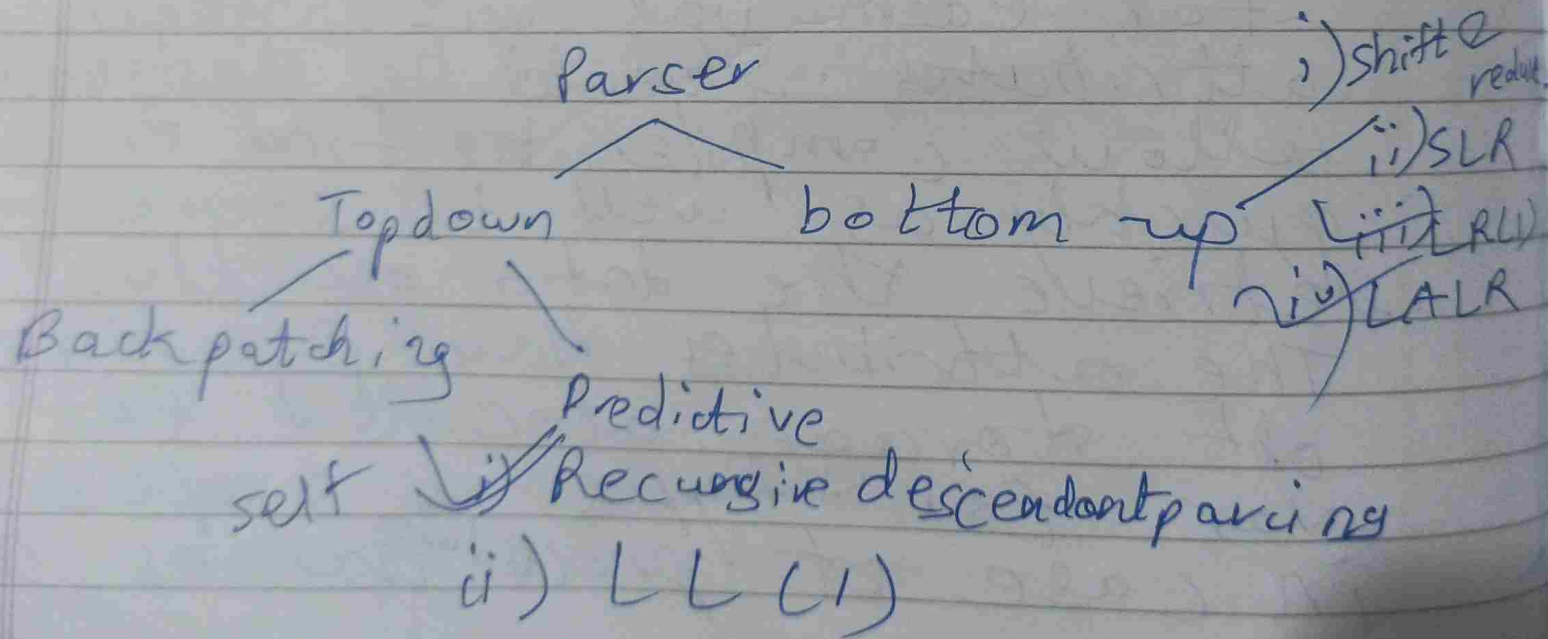
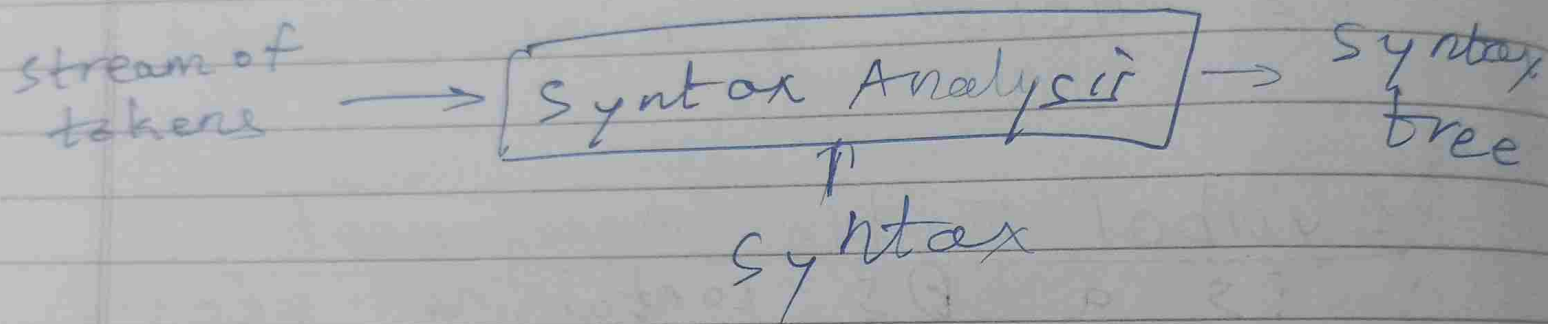


