

## Scalability Examples

Wednesday, September 6, 2017 7:49 PM

$$\text{Speed-up: } \frac{T_1}{T_n} \quad 0 \leq S_p \leq \text{Amdahl's Law}$$

$$T_1 = 1 \text{ min} = 60 \text{ sec}$$

$$T_4 = 20 \text{ sec} \quad T_9 = 15 \text{ sec}$$

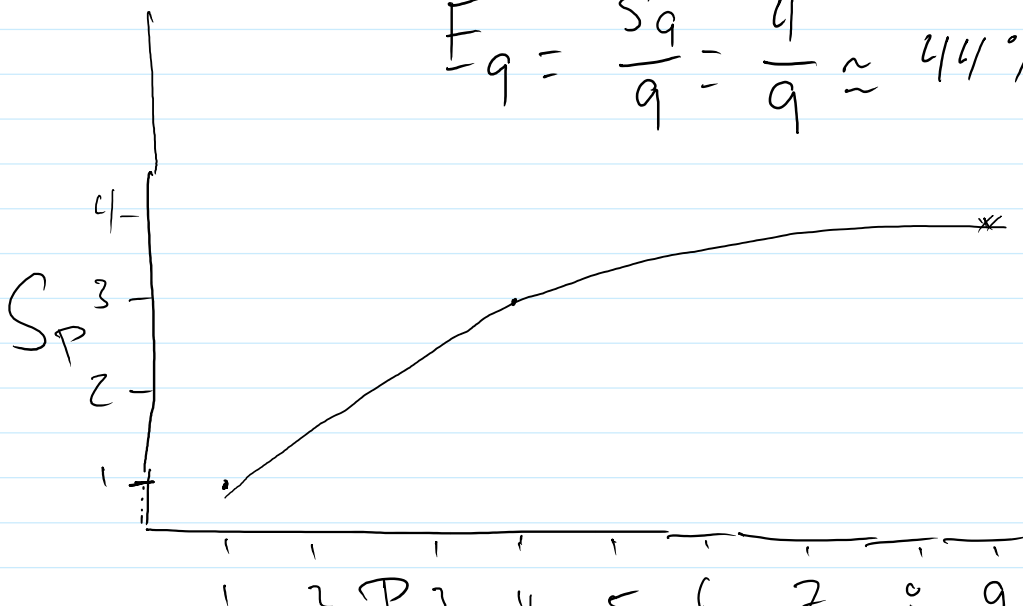
$$S_p = \frac{60 \text{ s}}{20 \text{ s}} = 3 \quad S_9 = \frac{60}{15} = 4 \times$$

$$S_4 = 3$$

$$\text{Efficiency: } E_p = \frac{S_p}{p}$$

$$E_4 = \frac{S_4}{4} = \frac{3}{4} = 75\%$$

$$E_9 = \frac{S_9}{9} = \frac{4}{9} \approx 44\%$$



1 2 P 3 4 5 6 7 8 9

$$S_k = \frac{T_1}{T_k} = \frac{T_s + T_p}{T_s + T_p/k} \left( \frac{T_1}{T_1} \right)$$

$$= \frac{1}{f_s + \frac{(1-f_s)}{k}}$$

$$S_{\infty} \rightarrow \frac{1}{f_s}$$

5% Serial

$$S_{\infty} = \frac{1}{0.05} = 20x$$

## Functional Profile

What percentage of time each function consumes.

5 routines, all taking 20% of run-time.

- for each routine optimized, the best you can do is ~~20%~~ 25% improvement

$$S_p = \frac{T_1}{T_{opt}} = \frac{T_p + T_s}{T_p} = 1 + \frac{T_s}{T_p}$$

$$= \frac{1}{.8} = 1.25 \times$$

$$= \frac{1}{.4} = 2.5 \times$$