

Digital Imaging Systems Project 01

Q1

Q1 a)

In [1]:

```
1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4 from IPython.display import Image
5
6 %matplotlib inline
```

In [2]:

```
1 image = cv2.imread("lena.png")
2 gray_image = cv2.cvtColor(image, cv2.COLOR_BGR2GRAY)
3 gray_image.shape
```

Out[2]:

(440, 440)

In [3]:

```
1 image_wolves = cv2.imread("wolves.png")
```

In [4]:

```
1 image1 = cv2.cvtColor(image, cv2.COLOR_BGR2RGB)
2 plt.imshow(image1)
3 plt.title('Color Lena Image')
4 plt.axis('off')
5 plt.show()
```

Color Lena Image



In [5]:

```
1 image_wolves = cv2.cvtColor(image_wolves, cv2.COLOR_BGR2RGB)
2 plt.imshow(image_wolves)
3 plt.title('Wolves color')
4 plt.axis('off')
5 plt.show()
```

Wolves color



In [6]:

```
1 plt.imshow(gray_image, cmap = "gray")
2 plt.title('Gray Lena Image')
3 plt.axis('off')
4 plt.show()
```

Gray Lena Image



Padding function

In [7]:

```

1  #pad is value of padding and is initialized to zero
2  #kernel_rows
3  #kernel_cols
4
5  def padding(input_image, pad = 0, kernel_rows = 0, kernel_cols = 0):
6
7      #pad = 0 for zero padding
8      #pad = 1 for wrap around
9      #pad = 2 for copy edge
10     #pad = 3 for reflect across edge
11
12     input_dims = (input_image.shape[0], input_image.shape[1])
13
14     #individual padding values for rows
15     top_row_pad_value = int(np.ceil((kernel_rows-1)/2))
16     bottom_row_pad_value = int(np.floor((kernel_rows-1)/2))
17
18     #individual padding values for cols
19     left_col_pad_value = int(np.ceil((kernel_cols-1)/2))
20     right_col_pad_value = int(np.floor((kernel_cols-1)/2))
21
22     if pad == 0:
23         #zero padding
24         padded_dims = (input_image.shape[0] + top_row_pad_value + bottom_row_pad_value
25                        input_image.shape[1] + left_col_pad_value + right_col_pad_value
26
27         padded_image = np.zeros(padded_dims)
28
29         #inserting the original image to the zeros image
30         padded_image[top_row_pad_value : top_row_pad_value + input_image.shape[0],
31                      left_col_pad_value : left_col_pad_value + input_image.shape[1]] =
32
33     if pad == 1:
34
35         #wrap around
36         padded_dims = (input_image.shape[0] + top_row_pad_value + bottom_row_pad_value
37                        input_image.shape[1] + left_col_pad_value + right_col_pad_value
38
39         padded_image = np.zeros(padded_dims)
40
41         #inserting the original image to the zeros image
42         padded_image[top_row_pad_value : top_row_pad_value + input_image.shape[0],
43                      left_col_pad_value : left_col_pad_value + input_image.shape[1]] =
44
45
46         #upper most row padding
47         if top_row_pad_value != 0:
48             padded_image[0 : top_row_pad_value, : ] = padded_image[-1*(top_row_pad_val
49         #lowest row padding
50         if bottom_row_pad_value != 0:
51             padded_image[-1*(bottom_row_pad_value) : , : ] = padded_image[top_row_pad_
52         #right most column padding
53         if right_col_pad_value != 0:
54             padded_image[ : ,-1*(right_col_pad_value) : ] = padded_image[ : ,left_col_
55         #left most column padding
56         if left_col_pad_value != 0:
57             padded_image[ : ,0 : left_col_pad_value] = padded_image[ : ,-1*(left_col_p
58
59     if pad == 2:

