



## Searching algo

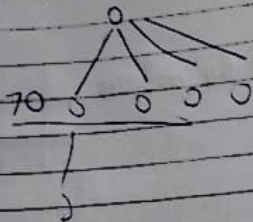
BFS

DFS

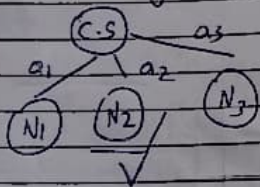
$d=10$

$l=7$

Depth limited search



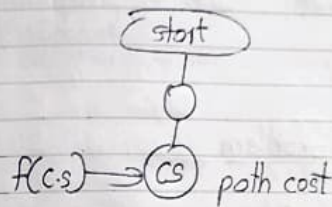
Practical  
⇒ Heuristic Algo



## Best first search

$$A^* \text{ Algo} \Rightarrow f(n) = g(n) + h(n)$$

$\downarrow$  Path cost       $\downarrow$  heuristic



## Simulated Annealing

It takes params:

- ① problem
- ② Schedule

inputs  $r$  is a problem

ooo

- ② Schedule that takes care of mapping

local var current

next - next node

$T \Rightarrow$  controls temp

current ← make\_node (Initial State (problem))

for  $t=1$  to  $\infty$

$T \leftarrow$  Schedule  $[t]$

if  $T=0$  then return current

next ← randomly selected successor of current state



$$\Delta E = \text{value}[\text{next}] - \text{value}[\text{current}]$$

If  $\Delta E$  is greater than 0  
 else  
 current  $\leftarrow$  next with the probability  $\frac{e^{\Delta E/T}}{e^{\Delta E/T} + 1}$

### \* Constraint satisfaction problem

N variables  $N_1, \dots, N_n$   
 $C_1, \dots, C_m$

Soln values to  $N_1, \dots, N_n$

feasible soln



Optimal solution - needs to be feasible & minimize no. of colours

### Cryptarithmic problem

operand A to Z

assign number to letters (0-9)

$$\begin{array}{r} G(1) C_4 \quad 4 \quad G_2 \quad G_1 \\ \quad \quad R \quad 0 \quad 3 \quad 5 \\ \quad \quad R \quad 0 \quad A(6) \quad D(1) \quad S \\ D(3) A(6) \quad N \quad 4 \quad E \quad R \end{array}$$

assumed

$$E = D + S + C_1$$

C5 will be 1. So  $0 = 1$

$$> 9 \quad A = C + R + C_4 (1/0)$$

$A = 0, 2, 3, 4, 5$   
 $(10) (12) (13) (14) (15)$

$$C + R + C_4 (0)$$

$$N < 9$$

or

$$C + R + C_4 (1)$$

$$n > 10$$

$C_5(1)$	$C_4(0)$	$C_3(6)$	$C_2(0)$	$C_1(0)$	
	$C(0)$	$R(6)$	$O(2)$	$S(3)$	$S(3)$
	$R(6)$	$O(2)$	$A(5)$	$D(1)$	$S(3)$
$D(1)$	$A(5)$	$N(8)$	$4(7)$	$E(4)$	$R(6)$

$A(5) \quad C(8) \quad D(1) \quad E(4) \quad 4(9) \quad R(6) \quad S(3)$   
 $N(0)$

2 G(1) G(1) G(1) C(1)  
 N(1) N(1) D(1)  
 M(1) R(1) E(1)  
 M(1) O(1) F(1) Y(1)

2 DONALD  
 6 FERALD

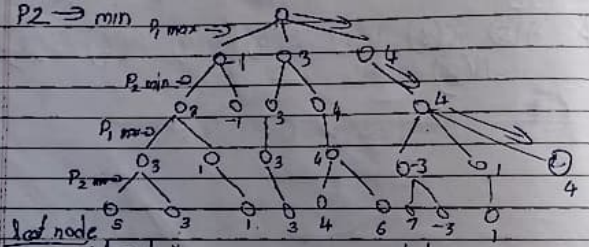
9 > 0  
 (S(1) G(1) G(1) G(1) G(1)  
 S(1) E(1) N(1) D(1)  
 M(1) O(1) R(1) F(1)  
 M(1) O(1) 4 E(1) Y(1)

D(1) O(1) N(1) A(1) L(1) D(1)  
 G(1) E(1) R(1) A(1) L(1) D(1)  
 R(1) O(1) F(1) E(1) R(1) T(1)

