# **Comparing Costs of Classification**

Cost Matrix	PREDICTED CLASS					
ACTUAL CLASS	C(i j)	+	-			
	+	-1	100			
	-	1	0			

Model M <sub>1</sub>	PRED	ICTED (	CLASS	
ACTUAL CLASS		+	-	
	+	150	40	
	-	60	250	

Model M <sub>2</sub>	PREDICTED CLASS						
ACTUAL CLASS		+	-				
	+	250	45				
	-	5	200				

Accuracy = 80% Cost = 3910 Accuracy = 90% Cost = 4255

#### Cost vs Accuracy

Count	PREDICTED CLASS						
		Class=Yes	Class=No				
ACTUAL CLASS	Class=Yes	а	b				
	Class=No	С	d				

Cost	PREDICTED CLASS						
ACTUAL		Class=Yes	Class=No				
	Class=Yes	р	q				
CLASS	Class=No	q	р				

Accuracy is proportional to cost if

- 1. C(Yes|No)=C(No|Yes) = q
- 2. C(Yes|Yes)=C(No|No) = p

$$N = a + b + c + d$$

Accuracy = 
$$(a + d)/N$$

## **Cost-Sensitive Measures**

Precision (p) = 
$$\frac{a}{a+c}$$

Recall (r) = 
$$\frac{a}{a+b}$$

F-measure (F) = 
$$\frac{2rp}{r+p}$$
 =  $\frac{2a}{2a+b+c}$ 

Weighted Accuracy = 
$$\frac{w_1 a + w_4 d}{w_1 a + w_2 b + w_3 c + w_4 d}$$

## **Model Evaluation**

- Metrics for Performance Evaluation
  - How to evaluate the performance of a model?

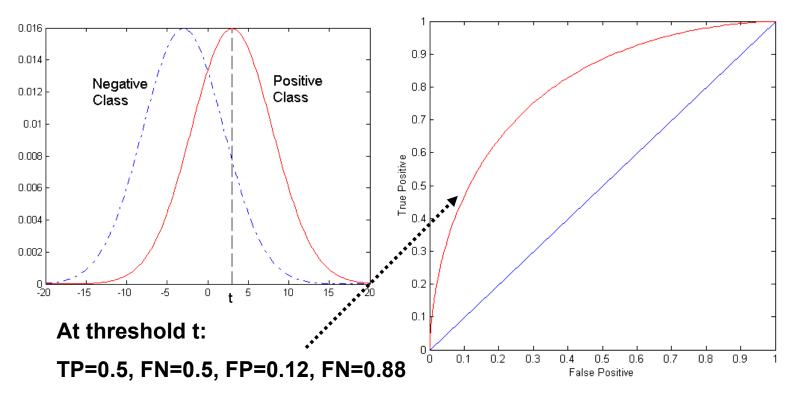
- Methods for Model Comparison
  - How to compare the relative performance among competing models?

#### **ROC** (Receiver Operating Characteristic)

- Developed in 1950s for signal detection theory to analyze noisy signals
  - Characterize the trade-off between positive hits and false alarms
- ROC curve plots TP (on the y-axis) against FP (on the x-axis)
- Performance of each classifier represented as a point on the ROC curve
  - changing the threshold of algorithm, sample distribution or cost matrix changes the location of the point

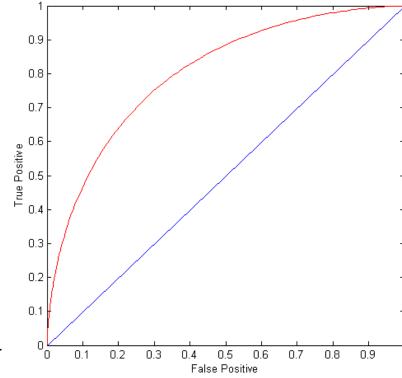
## **ROC Curve**

- 1-dimensional data set containing 2 classes (positive and negative)
- any points located at x > t is classified as positive