Parser -



to
R/

A
to d
stru
as
seq
op

Gram
G =

Term

alphabet
0-9
generally
lowercase

Parser ↓ Grammar

Set of formal rules which checks correctness of sentence or we can gen syn correct sentence using these rules

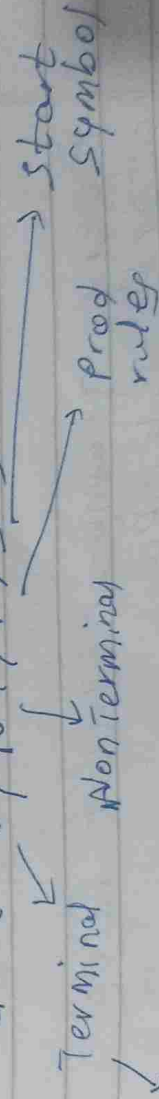
A Grammar G is used basically for 2 purposes

1. To gen valid string for given lang. (Derivation op.)
2. To recognise a valid string for the given lang is called R/reduction op.

A parse tree is used to depict the syntactic structure of a valid string as it emerges during the seq. of derivation & deduction op.

Grammar is quadruple of

$$G = \{ T, NT, P, S \}$$



alphabet

generally lowercase

$$\Sigma = \{a, b, c, \dots, z, 0, \dots, 9\}$$

A string is the finite seq
of symbols rep by roman
symbols $\alpha, \beta, \gamma, \dots$

$$\alpha \xrightarrow{\quad} aob$$

Non terminal is the name of syntax category of lang

e.g. Noun, verb, adj.

Capital letters or <>

Prod rules :- Rules in Grammar

The manner in which terminal and non-terminal can be combined to form a string

NT symbol \Rightarrow string of terminals
~~Q~~ NTs

$\langle \text{article} \rangle = a \mid an \mid the$

Every grammar must have start symbol.

Chomsky Grammars are classified on the nature of production.

Type (0) - Unstructured Grammar

$\alpha \rightarrow \beta$
No restriction

Type (1) - Context sensitive

$\alpha \rightarrow \beta$
except ' ϵ '

start symbol does not appear to the right side of the grammar

Type (2) - Context free grammar

$A \rightarrow \pi_{\text{string}}$

LHS contains only one non terminal

start symbol can appear at RHS.

Type (3) - Regular or linear

LHS only | NT
RHS only | NT

$A \rightarrow t B t$ \rightarrow right linear

$A \rightarrow B t$
 \downarrow
left linear

operator grammar (?)