Games max-min

2 players  $\rightarrow$  objective function

P1  $\rightarrow$  max  
 P2  $\rightarrow$  min



leaf node

X	0	X
X	X	0
0	X	0

level 1

X	0	0
X	X	0
0	X	0

level - 5

utility function (n)  
 low

utility function (n)  
 higher on one side & lower

Alpha-beta pruning

Prune a part of tree which gives better result

$-\infty \rightarrow \alpha \rightarrow$  max player (better for max player)  
 $+\infty \rightarrow \beta \rightarrow$  min (lower better for min player)

$\alpha \geq \beta \rightarrow$  prune the tree

Algorithm

AlphaBetaSearch(state)  $\rightarrow$  returns action

$\{$   $v \leftarrow \text{max\_value}(\text{state}, -\infty, +\infty)$   
 this returns the action in  $\beta$  successor of the state with value  $v$   
 Successor(state)  
 $\}$

function max\_value(state,  $\alpha$ ,  $\beta$ )  $\rightarrow$  return utility value

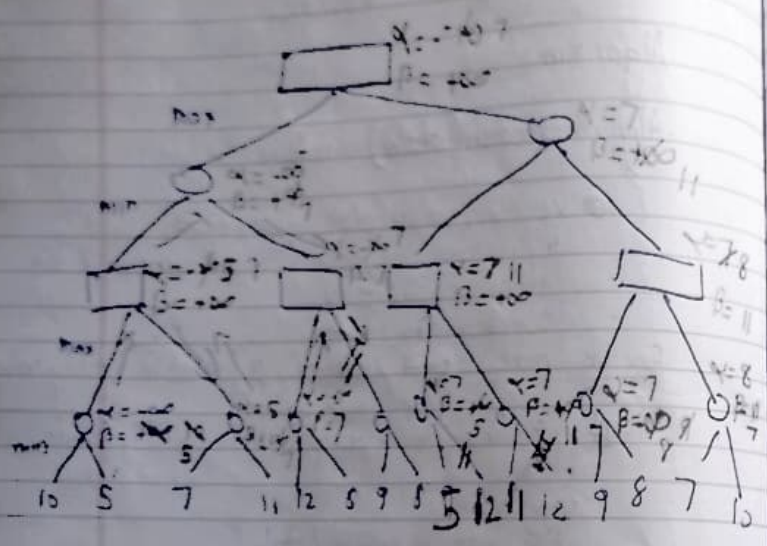
$\{$  If terminal, test(state) return utility(state)  
 else  
 $v \leftarrow -\infty$   
 for a, s successor(state)  
 $v \leftarrow \text{max}(v, \text{min\_value}(s, \alpha, \beta))$   
 if  $v \geq \beta$  return  $v$   
 $\alpha \leftarrow \text{max}(\alpha, v)$   
 return  $v$   
 $\}$

function min\_value(state,  $\alpha$ ,  $\beta$ )  $\rightarrow$  return utility value

$\{$  If terminal, test(state) return utility(state)  
 else



$\forall x \in S$  success (state)  
 $\forall x \in S$  state (S, V, B)  
 $\forall x \in S$  state V  
 $\forall x \in S$  state V  
 $\forall x \in S$  state V



# Knowledge Representations

First order logic  
 Predicate calculus  
 Quantifiers  
 variables  
 relations

$\forall x$   
 $\exists y$

like (John, apple)  
 like (John, papaya)  
 like (Joe, Mango) } facts

$like(x, y)$   
 John —  
 —

Joe mango

All kings like crown  
 $\forall x \forall y$  King(x)  $\wedge$  crown(y)  $\wedge$  wears (x, y)

$wear(\forall x, y)$   
 crown

$stud(x)$  University(y)  $\Rightarrow$  implication

all stud at gcc are affiliated to gcc, all gcc entity not affiliated to gcc  
 $\forall x, y \exists z$  student(x)  $\wedge$  college(y)  $\wedge$  university(z)  $\wedge$  affiliated(y, z)  $\wedge$  study(x, y)  $\Rightarrow$  associated(x, z)

Premise  $\Rightarrow$  conclusion

Implication

$$A \Rightarrow B = \neg A \vee B$$

$$A \Leftrightarrow B = (A \Rightarrow B) \wedge (B \Rightarrow A)$$

$$= (\neg A \vee B) \wedge (\neg B \vee A)$$

$$\neg(A \vee B) = \neg A \wedge \neg B$$

facts  
rules  
connectives

$\neg \vee \neg$  facts { student(ravi, gec)  
college(gec)  
attila(gec, gu)

