Here are **30 one-line problem statements** categorized by **Advanced Dynamic Programming** techniques:

ℰ Divide & Conquer DP

- 1. Minimize cost to partition an array into k segments with defined cost per segment.
- 2. Given n matrices, find the minimum multiplication cost using optimal order (Matrix Chain Multiplication).
- 3. Find optimal binary search tree construction with minimal expected search cost.
- 4. Partition a sequence into k parts minimizing sum of costs of each part.
- 5. Segment n elements such that total penalty from segment transitions is minimized.

V DP with Bitmasks

- 6. Count the number of ways to assign n jobs to n workers with constraints.
- 7. Find minimum cost to visit all cities exactly once (Traveling Salesman Problem).
- 8. Compute number of Hamiltonian paths in a directed graph.
- 9. Maximize the score of selecting a subset of items with non-overlapping properties.
- 10. Count the number of valid ways to tile an n x m grid using dominos.

Tree DP (including rerooting)

- 11. For each node in a tree, compute the sum of distances to all other nodes.
- 12. Find size of largest independent set in a tree.
- 13. Count number of subtrees with even number of nodes.
- 14. Compute max path sum (diameter) for a tree.
- 15. Reroot tree at every node and calculate answer for each new root (e.g., sum of distances).

♥ Slope Trick (Convex DP Optimization)

- 16. Minimize cost of aligning n positions with minimum movement cost.
- 17. Dynamic programming with dp[i] = min(dp[j] + cost(j, i)) where cost is convex.
- 18. Optimal checkpoint placement on a line to minimize total deviation from k centers.
- 19. Scheduling jobs to minimize weighted tardiness penalty (Convex cost).
- 20. Place facilities on a line with penalty increasing quadratically from optimal location.

W Knuth Optimization

- 21. Optimal matrix parenthesization with cost function satisfying quadrangle inequality.
- 22. Partition a string into palindromic substrings with minimum cuts.
- 23. Merge stones with minimal total cost when merging only k at a time.
- 24. Minimize total cost to concatenate n strings where merging cost is proportional to length.
- 25. Find minimal edit cost when operations follow associative/triangle inequality rules.

Monotonic Queue Optimization

- 26. Maximize score by jumping k steps forward at each move with cost per jump.
- 27. Find minimum cost to paint fence sections with restrictions on adjacent colors.
- 28. Largest sum of subarray with at most k elements using sliding window DP.
- 29. Maximize profit from stock trading with cooldown using windowed profit tracking.
- 30. Minimize cost of climbing stairs with jump limits using deque-based DP.

Let me know if you want full problems with constraints, explanations, or code.

You said:

. Advanced Graph Algorithms • Strongly Connected Components (Kosaraju/Tarjan) • Biconnected Components • 2-SAT Problem • Bridges and Articulation Points • Minimum Cost Flow • Flow with Lower Bounds • Maximum Matching in Bipartite Graph (Kuhn's, Hopcroft-Karp) • Min-Cost Max Flow

ChatGPT said:

Here are **30 one-line problem statements** categorized by **Advanced Graph Algorithms** topics:

♥ Strongly Connected Components (Kosaraju / Tarjan)

- 1. Find the number of strongly connected components in a directed graph.
- 2. Identify which nodes belong to the same SCC in a graph.
- 3. Shrink a graph to its component DAG using SCC decomposition.
- 4. Find the minimal number of edges to add to make a directed graph strongly connected.
- 5. Determine if each node in a graph can reach every other node (strong connectivity check).

Solution Biconnected Components

- 6. Find all biconnected components in an undirected graph.
- 7. Count the number of articulation points in a graph.
- 8. Identify critical edges whose removal increases number of connected components.
- 9. Check if a graph is biconnected (no articulation point).
- 10. List all edge-biconnected components of a graph.

⊘ 2-SAT Problem

- 11. Check if a set of 2-variable boolean constraints can be satisfied.
- 12. Find one satisfying assignment for a given 2-SAT formula.
- 13. Minimize number of true variables satisfying all 2-variable clauses.
- 14. Check satisfiability of constraints like "if A is true, then B must be false".
- 15. Determine feasibility of scheduling two types of events with exclusive overlaps.