```

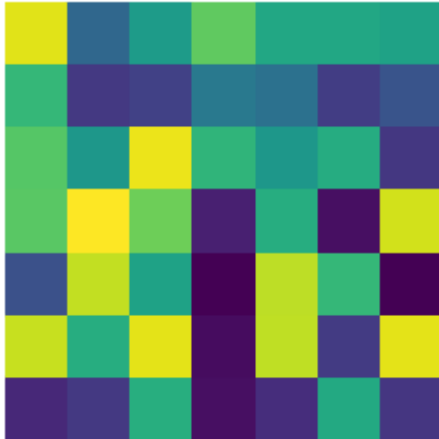
```

60
61     #copy edge
62     padded_dims = (input_image.shape[0] + top_row_pad_value + bottom_row_pad_value
63                    input_image.shape[1] + left_col_pad_value + right_col_pad_value
64
65     #print(padded_dims)
66     padded_image = np.zeros(padded_dims)#.astype(int)
67     #print("Dimensions of the padded image:", padded_image.shape)
68
69     #inserting the original image to the zeros image
70     padded_image[top_row_pad_value : top_row_pad_value + input_image.shape[0],
71                  left_col_pad_value : left_col_pad_value + input_image.shape[1]] =
72
73
74     #upper most row padding
75     if top_row_pad_value != 0:
76         padded_image[0 : top_row_pad_value, : ] = padded_image[[top_row_pad_value]
77     #lowest row padding
78     if bottom_row_pad_value != 0:
79         padded_image[-1*(bottom_row_pad_value) : , : ] = padded_image[[-1*bottom_r
80     #right most column padding
81     if right_col_pad_value != 0:
82         padded_image[ : ,-1*(right_col_pad_value) : ] = padded_image[ : ,[-1*(righ
83     #left most column padding
84     if left_col_pad_value != 0:
85         padded_image[ : ,0 : left_col_pad_value] = padded_image[ : ,[left_col_pad_
86
87 if pad == 3:
88
89     #reflect across edge
90     padded_dims = (input_image.shape[0] + top_row_pad_value + bottom_row_pad_value
91                    input_image.shape[1] + left_col_pad_value + right_col_pad_value
92
93     #print(padded_dims)
94     padded_image = np.zeros(padded_dims)#.astype(int)
95     #print("Dimensions of the padded image:", padded_image.shape)
96
97     #inserting the original image to the zeros image
98     padded_image[top_row_pad_value : top_row_pad_value + input_image.shape[0],
99                  left_col_pad_value : left_col_pad_value + input_image.shape[1]] =
100
101
102     #upper most row padding
103     if top_row_pad_value != 0:
104         padded_image[0 : top_row_pad_value, : ] = np.flip(padded_image[top_row_pad
105     #lowest row padding
106     if bottom_row_pad_value != 0:
107         padded_image[-1*(bottom_row_pad_value) : , : ] = np.flip(padded_image[-2*(
108     #right most column padding
109     if right_col_pad_value != 0:
110         padded_image[ : ,-1*(right_col_pad_value) : ] = np.flip(padded_image[ : ,-
111     #left most column padding
112     if left_col_pad_value != 0:
113         padded_image[ : ,0 : left_col_pad_value] = np.flip(padded_image[ : ,left_c
114
115     return padded_image

```

In [8]:

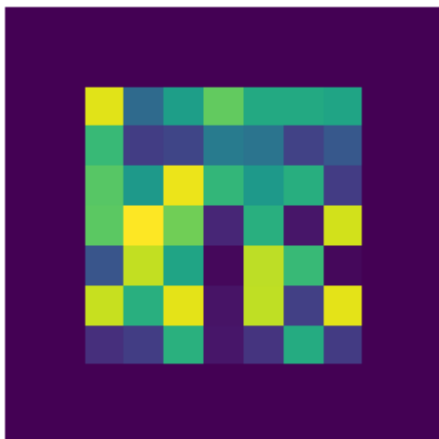
```
1 #random image to visualize padding
2 test_image_1 = np.random.randint(0,255,(7,7), dtype = np.uint8)
3 plt.imshow(test_image_1)
4 plt.axis('off')
5 plt.show()
```



Zero Padding

In [9]:

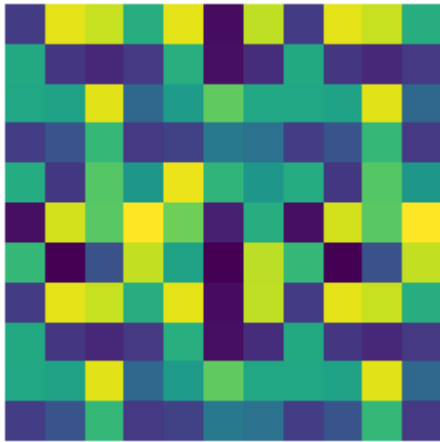
```
1 Image = padding(test_image_1, 0, 5, 5)
2 plt.imshow(Image)
3 plt.axis('off')
4 plt.show()
```



Wrap around Padding

In [10]:

```
1 Image = padding(test_image_1, 1, 5, 5)
2 plt.imshow(Image)
3 plt.axis('off')
4 plt.show()
```



Copy Edge Padding

In [11]:

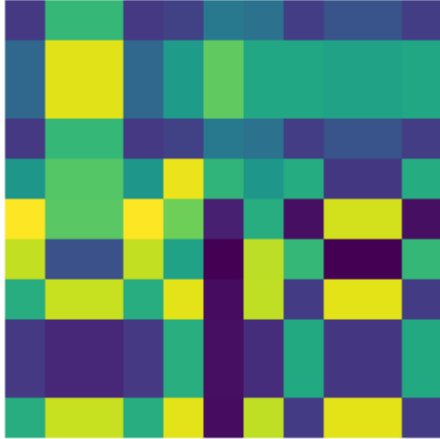
```
1 Image = padding(test_image_1, 2, 5, 5)
2 plt.imshow(Image)
3 plt.axis('off')
4 plt.show()
```



