



Bansilal Ramnath Agarwal Charitable Trust's
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Subject Name & Code: **Design and Analysis of Algorithm**

Title of Assignment: **Implement All Pair Shortest paths problem using Floyd's Algorithm.**

Assignment No: 04

Aim:

Implement All Pair Shortest paths problem using Floyd's Algorithm.

Problem Statement:

Implement All Pair Shortest paths problem using Floyd's Algorithm.

Background Information:

The Floyd Warshall Algorithm:

The Floyd Warshall Algorithm is for solving all pairs shortest path problems. The problem is to find the shortest distances between every pair of vertices in each edge-weighted directed Graph.

Algorithm:

- Initialize the solution matrix same as the input graph matrix as a first step.
- Then update the solution matrix by considering all vertices as an intermediate vertex.
- The idea is to one-by-one pick all vertices and updates all shortest paths which include the picked vertex as an intermediate vertex in the shortest path.
- When we pick vertex number k as an intermediate vertex, we already have considered vertices $\{0, 1, 2, \dots, k-1\}$ as intermediate vertices.
- For every pair (i, j) of the source and destination vertices respectively, there are two possible cases.
- k is not an intermediate vertex in shortest path from i to j . We keep the value of $\text{dist}[i][j]$ as it is.
- k is an intermediate vertex in shortest path from i to j . We update the value of $\text{dist}[i][j]$ as $\text{dist}[i][k] + \text{dist}[k][j]$ if $\text{dist}[i][j] > \text{dist}[i][k] + \text{dist}[k][j]$

Software Requirements:

Text Editor: VSCode, Online GDB Compiler

Environment: GCC C++

Program Code:

```
#include <bits/stdc++.h>

using namespace std;

#define V 4

#define INF 99999

void printSolution(int dist[][V]);

void floydWarshall(int graph[][V])
{
    int dist[V][V], i, j, k;

    for (i = 0; i < V; i++)
        for (j = 0; j < V; j++)
            dist[i][j] = graph[i][j];

    for (k = 0; k < V; k++) {
        for (i = 0; i < V; i++) {
            for (j = 0; j < V; j++) {
                if (dist[i][j] > (dist[i][k] + dist[k][j])
                    && (dist[k][j] != INF
                        && dist[i][k] != INF))
                    dist[i][j] = dist[i][k] + dist[k][j];
            }
        }
    }

    printSolution(dist);
}

void printSolution(int dist[][V])
{
    cout << "The following matrix shows the shortest "
           "distances"
           " between every pair of vertices \n";

    for (int i = 0; i < V; i++) {
        for (int j = 0; j < V; j++) {
            if (dist[i][j] == INF)
                cout << "INF"
                    << "    ";
        }
    }
}
```

```

        else
            cout << dist[i][j] << "    ";
        } cout << endl;
    }}int main()
{
    int graph[V][V] = { { 0, 5, INF, 10 },
                        { INF, 0, 3, INF },
                        { INF, INF, 0, 1 },
                        { INF, INF, INF, 0 } };

    floydWarshall(graph);

    return 0;}

```

Output:

```

The following matrix shows the shortest distances between every pair of vertices
0      5      8      9
INF     0      3      4
INF     INF     0      1
INF     INF     INF     0
-----

```

Conclusion:

Implemented All Pairs Shortest Path Problem using Floyd Warshall Algorithm.