V Bridges and Articulation Points

- 16. Find all bridge edges in an undirected graph.
- 17. Count number of connected components formed after removing one articulation point.
- 18. Identify articulation points in a graph that disconnect it on removal.
- 19. List bridge edges whose removal increases number of connected components.
- 20. Build a bridge tree from a given undirected graph.

Minimum Cost Flow

- 21. Given supply and demand at nodes, compute minimum cost to send all required flow.
- 22. Transport goods across a weighted network minimizing shipping cost.
- 23. Compute cost of fulfilling all orders in a supply chain with capacity and price constraints.
- 24. Route data packets from sources to sinks minimizing total transmission cost.
- 25. Solve project task dependencies with resource flow minimizing total cost.

Flow with Lower Bounds

- 26. Given a network with lower and upper bounds on flow, check if feasible flow exists.
- 27. Find feasible flow in a network respecting both lower and upper capacity bounds.
- 28. Route flow through a network where each edge has a minimum flow requirement.
- 29. Model flow constraints with mandatory delivery quotas per edge.
- 30. Balance a supply chain network where each route must carry at least a baseline flow.

⊘ Maximum Matching in Bipartite Graph (Kuhn's / Hopcroft-Karp)

- 31. Find maximum number of job assignments for workers and jobs.
- 32. Match students to projects such that no two students share the same project.
- 33. Determine if a perfect matching exists in a bipartite graph.
- 34. Calculate maximum matching between doctors and patients based on availability.
- 35. Maximize number of pairings between applicants and apartments with preferences.

Min-Cost Max Flow

- 36. Assign workers to tasks minimizing total cost while maximizing number of assignments.
- 37. Match buyers to sellers maximizing trades and minimizing cost of transactions.
- 38. Optimize resource allocation with both quantity and cost constraints.
- 39. Schedule k projects with minimum cost and maximum profit flow.
- 40. Find max flow of goods through a network with the least total delivery cost.

Let me know if you want code, explanations, or visualizations for any of these.

You said:

Data Structures • Mergeable Heaps (e.g., Leftist Tree, Skew Heap) • Persistent Segment Trees • Treap / Splay Tree (Implicit Treap for sequence manipulation) • Heavy-Light Decomposition (HLD) • Mo's Algorithm (with updates) • Segment Tree Beats

ChatGPT said:

Here are **30 one-line problem statements** categorized by advanced **Data Structures** topics:

⊘ Mergeable Heaps (Leftist Tree, Skew Heap)

- 1. Perform a sequence of merge and extract-min operations on disjoint heaps efficiently.
- 2. Merge two priority queues in logarithmic time and extract the minimum.
- 3. Maintain a set of disjoint heaps and support deletion of any element.
- 4. Simulate a multiway tournament with players stored in mergeable heaps.
- 5. Support insertion and deletion from multiple heaps with quick merges.

Persistent Segment Trees

- 6. Support range sum queries on historical versions of an array.
- 7. Rollback or jump to any previous version of the array and perform queries.
- 8. Count how many numbers $\leq x$ in a subarray [1, r] using persistence.
- 9. Find the k-th smallest number in a range [1, r] over multiple versions.
- 10. Track versioned data structure for undo/redo operations and interval queries.

♥ Treap / Splay Tree (Implicit Treap for sequence manipulation)

- 11. Perform insert, erase, split, merge on an array-like sequence in logarithmic time.
- 12. Reverse a subarray in a dynamic array using implicit treap.
- 13. Move a subsegment [1, r] to front/middle/end using sequence manipulation.
- 14. Maintain a dynamic string with cut-paste-reverse operations.
- 15. Find and delete the k-th element in a mutable sequence.

Heavy-Light Decomposition (HLD)

- 16. Answer path queries (e.g., sum/max) between any two nodes in a tree efficiently.
- 17. Update values on paths or subtrees in a tree with logarithmic complexity.
- 18. Find lowest common ancestor (LCA) of any two nodes using HLD.
- 19. Process a tree where you need to handle queries like "maximum value on a path".
- 20. Support range updates and queries on rooted tree paths.

⊘ Mo's Algorithm (with updates)

- 21. Count the number of distinct elements in range [1, r] for multiple queries.
- 22. Answer frequency of most occurring element in a range [1, r].
- 23. Support adding/removing updates and range queries with offline processing.
- 24. Answer queries like "how many values appear at least k times in range [1, r]?"
- 25. Process queries with range add and range count using Mo's with updates.