Reflect Edge Padding

In [12]:

```
1 #reflect edge padding
2 Image = padding(test_image_1, 3, 5, 5)
3 plt.imshow(Image)
4 plt.axis('off')
5 plt.show()
```



Function that multiplies the sub-image of the image(f) with the kernel

In [13]:

```
1 def convolution(f,w):
2
3     return np.sum(f*w)
```

Conv2 Function

In [14]:

```

1  def conv2(f,w,pad = 0):
2
3      if len(f.shape)< 3:
4
5          image_padded = padding(f, pad, w.shape[0], w.shape[1])
6
7          conv_image = np.zeros((f.shape[0], f.shape[1]))
8
9          for row in range(conv_image.shape[0]):
10
11              for col in range(conv_image.shape[1]):
12
13                  conv_image[row][col] = convolution(image_padded[row:row+w.shape[0],col:col+w.shape[1]],w)
14
15          return conv_image
16
17
18      elif len(f.shape) == 3:
19
20          b,g,r = cv2.split(f)
21
22          image_padded_b = padding(b, pad, w.shape[0], w.shape[1])
23          image_padded_g = padding(g, pad, w.shape[0], w.shape[1])
24          image_padded_r = padding(r, pad, w.shape[0], w.shape[1])
25
26          conv_image_b = np.zeros((b.shape[0],b.shape[1]))
27          conv_image_g = np.zeros((g.shape[0],g.shape[1]))
28          conv_image_r = np.zeros((r.shape[0],r.shape[1]))
29
30          for row in range(conv_image_b.shape[0]):
31
32              for col in range(conv_image_b.shape[1]):
33
34                  conv_image_b[row][col] = convolution(image_padded_b[row:row + w.shape[0],col:col + w.shape[1]],w)
35                  conv_image_g[row][col] = convolution(image_padded_g[row:row + w.shape[0],col:col + w.shape[1]],w)
36                  conv_image_r[row][col] = convolution(image_padded_r[row:row + w.shape[0],col:col + w.shape[1]],w)
37
38          conv_image = cv2.merge((conv_image_b, conv_image_g, conv_image_r)).astype(np.uint8)
39
40
41          return conv_image

```

Testing on a simple image

In [15]:

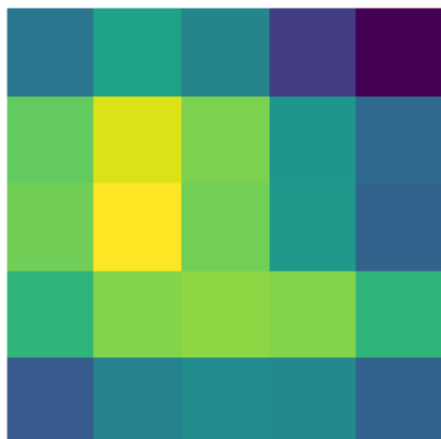
```
1 test_image_1 = np.random.randint(0,255,(5,5), dtype = np.uint8)
2 plt.imshow(test_image_1)
3 plt.axis('off')
4 plt.show()
```



In [16]:

```
1 # box filter on color image
2 w = 1/9*np.ones((3,3))
3 g = conv2(test_image_1,w,0)
4 plt.imshow(g)
5 plt.title('Convolution with 3*3 Box Filter on test image')
6 plt.axis('off')
7 plt.show()
```

Convolution with 3*3 Box Filter on test image



Box Filter on the lena image

In [17]:

```
1 # box filter on color image
2 w = 1/9*np.ones((3,3))
3 g = conv2(image1,w,0)
4 plt.imshow(g)
5 plt.title('3*3 Box Filter on gray image')
6 plt.axis('off')
7 plt.show()
```

3*3 Box Filter on gray image



Box Filter on wolves image

In [18]:

```
1 w = 1/9*np.ones((3,3))
2 g = conv2(image_wolves,w,0)
3 plt.imshow(g)
4 plt.title('3*3 Box Filter on color image')
5 plt.axis('off')
6 plt.show()
```