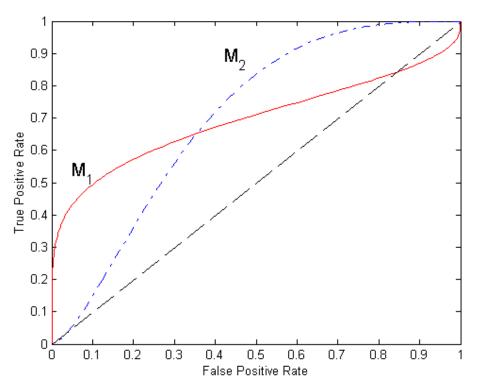


# ROC Curve (TP,FP):

- (0,0): declare everything to be negative class
- (1,1): declare everything to be positive class
- (1,0): ideal
- Diagonal line:
  - Random guessing
  - Below diagonal line:
    - prediction is opposite of the true class



# Using ROC for Model Comparison



- No model consistently outperforms the other
  - ? M<sub>1</sub> is better for small FPR
  - M<sub>2</sub> is better for large FPR
- ? Area Under the ROC curve
  - ! Ideal:
    - Area = 1
  - ? Random guess:
    - Area = 0.5

#### How to Construct an ROC curve

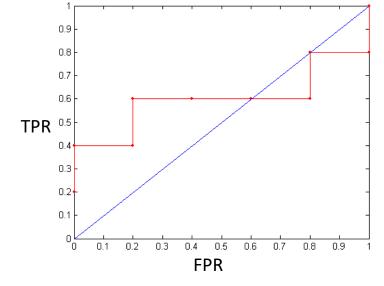
Instance	P(+ A)	True Class
1	0.95	+
2	0.93	+
3	0.87	-
4	0.85	-
5	0.85	-
6	0.85	+
7	0.76	-
8	0.53	+
9	0.43	-
10	0.25	+

- Use classifier that produces posterior probability for each test instance P(+|A)
- Sort the instances according to P(+|A) in decreasing order
- Apply threshold at each unique value of P(+|A)
- Count the number of TP, FP, TN, FN at each threshold
- TP rate, TPR = TP/(TP+FN)
- FP rate, FPR = FP/(FP + TN)

# How to construct an ROC curve

	Class	+	-	+	-	-	-	+	-	+	+	
Threshol	d >=	0.25	0.43	0.53	0.76	0.85	0.85	0.85	0.87	0.93	0.95	1.00
	TP	5	4	4	3	3	3	3	2	2	1	0
	FP	5	5	4	4	3	2	1	1	0	0	0
	TN	0	0	1	1	2	3	4	4	5	5	5
	FN	0	1	1	2	2	2	2	3	3	4	5
<b></b>	TPR	1	0.8	0.8	0.6	0.6	0.6	0.6	0.4	0.4	0.2	0
<b>→</b>	FPR	1	1	0.8	0.8	0.6	0.4	0.2	0.2	0	0	0





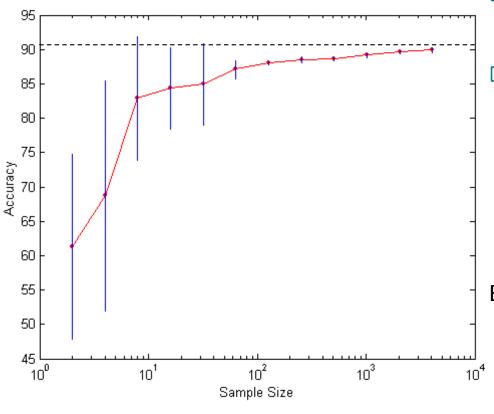
#### Methods for Performance Evaluation

- How to obtain a reliable estimate of performance?
- Performance of a model may depend on other factors besides the learning algorithm:
  - Class distribution
  - Cost of misclassification
  - Size of training and test sets

### Methods of Estimation

- Holdout
  - Reserve 2/3 for training and 1/3 for testing
- Random subsampling
  - Repeated holdout
- Cross validation
- Stratified sampling
  - Keeps relative frequency of different labels intact
- Bootstrap
  - Sampling with replacement

# **Learning Curve**



- Learning curve shows how accuracy changes with varying sample size
- ? Requires a sampling schedule for creating learning curve:
  - Arithmetic sampling (Langley, et al)
  - Geometric sampling (Provost et al)

Effect of small sample size:

- Bias in the estimate
- Variance of estimate