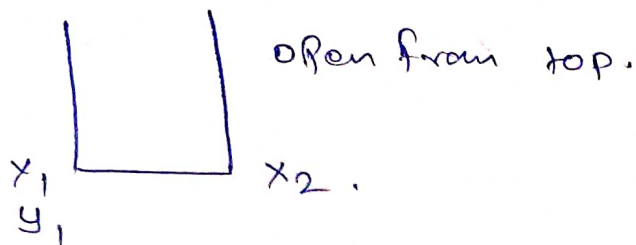


Priority Search Tree

- ① Hybrid of Priority Q. + BST.
- ② Tree data st. to store points in 2D.
- ③ Extension of Priority Q. + Improve search time.
- ④ Set of 2D points ordered by priority + at the same time split by x/y coordinates.
- ⑤ Essentially a heap + BST.
- ⑥ Each node - point in data set.
+ key value (divides the points in left sub tree & right sub tree).
- ⑦ Priority - can be either " x " / " y "
- Not both.
- ⑧ used for unbounded search $[x_1, x_2] [y_1, \dots]$
- ⑨ Unbounded Range Search.

Ex.



Construction Process.

* let S be the set of points.

- ① If S is empty return null.
- ② find point P (with highest value of y coord.) from S and set P as the root R .
- ③ find $S-P$ (remove P from S)
- ④ If $S-P$ is empty, return P .
- ⑤ find $x(P)$ such that x divides points in $S-P$ into 2 equal halves (sets) on x coordi.
- ⑥ Recursively apply above steps on left & rt. child.

Ex. Given points

(25, 35)

(50, 10)

(85, 15)

(90, 5)

(5, 45)

(35, 40)

(60, 75)

(80, 65)

① Sort on x axis.

(5, 45)

(25, 35)

(35, 40)

(50, 10)

(60, 75)

(80, 65)

(85, 15)

(90, 5)

$S = (5, 45) (25, 35) (35, 40) (50, 10) (60, 75)$
 $(80, 65) (85, 15) (90, 5)$

$P = (60, 75)$ Highest y co-ordi.

$S-P = (5, 45) (25, 35) (35, 40) \mid (50, 10) (80, 65)$
 $(90, 5)$

$x(P) = 43$ (Median).

create PST.

$S = (5, 45) (25, 35) (35, 40)$

$P = (5, 45)$

$S-P = (25, 35) \mid (35, 40)$

$x(P) = 30$ (Median).

↓ create PST.

$S = (50, 10) (80, 15)$
 $(90, 5)$

$P = (80, 15)$

$S-P = (50, 10) \mid (90, 5)$



$$S = (25, 35)$$

$$P = (25, 35) \text{ A}$$

$S - P = \text{empty}$

return (A)

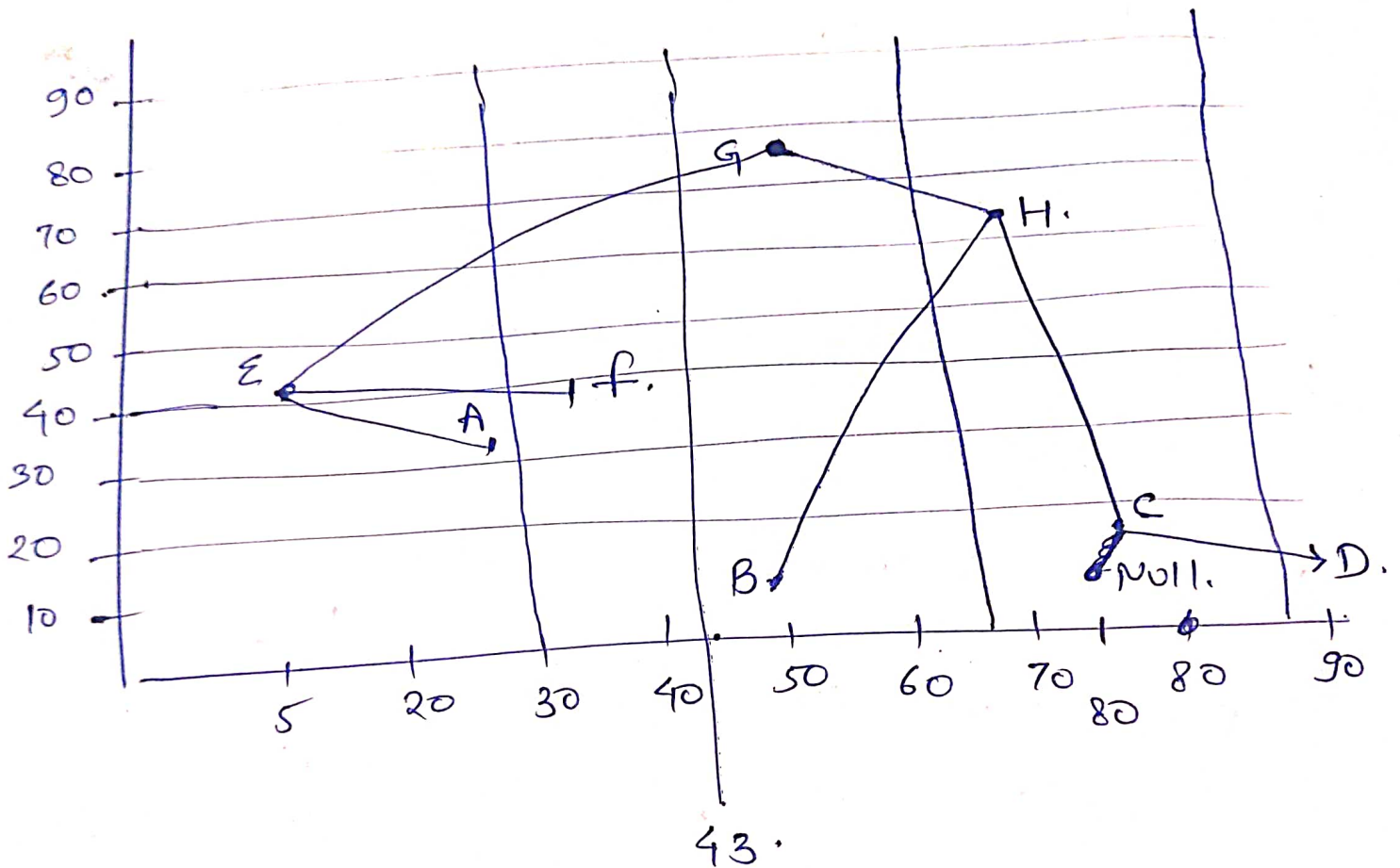


$$S = (35, 40)$$

$$P = f(35, 40)$$

$S - P = \text{empty}$

return f.



pdf.

Brown Uni. Computer Science.

P.S.T. - Part I