Segment Tree Beats

- 26. Support range minimum/maximum updates and queries where lazy propagation fails.
- 27. On a range, apply "set all values $\leq x$ to x" efficiently.
- 28. Support "minimize" or "maximize" a range with conditional updates.
- 29. Find the sum, min, and count of min in a range with conditional modifications.
- 30. Solve range-chmin, range-chmax, and range-add with complex segment logic.

Let me know if you'd like to expand any of these into full problems or want implementations.

You said:

Matrix Exponentiation (for Linear Recurrences) • Fast Walsh–Hadamard Transform (FWHT)

• Fast Fourier Transform (FFT) • Number Theoretic Transform (NTT) • Diophantine Equations • Gaussian Elimination (Modulo and Floating Point) • Combinatorics with Generating Functions • Mobius Inversion • Burnside's Lemma and Polya Enumeration

ChatGPT said:

Here are **30 one-line problem statements** categorized under advanced **Math & Algebraic Techniques** in competitive programming:

✓ Matrix Exponentiation (for Linear Recurrences)

- 1. Find the N-th Fibonacci number modulo 1e9+7.
- 2. Compute N-th term of a linear recurrence with given initial terms and coefficients.
- 3. Count number of ways to tile a 2×N board using dominoes and trominoes.
- 4. Calculate population growth in N years modeled by a linear recurrence.
- 5. Simulate linear recurrence for stocks/investments for very large N.

♥ Fast Walsh–Hadamard Transform (FWHT)

- 6. Compute XOR convolution of two binary arrays efficiently.
- 7. Count number of subsets whose XOR is less than a given value.
- 8. Solve subset convolution problems where operation is XOR instead of sum.
- 9. Perform subset convolution in exponential time with bitmask-based transforms.
- 10. Count the number of ways to select disjoint sets with a specific XOR value.

∜ Fast Fourier Transform (FFT)

- 11. Multiply two large polynomials or integers efficiently.
- 12. Find the number of pairs of elements from two arrays that sum up to a given value.
- 13. Count number of subarrays with a fixed sum using convolution.
- 14. Perform pattern matching using polynomial multiplication.
- 15. Multiply two numbers each with up to 1e6 digits using FFT.

♥ Number Theoretic Transform (NTT)

16. Multiply large polynomials under a modulo (like 998244353) using NTT.

- 17. Compute convolution of integer sequences modulo a prime using NTT.
- 18. Solve polynomial equations in modular arithmetic using NTT.
- 19. Find the number of ways to make a sum using coins (modulo prime) using NTT.
- 20. Efficiently multiply polynomials for combinatorics problems under mod.

V Diophantine Equations

- 21. Solve for integer solutions of ax + by = c.
- 22. Find smallest positive solution of $ax \equiv b \mod m$.
- 23. Count number of solutions of $x^2 + y^2 = z^2$ for given z.
- 24. Solve ax + by + cz = d in integers using parameterization.
- 25. Determine if it's possible to express a number as a linear combination of two given integers.

♥ Gaussian Elimination (Modulo and Floating Point)

- 26. Solve system of linear equations under mod p.
- 27. Find rank of a matrix under modulo arithmetic.
- 28. Compute inverse of a matrix modulo prime.
- 29. Determine consistency and number of solutions of a system of equations.
- 30. Perform Gaussian elimination to solve circuit flow or current balance equations.

V Combinatorics with Generating Functions

- 31. Count number of integer partitions of n into odd parts.
- 32. Use exponential generating functions to count labeled trees.
- 33. Solve linear recurrence using generating function roots.
- 34. Count compositions of n with given part sizes using polynomial multiplication.
- 35. Use generating functions to solve constrained dice roll sums.

⊘ Mobius Inversion

- 36. Count the number of coprime pairs in a given range using Möbius function.
- 37. Compute sum over divisors efficiently using Möbius inversion.
- 38. Invert a Dirichlet convolution for number-theoretic functions.
- 39. Count number of integers whose GCD with n is exactly k.
- 40. Use Möbius inversion to compute primitive necklaces of given length.

⊘ Burnside's Lemma and Polya Enumeration

- 41. Count distinct colorings of a bracelet considering rotation symmetry.
- 42. Count number of non-equivalent ways to color faces of a cube.
- 43. Compute number of unique tilings of a board under rotation.
- 44. Count labeled graphs modulo automorphism using Burnside's lemma.
- 45. Use Polya enumeration to count distinct chemical compound structures.