operation on grammar

derivative

reduction

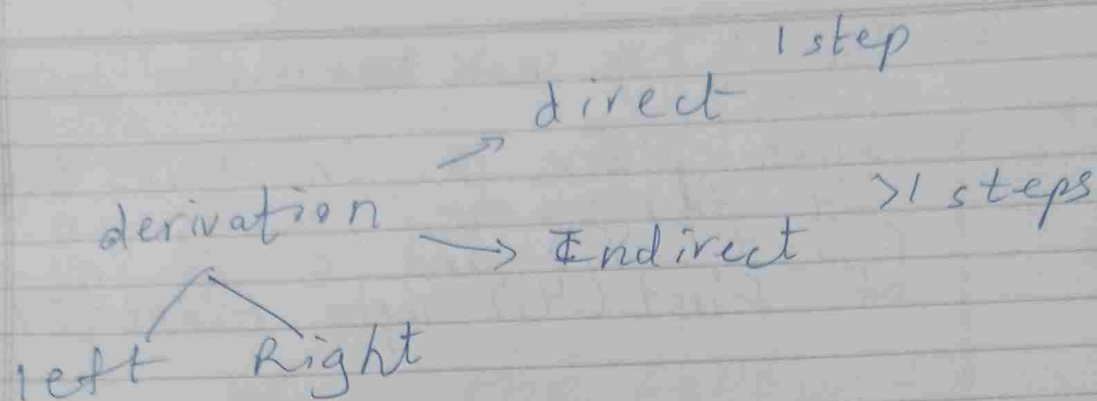
let

$P_1 : A \rightarrow \alpha$

& let B be the string
such that

$B \rightarrow P A \theta$

Then replacement of A
by the string α
according to P_1
is called derivation of



Let

$P_1 : A \rightarrow \alpha$
and let δ be string such
that $\delta \rightarrow \gamma \alpha \theta$ then
replacement of α by NTA
in δ is according to P_1
is called reduction.

Top Down (LL(1))

First & Follow set
 $First(X)$ be the set of the
terminals that begins the
string derived from X
 $First(X) \Rightarrow \{a\}$. If $X \Rightarrow \epsilon$ then
 ϵ is also in the $First(X)$

Rules for First Set

1. If X is a terminal then
 $First(X) \Rightarrow \{X\}$
2. If $X \Rightarrow \epsilon$ then add ϵ in
 $First(X)$

3. If x is non terminal and $x \rightarrow y_1 y_2 \dots$ then place a in $\text{First}(x)$ if for some i , a is in the $\text{First}(y_i)$ and ϵ is in all of $\text{First}(y_1)$ upto $\text{First}(y_{i-1})$

- 1 $E \rightarrow TE'$
- 2 $E' \rightarrow +TE' / \epsilon$
- 3 $T \rightarrow (T'$
- 4 $T' \rightarrow *FT' / \epsilon$
- 5 $F \rightarrow (E) | id$

$$\text{First}(E) = \{$$

$$\text{First}(E) = \text{First}(T) = \text{First}(F)$$

$$= \{ (, id \}$$

$$\text{First}(E') = \{ +, \epsilon \}$$

$$\text{First}(T') = \{ *, \epsilon \}$$

Follow set:-

For non terminal a , is the set of terminals $\{a\}$ that can appear to the right of a in some sentential form $\alpha a \beta$ s.t. there exist

a derivation of the form
 $S \xrightarrow{*} \alpha A \alpha \beta$ for some α, β

Rules:-

1. Place $\$$ in the follow(S)
 $\text{follow}(S) = \{ \$ \}$
end marker
2. If there exists a production
in the form
 $A \rightarrow \alpha B \beta$
Then everything in the $\text{First}(B)$
except ϵ is placed in the
 $\text{follow}(B)$
3. If \exists a production $A \rightarrow \alpha B \beta$, or
 $A \rightarrow \alpha B \beta$, where in the
 $\text{First}(B)$ contains ϵ then
everything in the $\text{follow}(A)$ is
in the $\text{follow}(B)$

$$\text{Follow}(E) = \{ \$, \} \}$$

$$\text{Follow}(E') = \{ \$, \} \}$$

$$\text{Follow}(T) = \text{Follow}(T')$$

$$= \{ \epsilon, \$ \}$$

$\epsilon \rightarrow \text{follow}$
 $\text{else} \rightarrow \text{First}$

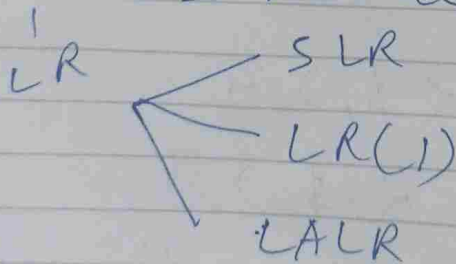
Follow(F) = { +, *,), \$ }

Table M:-

Non Term	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$		$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$	
T	$T \rightarrow FT'$		$T \rightarrow FT'$	$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$	
F	$F \rightarrow id$			$F \rightarrow (E)$		