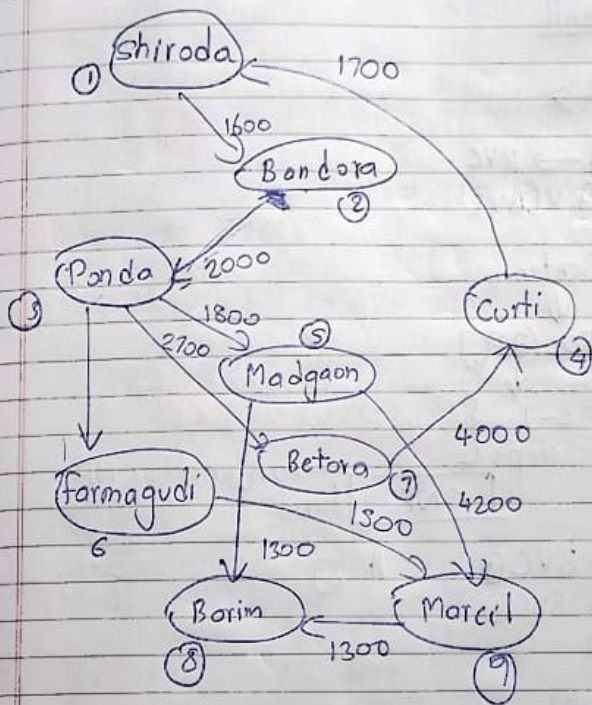
Unification  
Resolution

student(x, y)  
{x/ravi, y/gec}  
fact student(ravi, gec)

$$s(x, y) \wedge c(y) \wedge a(y, z) \Rightarrow \text{associated}(x, z)$$

s(ravi, gec)	x/ravi
c(gec)	y/gec
a(gec, gu)	z/gu

Exp 1  
AIM - To implement BFS · DFS  
Depth limited search.





$x = 100$

Resolution



$A \rightarrow BVC$   
 $\neg A \vee (BVC)$

eg sentence

↓  
 FOL (BPL)

↓  
 6-7 steps

CNF form conjunctive NF

$A \rightarrow BVC$  ①      $A$  ②  
 $\neg A \vee BVC$  ①  
 $\neg C$  ③

Pure B?

Assumption:  $\neg B \rightarrow$  wrong  $\therefore B$  true

$\neg B$       $\neg A \vee BVC$

$\neg A \vee C$       $A$

$\neg C$  ③

$\neg C$  assumption is wrong

steps

① Eliminate implication

$A \rightarrow B$   
 $\neg A \vee B$

$A \leftrightarrow B$       $(A \rightarrow B) \wedge (B \rightarrow A)$   
 $(\neg A \vee B) \wedge (\neg B \vee A)$

step 2

Reduce the scope of

$\neg$  to single term

$\neg(a \vee b) = \neg a \wedge \neg b$

$\neg(a \wedge b) = \neg a \vee \neg b$

$\neg \forall x : P(x) = \exists x : \neg P(x)$

$\neg \exists x : P(x) = \forall x : \neg P(x)$

step 3

standardize the variable such that each quantifier binds to a unique variable

$\forall x : P(x)$

$\forall x : Q(x)$

$\forall x$  father (x, x)

"

$\forall y : Q(y)$

Step 4

Move all the quantifiers to the left of the formula without changing the relative orders

$\forall x \forall y : P(x) \wedge Q(y)$

$\forall x : P(x) \wedge \forall y : Q(y)$

$\forall x \forall y : P(x) \wedge Q(y)$

5 eliminate existential quantifier  
 Skolemisation  $\rightarrow$  Skolem value  
 $\rightarrow$  " function

$\forall x \exists y \text{ President}(s, x)$

$\forall x \exists y \text{ father}(y, x)$

$\forall x \exists y \text{ father}(g(x), x)$

Step 6:

Eliminate universal quantifier  
 no extra rule as such

Step 7:

Convert the matrix to an conjunction of  
 disjoints

$(a \vee b) \wedge (c \vee d)$

Step 8:

create a separate clause corresponding  
 to each conjunct

$(a \vee c) \wedge (b \vee d)$

① Anyone passing a toe exam and winning a  
 lottery is happy

② Anyone who studies or is lucky can pass  
 the exam

③ John did not study but he was lucky

④ Anyone who is lucky wins a lot lottery

$\rightarrow$  by using resolution prove whether john  
 is happy

student(x)  $\rightarrow$  exam(y)  $\rightarrow$  passing(z)