Let me know if you want full problems, code, or visualizations for any topic.

You said:

. String Algorithms • Suffix Automaton • Z-function, KMP, Aho-Corasick • Manacher's Algorithm • Lyndon Factorization • Palindromic Tree / Eertree • Hashing with Collision Control • Trie with Bitmask Compression

ChatGPT said:

Here are 30 one-line problem statements categorized under advanced String Algorithms:

Suffix Automaton

- 1. Count the number of distinct substrings of a given string.
- 2. Find the length of the longest common substring between two strings.
- 3. Count occurrences of each substring in the input string.
- 4. Given a string and its suffix automaton, answer if a pattern exists as a substring.
- 5. Find the lexicographically smallest substring of length k.

♥ Z-function, KMP, Aho-Corasick

- 6. Find all occurrences of a pattern in a text using Z-algorithm.
- 7. Preprocess a pattern for fast pattern matching using KMP.
- 8. Given multiple patterns, find all their occurrences in a large text (Aho-Corasick).
- 9. Find the smallest period of a string using Z or KMP.
- 10. Detect if any of the banned words (from a list) appear in a message.

⊘ Manacher's Algorithm

- 11. Count total number of palindromic substrings in a string in linear time.
- 12. Find the longest palindromic substring in a given string.
- 13. Check if a string can be made palindrome by changing at most one character.

- 14. Identify the maximum even/odd-length palindrome centered at every index.
- 15. Find the minimal characters to add to make the string a palindrome.

V Lyndon Factorization

- 16. Break a string into lexicographically smallest Lyndon substrings.
- 17. Generate minimal string rotation using Lyndon decomposition.
- 18. Sort all rotations of a string using Lyndon factorization.
- 19. Compress a string using canonical Lyndon factor sequences.
- 20. Find the number of distinct Lyndon factors in a string.

♥ Palindromic Tree / Eertree

- 21. Count how many distinct palindromic substrings exist in a string.
- 22. Insert characters one by one and maintain list of all palindromic suffixes.
- 23. Track longest palindromic suffix after each insertion in a stream.
- 24. For each prefix, find how many new palindromes were formed.
- 25. Calculate palindromic factorizations of a string.

∀ Hashing with Collision Control

- 26. Use double hashing to avoid false positives in substring comparison.
- 27. Compare two substrings for equality in constant time using polynomial hashing.
- 28. Detect repeated substrings of length k using rolling hash.
- 29. Find longest prefix which is also a suffix (not equal to full string).
- 30. Count how many times a pattern appears using hash and sliding window.

♥ Trie with Bitmask Compression

- 31. Store dictionary of words with compressed bitmask nodes to save memory.
- 32. Insert and search words using compressed trie.
- 33. Count how many strings share a given prefix using bitmask trie.
- 34. Find the most frequent prefix in a list of strings using trie + bitmasks.
- 35. Auto-suggest completions based on input prefix using compressed trie structure.

Let me know if you'd like code templates, visualizations, or deep-dive tutorials on any of these.

You said:

Geometry (Advanced) • Convex Hull Trick (CHT) • Rotating Calipers • Line Sweep for Intersections • Segment Intersection using Order Set • Point in Polygon / Convex Hull Inclusion • Circle Intersection and Geometry Tricks

ChatGPT said:

Here are **30 one-line problem statements** categorized under **Advanced Geometry Algorithms**:

♥ Convex Hull Trick (CHT)

- 1. Maintain a set of linear functions and answer min/max at point x.
- 2. Optimize dynamic programming recurrence: dp[i] = min(dp[j] + a[i]*b[j]).
- 3. Compute the minimum cost path through a series of linear decisions.
- 4. Find minimal cost with linear penalty functions over sorted inputs.
- 5. Solve slope-based DP problems efficiently using dynamic or static CHT.

V Rotating Calipers

- 6. Find the diameter (farthest pair of points) of a convex polygon.
- 7. Compute the width of a convex polygon (minimum bounding strip).
- 8. Given a convex polygon, find the pair of sides with the greatest distance.
- 9. Find the maximum area of a triangle that can be inscribed in a convex polygon.
- 10. Use rotating calipers to find maximum rectangle inside a convex polygon.

