
- □ Its simplest of all and easy to design



4/4/2024

### Nondeterministic Finite Automata

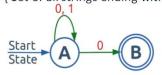
- For given current state and input, there could be multiple next states
- ☐ The next state could be chosen at random
- □ All the next states may be chosen in parallel



pra-sâmi

# NFA - Example

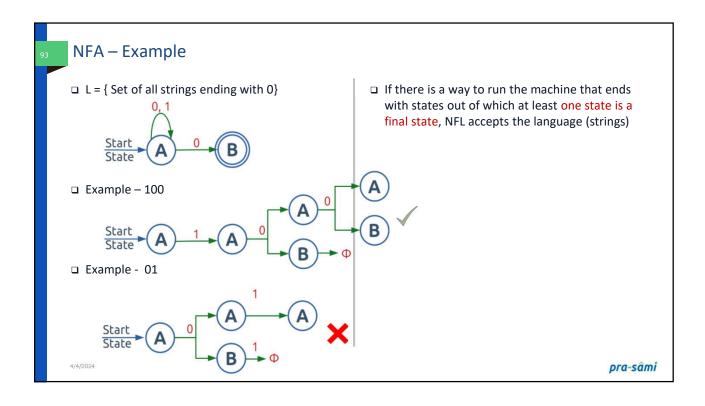
□ L = { Set of all strings ending with 0}



- $\square$  Defined using a tuple of (Q,  $\Sigma$ , q<sub>0</sub>, F,  $\delta$ )
  - ❖ Q : Set of all states = {A, B},
  - **❖** Σ: inputs =  $\{0, 1\}$ ,
  - ❖ q₀: Start State / Initial State= A,
  - ❖ F: Final State(s) = {B},
  - ♦  $\delta$  = transition function from Q x  $\Sigma$   $\rightarrow$  \_\_\_????

- ☐ State A on getting any input where all can it go?
  - ♦ A x 0 → A
  - ♦ A x 0 → B
  - ♦ A x 1 → A
  - ♦ B x 0 → φ
  - ♦ B x 1 → φ
  - A on getting input 0 can go to A as well as B
  - In this case Total possibilities are { A, B, AB, φ} →
     4 Nos.
- □ What happens if there are three states?
  - Total possibilities are {A, B, C, AB, AC, BC. ABC, φ}
     → 8 nos.
- ☐ In general, we can say total possibilities are 20

4/4/2024



# Pushdown Automata

- □ A Pushdown automata is a way to implement a context Free Grammar in a similar way we design Finite Automata for Regular Grammar
  - \* More powerful than FSM
  - ❖ More memory than FSM
  - PDA is FSM plus a Stack ( Arrangement of elements on one on top of another)
    - > Example : pile of books
    - > Push : add on top of the stack
    - > Pop : remove from the top

4/4/2024

# Pushdown Automata

- □ 3 components
  - An input tape
  - Finite control unit
  - Stack of infinite size
- $\square$  Defined by a tuple of (Q,  $\Sigma$ ,  $\Gamma$ ,  $\delta$ ,  $q_0$ ,  $z_0$ , F), where
  - \* Q : A finite set of States
  - \* Σ(sigma) : A finite set of Input Symbols
  - ❖ 「(gamma): A finite Stack Alphabet

  - q<sub>0</sub>: start state,
  - ❖ z₀: The Start Stack Symbol,
  - F: set of Final / Accepting State

4/4/2024

pra-sâmi

### Pushdown Automata

- $\Box$   $\delta$  takes a tuple as argument ( q,  $\alpha$ , X)
  - ❖ q is a State in Q
  - \* α is either an Input Symbol in Σ or ε
  - ${\boldsymbol *} \ \ \, {\boldsymbol X}$  is a Stack Symbol which is part of  $\Gamma$
- $\Box$  The output of  $\delta$  is a tuple (p,  $\gamma$ ) where
  - p is new state
  - $\boldsymbol{\div} \hspace{0.1cm} \gamma$  is a string of stack symbol that replaces X at the top of the stack
  - ♦ If  $\gamma = \epsilon$  → stack is empty
  - ♦ If γ = X → stack is unchanged
  - If γ = YZ → X is replaced by Z and Y is pushed onto the stack

Pushdown Automata

tack

Pushdown Automata

Symbol on top of the Stack This symbol is pushed onto the Stack.

'e' means nothing to pop his popshor top of the Stack.

'e' means nothing to push

4/4/2024

# Example Pushdown Automata □ A PDA that accepts L = { 0^1^n | n ≥ 0 } i.e. L = 000111 → All 0s and 1s need to be together 44/2024