①  $\forall x \text{ pass}(x, \text{toe}) \wedge \text{win}(x, \text{lottery}) \Rightarrow \text{happy}(x)$

$\neg (\text{pass}(x, \text{toe}) \wedge \text{win}(x, \text{lottery})) \vee \text{happy}(x)$

$\vee \neg (\text{pass}(x, \text{toe}) \vee \neg (\text{win}(x, \text{lottery}))) \vee \text{happy}(x)$   
 $\rightarrow$  ① . i

②  $\forall y \exists z \text{ studies}(y) \vee \text{lucky}(y) \rightarrow \text{pass}(y, z)$

$\neg (\text{study}(y) \vee \text{lucky}(y)) \vee \text{pass}(y, z)$

$(\neg (\text{study}(y)) \wedge \neg (\text{lucky}(y))) \vee \text{pass}(y, z)$

$(\neg (\text{study}(y)) \wedge \neg (\text{lucky}(y))) \vee \text{pass}(y, s_1)$

$\neg \text{study}(y) \vee \text{pass}(y, s_1) - 2i) \neg \text{lucky}(y) \vee \text{pass}(y, s_1) - 2i)$



③  $\exists x \text{ study}(x, \text{John})$  3i)  
 $\exists x \text{ lucky}(x, \text{John})$  3ii)

$\forall v \text{ lucky}(v) \Rightarrow \text{win}(v, \text{lottery})$   
 $\neg \text{lucky}(v) \vee \text{win}(v, \text{lottery}) = 4$

$\neg \text{happy}(\text{John})$  ①  
 $\neg \exists x / \text{John}$

$\neg (\text{pass}(\text{John}, \text{loc})) \vee \neg \text{win}(\text{John}, \text{lottery})$

$\neg \text{study}(\text{John}) \vee \neg \text{win}(\text{John}, \text{lottery})$   
 $\text{fact}$

$\neg \text{win}(\text{John}, \text{lottery})$   
 $\vee \text{John}$

$\neg \text{lucky}(\text{John})$  3ii)  
 $\text{nil}$

John was happy

1) All people who are not poor and are smart are happy

2) Those people who read books are intelligent

3) John reads the book and is wealthy

4) Happy people have a good life

By resolution prove if anyone be found with a good life

1)  $\neg \exists x \neg \text{poor}(x) \wedge \text{smart}(x) \Rightarrow \text{happy}(x)$

2)  $\neg \exists x (\neg \text{poor}(x) \wedge \text{smart}(x) \wedge \neg \text{happy}(x))$   
 $\text{poor}(x) \vee \neg \text{smart}(x) \vee \text{happy}(x)$

2)  $\forall y \text{ read}(y, \text{books}) \Rightarrow \text{intelligent}(y)$   
 $\neg \text{read}(y, \text{books}) \vee \text{intelligent}(y)$

$\neg (\text{good life}(v))$  ④

$\neg \text{happy}(v)$  ①

$\text{poor}(v) \vee \neg \text{smart}(v)$  ②

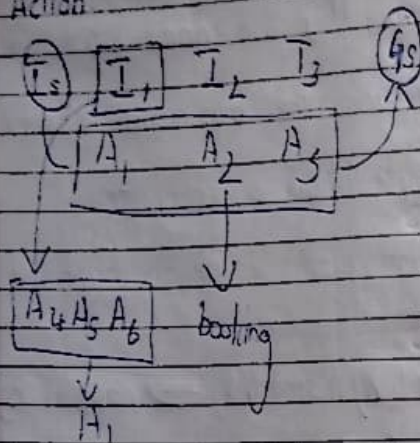
$\text{poor}(v) \vee \neg \text{read}(v, \text{books})$  3i)  
 $\text{poor}(\text{John}) \vee \neg \text{read}(\text{John}, \text{books})$

## Planning

→ sequence of action to achieve sequence of tasks

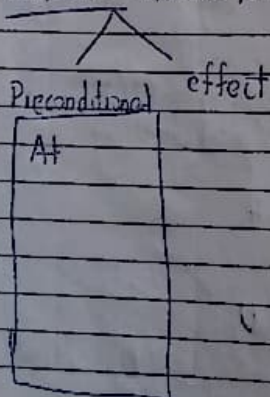
PODL

Action:

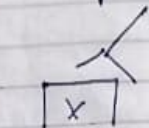


should be reusable

action: generic form

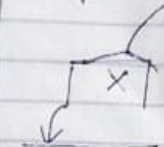


Action for  
① Pickup (X)



PC  
OT(X)  
Armempty()  
At(X)  
clear(X)  
effect  
OT(X)  
Armempty()  
holding(X)

robotic line  
putdown(X)



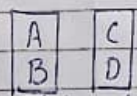
PC  
Table empty()  
holding(X)  
effect  
holding(X)  
armempty(X)  
OT(X)

stack(y) unstack(X,Y)



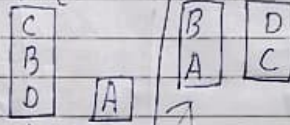
PC  
stack(X,Y)  
holding(X)  
clear(Y)  
effects  
holding(X)  
armempty()  
on(X,Y)  
unstack(X,Y)  
PC  
armempty()  
on(X,Y)  
clear(X)

Initial



OT(B), OT(D)  
on(A,B), on(C,D)  
clear(A), clear(C)

Goal



on(B,A)  
on(D,C)

Goal stack  
Armempty()

planning problem

unstack(A,B)  
unstack(A,B), putdown(A)  
pickup(B), stack(B,A)  
unstack(C,D), putdown(C)  
pickup(D), stack(D,C)

Armempty()

on(A,B)  
clear(A)  
unstack(A,B)  
on(B,A)  
on(D,C)



holding(A)
putdown(A)
on(A,A)
on(D,C)

clear(A)	armempty()
holding(A)	on(A,B)
stack(A,B)	clear(B)
on(A,B)	unstack(A,B)
on(B,C)	<del>on(B,C)</del> on(B,C)

	off(B)
	armempty()
holding(A)	clear(B)
putdown(A)	pickup(B)
on(B,C)	on(B,C)

holding(A)
clear(B)
stack(B,C)
on(B,C)

P
Q
R

S
---

on(P,Q)  
 on(Q,R)  
 OT(S)  
 OT(R)  
 C(P)  
 C(S)  
 armempty()  
 unstack(P,Q)  
 putdown(P)  
~~steps~~ unstack(Q,R)  
 putdown(Q)  
 X/pickup(R)  
 stack(R,S)

R
S
P
Q

on(P,Q)  
 on(Q,P)  
 on(R,S)  
 OT(Q)  
 C(R)  
 pickup(P)  
 stack(P,Q)  
 pickup(S)  
 stack(S,P)  
 pickup(R)  
 stack(R,S)

holding(P)
putdown(P)
AR
on(Q,R)
C(Q)
unstack(Q,P)

→

holding(A)
putdown(A)
off(Q)
on(P,S)
on(S,P)
<del>on(P,Q)</del>

OT(S)  
 on(R,S)  
 on(S,P)  
 on(P,Q)

armempty()
pickup(R)
on(R,S)
on(Q,P)
on(P,Q)

stack(P,Q)
on(R,S)
on(S,P)
on(P,Q)

$OT(P)$ <del>Attempt!</del> <del>clear(P)</del> <del>Pickup(P)</del> $on(P,Q)$ $on(S,P)$ $on(R,S)$	$holding(P)$ <del>clear(P)</del> $stack(P,Q)$ $on(P,Q)$ $on(S,P)$ $on(R,S)$	$OT(S)$ <del>Attempt!</del> $clear(S)$ $Pickup(S)$ $on(S,P)$ $on(R,S)$
--	--	---

$holding(S)$ <del>clear(P)</del> $stack(S,Q)$ $on(S,P)$ $on(R,S)$	<del><math>OT(P)</math></del> <del>Attempt!</del> $clear(R)$ $Pickup(R)$ <del><math>on(R,S)</math></del> $on(R,S)$	$holding(R)$ <del>clear(S)</del> <del><math>on(S,P)</math></del> $on(R,S)$
---	---	---