Bottom Up Parser

shift & Reduce



Bottom up Parser Reduction

~~Top down~~ eg :-

$$\begin{aligned} S &\rightarrow a A B e \\ A &\rightarrow A b c \mid b \\ B &\rightarrow d \end{aligned}$$

$$\begin{aligned} a b b c d e & \\ a A b c d e & \quad \text{rule 2} \\ a A d e & \quad \text{rule 2} \\ a A B e & \quad \text{rule 3} \\ S & \quad \text{rule 1} \end{aligned}$$

$$\begin{aligned} 1 \quad E &\rightarrow E + E \\ 2 \quad E &\rightarrow E * E \\ 3 \quad E &\rightarrow (E) \\ 4 \quad E &\rightarrow id \end{aligned}$$

$$id + id * id.$$

$$E + E * E \quad 4$$

$$E * E \quad 1$$

$$E \quad 2$$

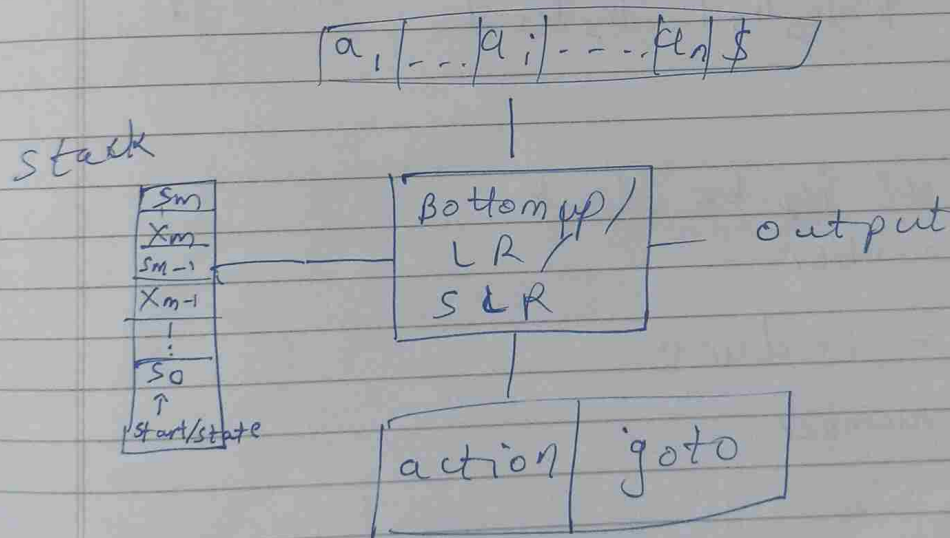
shift, reduce, accept, error

Using shift & Reduce

stack	I/p	Action
\$	id + id * id \$	shift
\$ id		Reduce 3
\$ E	+ id * id \$	shift
\$ E +	id * id \$	shift
\$ E + id	* id \$	Reduce 3
\$ E + E	* id \$	shift
\$ E + E *	id \$	shift
\$ E + E * id	\$	Reduce 3
\$ E + E * E	\$	Reduce 2
\$ E + E	\$	Reduce 1
\$ E	\$	

diff imp
 Topdown
 derivation
 Table M
 First, Follow

classmate
 Date _____
 Page _____
 Bottom up
 Reduction
 Table M
 First, Follow,
 LR(0) items/
 Closure ops
 SLR items
 goto operation



- 1 $E \rightarrow E + T$
- 2 $E \rightarrow T$
- 3 $T \rightarrow T * F$
- 4 $T \rightarrow F$
- 5 $F \rightarrow (E)$
- 6 $F \rightarrow id.$

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Table M:

state	(Terminal)						(Non-Terminal)		
	Action						goto		
	id	+	*	()	\$	E	T	F
0	S ₅			S ₄		accept	1	2	3
1	S ₆								
2	r ₂	S ₇			r ₂	r ₂			
3	r ₄	r ₄			r ₄	r ₄			
4	S ₅			S ₄			8	2	3
5	r ₆	r ₆			r ₆	r ₆			
6	S ₅			S ₄				9	3
7	S ₅			S ₄					10
8	S ₆				S ₁₁				
9	r ₁	S ₇			r ₁	r ₁			
10	r ₃	r ₃			r ₃	r ₃			
11	r ₅	r ₅			r ₅	r ₅			

S₅ = shift i/p to stack
 ↑
 state number

r₂ = reduce
 ↑
 rule number

Stack	LIP	Action
0	$id * id + id \$$	shift
0 id 5	$* id + id \$$	Reduce 6
0 F 3	$* id + id \$$	Reduce 4
0 T 2	$* id + id \$$	shift
0 T 2 * 7	$id + id \$$	shift
0 T 2 * 7 id 5	$+ id \$$	Reduce 6
0 T 2 * 7 F 10	$+ id \$$	Reduce 3
0 T 2	$+ id \$$	Reduce 2
0 E 1	$+ id \$$	shift
0 E 1 + 6	$id \$$	shift
0 E 1 + 6 id 5	$\$$	Reduce 6
0 E 1 + 6 F 3	$\$$	Reduce 4
0 E 1 + 6 T 9	$\$$	Reduce 1
0 E 1	$\$$	Accept

