

⑦ Fractional Knapsack Problem (Solved by Greedy Method)

There are 3 approaches of selecting the items :-

- ① Max. profit approach.
- ② Min. weight approach (to select more items)
- ③ $\left(\frac{\text{Profit}}{\text{Weight}}\right)_{\text{max}}$ approach.

Qm

Objects -	1	2	3	4	5	6	7
Profit (P) -	5	10	15	7	8	9	4
Weight (w) -	1	3	5	4	1	3	2
P/w →	5	3.3	3	1.75	8	3	2

$$\begin{matrix} W=15 \\ \eta=7 \end{matrix}$$

1st approach (Max profit)

Objects	Profit (P)	Weight (w)	Remaining Weight
3	15	5	15 - 5 = 10
2	10	3	10 - 3 = 7
6	9	3	7 - 3 = 4
5	8	1	4 - 1 = 3
4	$7 \times \frac{3}{4}$ $= \frac{21}{4} = 5.25$	3	3 - 3 = 0

$$\boxed{\text{Total P} = 47.25}$$

2nd approach (min weight)

1	5	1	15 - 1 = 14
5	8	1	14 - 1 = 13
7	4	2	13 - 2 = 11
2	10	3	11 - 3 = 8
6	9	3	8 - 3 = 5
4	7	4	5 - 4 = 1
3	$15 \times \frac{1}{5} = 3$	1	1 - 1 = 0

$$\boxed{\text{Total P} = 46}$$

3rd approach (max P/w ratio)

5	8	1	15 - 1 = 14
1	5	1	14 - 1 = 13
2	10	3	13 - 3 = 10
3	15	5	10 - 5 = 5
6	9	3	5 - 3 = 2
7	4	2	2 - 2 = 0

$$\boxed{\text{Total P} = 51}$$