V Line Sweep for Intersections

- 11. Count number of intersections among a set of horizontal and vertical segments.
- 12. Determine if any pair of segments in the plane intersect.
- 13. Find the leftmost intersection point among a set of line segments.
- 14. Report all intersection points between a set of segments (plane sweep).
- 15. Given rectangles, count how many pairs overlap.

\checkmark Segment Intersection using Order Set

- 16. Detect if any two segments intersect using a balanced BST (sweep line).
- 17. Maintain active segments while sweeping to detect event ordering.
- 18. Report the first intersection point in left-to-right sweep of segments.
- 19. Find all events (insert/remove/intersect) while sweeping through segments.
- 20. Handle dynamic segment insertion and intersection query with ordered sets.

⊘ Point in Polygon / Convex Hull Inclusion

- 21. Determine whether a given point lies inside, outside, or on the boundary of a polygon.
- 22. Check if a point lies inside a convex polygon in O(log N).
- 23. For each query point, check if it lies within the convex hull of given points.
- 24. Classify all points from a list as inside/outside/on polygon.
- 25. Compute convex hull and check if multiple points lie within it.

♥ Circle Intersection and Geometry Tricks

- 26. Count number of intersection points between two circles.
- 27. Compute common chord (line) of two intersecting circles.
- 28. Find area of intersection between two circles.
- 29. Determine number of distinct regions formed by multiple intersecting circles.
- 30. Given multiple circles, find all pairwise intersecting circle pairs.

Let me know if you want **code**, **formulas**, or **visualizations** for any problem type.

You said:

Bitmask & Brute Force • SOS DP (Sum over Subsets) • Meet in the Middle • Inclusion-Exclusion over subsets • Bitwise DP • Digit DP (Harder variations)

ChatGPT said:

Here are **30 one-line problem statements** categorized under **Bitmask & Brute Force** techniques:

∜ SOS DP (Sum Over Subsets DP)

- 1. Given f[mask], compute g[mask] = sum(f[submask]) for all $submask \subseteq mask$.
- 2. Count how many subsets of numbers XOR to a given value.
- 3. For each subset of size k, find the total sum of elements from all smaller subsets.
- 4. Preprocess frequency of elements to quickly answer XOR subset queries.
- 5. Find the number of supersets of every subset satisfying a given property.

⊘ Meet in the Middle

6. Count the number of subsets whose sum equals a target value when n > 30.

- 7. Find closest possible sum to target using subset sums of two halves.
- 8. Given weights, divide them into two sets with minimal difference (balanced partition).
- 9. Count number of triplets summing to target using first-half + second-half pairs.
- 10. Solve bounded knapsack for large constraints using half enumeration.

✓ Inclusion-Exclusion over Subsets

- 11. Count number of integers $\leq N$ divisible by at least one of a given set of primes.
- 12. Count number of ways to place objects where some combinations are forbidden.
- 13. Count subsets that satisfy at least one condition from a list.
- 14. Compute exact number of strings that violate none of the forbidden patterns.
- 15. Count permutations avoiding certain positions using principle of inclusion-exclusion.

Bitwise DP

- 16. Count number of ways to place tiles in a grid using mask-based DP.
- 17. Solve TSP using dp[mask] [last] for up to n = 20 cities.
- 18. Count ways to partition set into groups with no conflicting pairs (bitmask compatibility).
- 19. For a set of strings, find maximum chain such that each word is a subset of the next.
- 20. DP on subsets to build optimal combination of items with bitwise constraints.

V Digit DP (Harder Variations)

- 21. Count numbers \leq N having exactly K non-zero digits.
- 22. Count numbers between L and R such that sum of digits is divisible by D.
- 23. Count numbers in range [L, R] with no adjacent equal digits.
- 24. Count numbers \leq N where digits are strictly increasing.
- 25. Count numbers \leq N with at most two distinct digits.

Mixed / Bonus Problems

- 26. Count valid configurations in a puzzle using full bitmask brute force ($n \le 20$).
- 27. Find number of set bits in binary representations from 1 to N.
- 28. Count palindromes in a number range using digit DP.
- 29. Partition n elements into k groups such that each satisfies a bitmask property.
- 30. Count the number of valid ways to fill a 2 x n board using dominoes with transitions via bitmask DP.