Find states

- 1 $E \rightarrow E + T$
- 2 $E \rightarrow T$
- 3 $T \rightarrow T * F$
- 4 $T \rightarrow F$
- 5 $F \rightarrow (E)$
- 6 $F \rightarrow id$

Augmented Grammar

Rule 0 $E' \rightarrow E$ start symbol
in only 1 rule

Status

0 ✓
1 ✓
2 ✓
3 ✓
4 ✓
5 ✓
6 ✓
7 ✓

I_0 ✓
 $E' \rightarrow \cdot E$
 $E \rightarrow \cdot E + T$
 $E \rightarrow \cdot T$
 $T \rightarrow \cdot T * F$
 $T \rightarrow \cdot F$
 $F \rightarrow \cdot (E)$
 $F \rightarrow \cdot id$

not at start

shift dot by
1 char each
time

End when
dot at right
in all rules

1 shift = 1 state

I_1
 $E' \rightarrow E \cdot$
 $E \rightarrow E \cdot + T$

I_2

$E \rightarrow T \cdot$
 $T \rightarrow T \cdot * F$

I_3

$T \rightarrow F \cdot$

I_4

$I_1 \leftarrow F \rightarrow (\cdot E)$
 $E \rightarrow \cdot E + T$
 $I_2 \leftarrow E \rightarrow \cdot T$
 $T \rightarrow \cdot T * F$

$I_3 \leftarrow T \rightarrow \cdot F$

$F \rightarrow \cdot (E) \rightarrow I_4$
 $F \rightarrow \cdot id \rightarrow I_5$

If dot thru terminal
and next is non terminal
take rule with that
NT, and all NT
in

(I₅)

$F \rightarrow id \cdot$

(T₆)

$E \rightarrow E + \cdot T$

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$

$F \rightarrow \cdot (E)$

$F \rightarrow \cdot id$

(J₇)

$T \rightarrow T * \cdot F$

~~$E \rightarrow \cdot E + T$~~

~~$E \rightarrow \cdot T$~~

~~$T \rightarrow \cdot T * F$~~

~~$T \rightarrow \cdot F$~~

~~$F \rightarrow \cdot (E)$~~

$F \rightarrow \cdot id$

I₈

$F \rightarrow (E \cdot)$

Parsing Algo

i/p \rightarrow grammar

o/p \rightarrow Table M

Method:

1. $C = \{ I_0, \dots, I_n \}$ collection of Canonical set for G
2. State i is constructed from I_i

The parsing action for state i are determined as follows

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a) If $[A \rightarrow \alpha \cdot a \beta]$ is in I_i ^{Terminal}
then goto $[I_i, a] = I_j$
"shift" set action $[i, a]$ to "shift"

b) If $[A \rightarrow \alpha \cdot]$ is in I_i
then ~~set~~ set action "reduce
 $A \rightarrow \alpha$ " for all α in follow
of A

c) If $[S' \rightarrow s \cdot]$ is in I_i then
action $[i, \$]$ to "accept"

3. The goto transition for
state i is constructed
only for NT

If goto $[I_i, A] = I_j$ then
goto $(i, A) = j$

4. If 2 & 3 are not defined
any entry then error

GOTO

Mtable

$\therefore OE \rightarrow 1$

$I_0 \rightarrow I_1$

$E \rightarrow E$

$E \rightarrow E$

$I_0 \rightarrow I_2$

$OT \rightarrow 2$

$E \rightarrow T$

$E \rightarrow T$

SHEET

$I_1 \rightarrow I_6$

$1+ \rightarrow S6$

$E \rightarrow E + T$

$E \rightarrow E + T$

do + thru
NT A from
 I_i to I_j

$I_0 \rightarrow I_4$

$0L \rightarrow S4$

$F \rightarrow (E)$ $F \rightarrow (E)$

Follow set

$E' \rightarrow \{ \$ \}$

$E \rightarrow \{ \$, +,) \}$

$T \rightarrow \{ \$, +, *, \}$

$F \rightarrow \{ \$, +,), * \}$