Q

P
Q
R
S

S
R
Q
P

$OT(S)$   
 $on(R,S)$   
 $on(Q,R)$   
 $on(P,Q)$   
~~Attempt!~~

$OT(P)$   
 $on(Q,P)$   
 $on(Q,R)$   
 $on(R,S)$

Forward &  
backward search

fact  $\rightarrow$  goal  
 fact  $\rightarrow$  goal

$run(x) \Rightarrow sweat(x)$   
 $run(John)$        $sweat(John)$

planning problem

cargo

$C_1$

$C_2$

Airport  
 $A_1$

$A_2$

goal

$A_1 \rightarrow C_2$
$A_2 \rightarrow C_1$

Action  $\begin{cases} pre \\ effect \end{cases}$



Pre:  $\frac{\text{load}(C, P)}{\text{cargo}(C) \wedge \text{plane}(P) \wedge \text{At}(P, A) \wedge \text{Airport}(A)}$

effect:  $\text{In}(C, P) \wedge \neg \text{At}(C, A)$

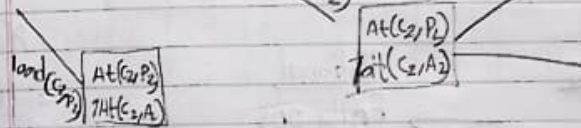
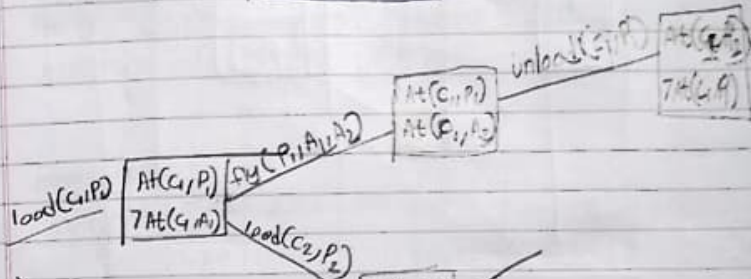
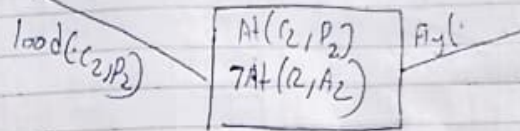
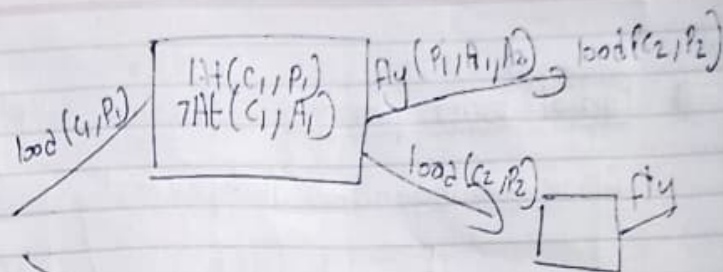
Pre:  $\frac{\text{Unload}(C, P)}{\text{cargo}(C) \wedge \text{plane}(P) \wedge \text{In}(C, P) \wedge \text{At}(P, A) \wedge \text{Airport}(A)}$

effect:  $\neg \text{In}(C, P) \wedge \text{At}(C, A)$

Pre:  $\frac{\text{Fly}(P, S, D)}{\text{plane}(P) \wedge \text{airport}(S) \wedge \text{airport}(D) \wedge \text{In}(C, P) \wedge \text{Cargo}(C)}$

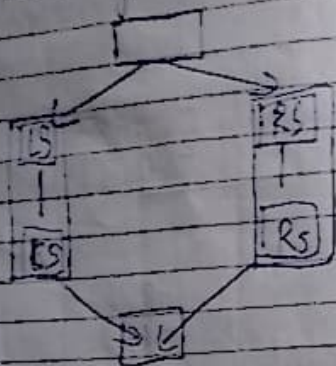
effect:  $\neg \text{At}(P, S) \wedge \text{At}(P, D)$

Initial  
 $C(C_1)$   
 $C(C_2)$   
 $A(A_1)$   
 $A(A_2)$   
 $\text{At}(C_1, A_1)$   
 $\text{At}(C_2, A_2)$   
 $\text{At}(P_1, A_1)$   
 $\text{At}(P_2, A_2)$



## \* Partial order planning

Goals → subgoals → Independently



Agent

Environment

Rational

Fully obs

Partly

→ likelihood

Probability

$$P(a/b) = \frac{P(b/a)}{P(b)}$$

P(T)	7P

## Partial order planning

$$P(a/b) = \frac{P(a \cap b)}{P(b)}$$

In a scenario two things can occur  
cavity of gum problem

cavity	TA		TTA		
	gum	7gum	gum	7gum	
cavity	0.108	0.012	0.072	0.008	0.2
7 cavity	0.016	0.064	0.164	0.576	0.2
					0.200

$$P(T/E) = \frac{P(T \cap E)}{P(E)} = \frac{0.120}{0.2} = 0.6$$

$$P(T/C, Y)$$

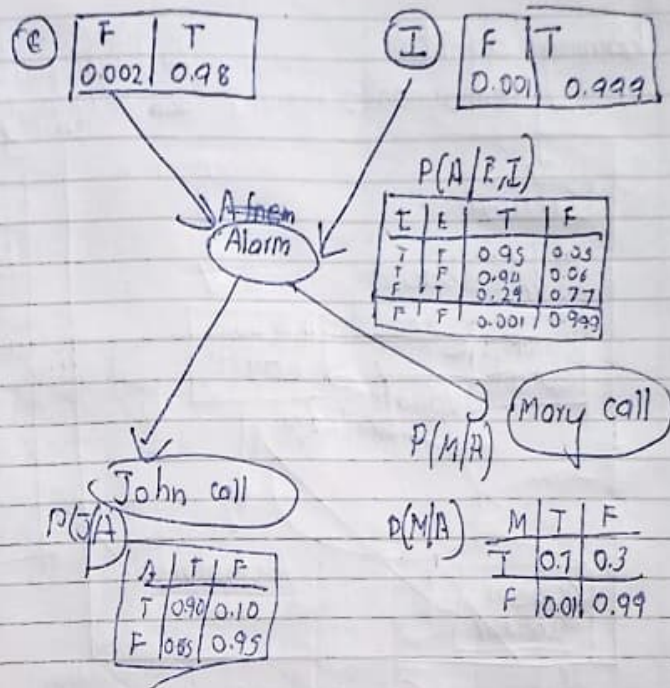
$$P(C/T) = \frac{P(C \cap T)}{P(T)} = \frac{P(Y/X)P(X)}{P(Y)}$$

$$= \frac{P(T/C)P(C)}{P(T)} = \frac{0.6 \times 0.2}{0.2} = 0.6$$



Use of  
Consider an event of ringing of alarm  
because of an earthquake or because  
of an intrusion & in response either  
John calls or Mary calls

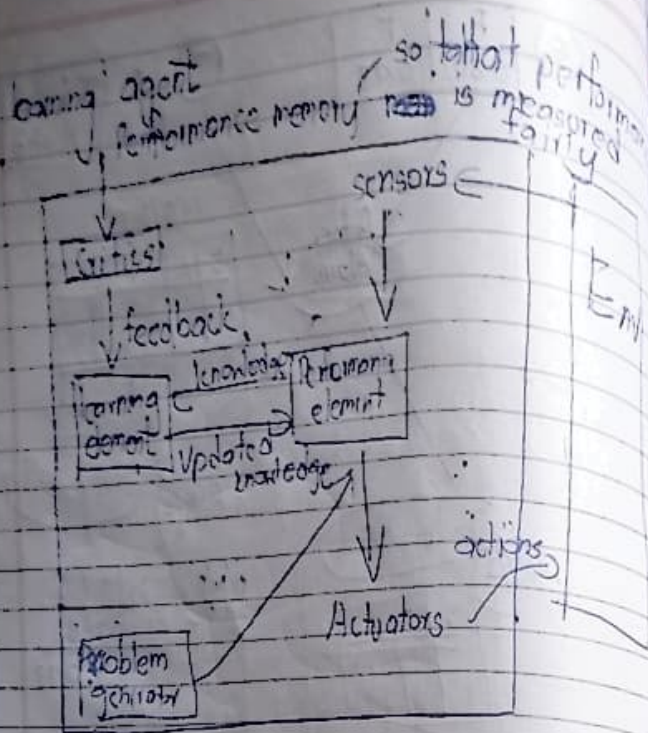
	John		Mary	
	Intiv	Intrusion	Intiv	Intrusion
E				
$\neg E$				



Learning  
Updating KB

New  
modifying  
deleting

- 1) observation
- 2) practise  $\rightarrow$  Rule learning
- 3) Experiments
- 4) Implementation



P
Q
R
S

unstack(P,Q)  
putdown(P)

S
R
Q
P

OT(S) clear(P)  
on(R,S)  
on(Q,R)  
on(P,Q)  
Aempty()

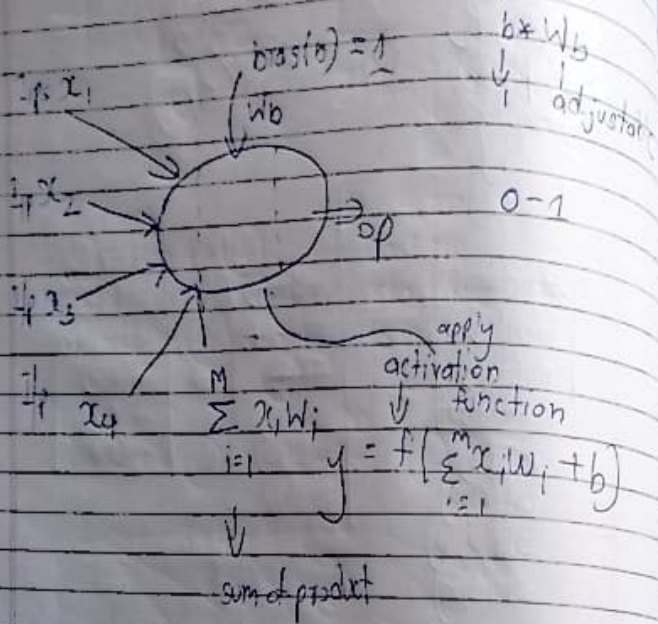
OT(P)  
on(Q,P)  
on(Q,R)  
on(R,S)

①  
Aempty()  
clear(P)  
on(P,Q)  
unstack(P,Q) →  
OT(P)  
on(Q,P)  
on(R,Q)  
on(S,R)

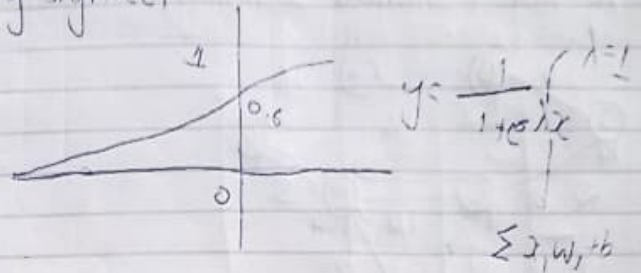
holding(P)  
putdown(P)  
OT(P) →  
on(Q,R)  
on(R,S)  
on(S,R)

Aempty()  
clear(Q)  
on(S,R)  
unstack(Q,R)  
on(Q,R)  
on(R,Q)  
on(S,R)



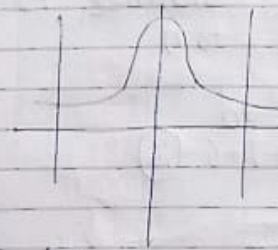


log sigmoid



tan sigmoid

Radial Basis func



n/w

step

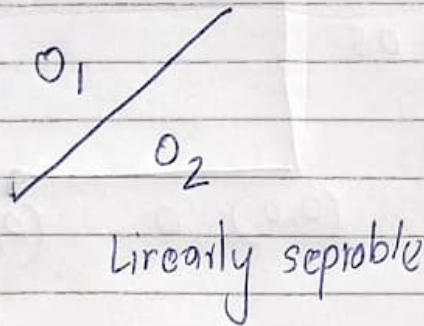
1
0

bipolar

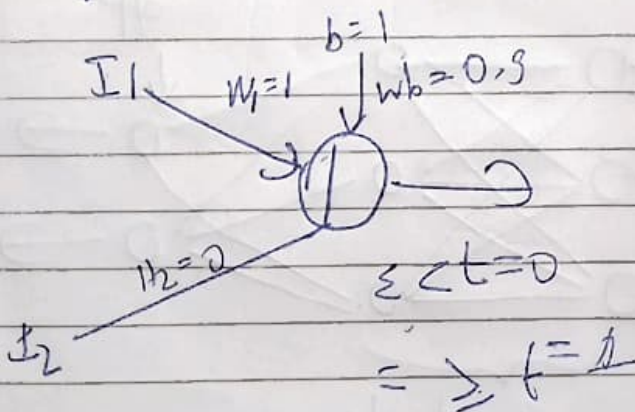
1
0
-1

# Neural Network

learn



OR		d/p	o/p
$I_1$	$I_2$		
0	0	0	0
0	1	1	0
1	0	1	0
1	1	1	1





XOR is not linearly separable