3*3 Box Filter on color image

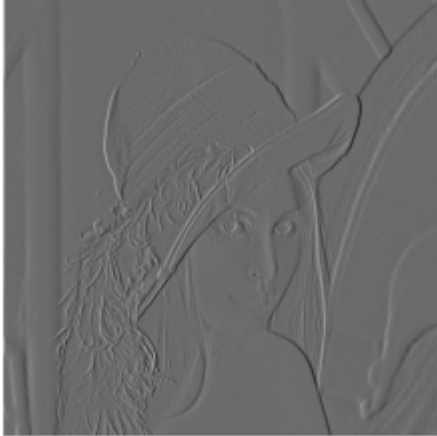


First Order Derivative Filter

In [19]:

```
1 w = np.array([[ -1,1]])
2 g = conv2(gray_image,w,0)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('First order derivative Filter on gray image (Mx)')
5 plt.axis('off')
6 plt.show()
```

First order derivative Filter on gray image (Mx)



In [20]:

```
1 w = np.array([[ -1], [1]])
2 g = conv2(gray_image,w,0)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('First order derivative Filter on gray image (My)')
5 plt.axis('off')
6 plt.show()
```

First order derivative Filter on gray image (My)



Prewitt Filter

In [21]:

```
1 #prewitt filter on gray image
2 w = np.array([[ -1,0,1],[ -1,0,1],[ -1,0,1]])
3 g = conv2(gray_image,w,0)
4 plt.imshow(g, cmap = 'gray')
5 plt.title('Prewitt Filter on gray image (Mx)')
6 plt.axis('off')
7 plt.show()
```

Prewitt Filter on gray image (Mx)



In [22]:

```
1 w = np.array([[1,1,1],[0,0,0],[ -1,-1,-1]])
2 g = conv2(gray_image,w,0)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('Prewitt Filter on gray image (My)')
5 plt.axis('off')
6 plt.show()
```

Prewitt Filter on gray image (My)



Roberts Filter

In [23]:

```
1 w = np.array([[0,1],[-1,0]])
2 g = conv2(gray_image,w,0)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('Roberts Filter on gray image (Mx)')
5 plt.axis('off')
6 plt.show()
```

Roberts Filter on gray image (Mx)



In [24]:

```
1 w = np.array([[0,1],[-1,0]])
2 g = conv2(image1,w,0)
3 plt.imshow(g)
4 plt.title('Roberts Filter on color image (Mx)')
5 plt.axis('off')
6 plt.show()
```

Roberts Filter on color image (Mx)



In [25]:

```
1 w = np.array([[1,0],[0,-1]])
2 g = conv2(image1,w,0)
3 plt.imshow(g)
4 plt.title('Roberts Filter on color image (My)')
5 plt.axis('off')
6 plt.show()
```

Roberts Filter on color image (My)

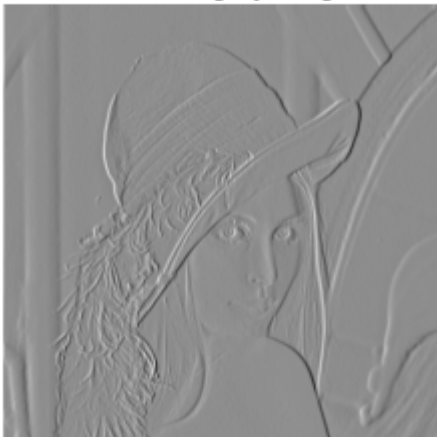


Sobel Filter

In [26]:

```
1 w = np.array([[ -1,0,1],[-2,0,2],[ -1,0,1]])
2 g = conv2(gray_image,w,0)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('Sobel Filter on gray image (Mx)')
5 plt.axis('off')
6 plt.show()
```

Sobel Filter on gray image (Mx)



In [27]:

```
1 w = np.array([[ -1, -2, -1], [0, 0, 0], [1, 2, 1]])
2 g = conv2(gray_image, w, 1)
3 plt.imshow(g, cmap = 'gray')
4 plt.title('Sobel Filter on gray image (My)')
5 plt.axis('off')
6 plt.show()
```

Sobel Filter on gray image (My)

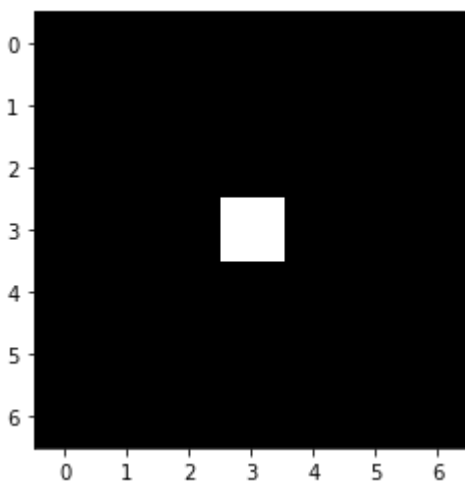


Q.1 b)

Visualizing the slice of the impulse image

In [28]:

```
1 impulse_image = np.zeros((1024,1024))
2 impulse_image[512,512] = 1
3 plt.imshow(impulse_image[509:516,509:516], cmap = 'gray')
4 plt.show()
```

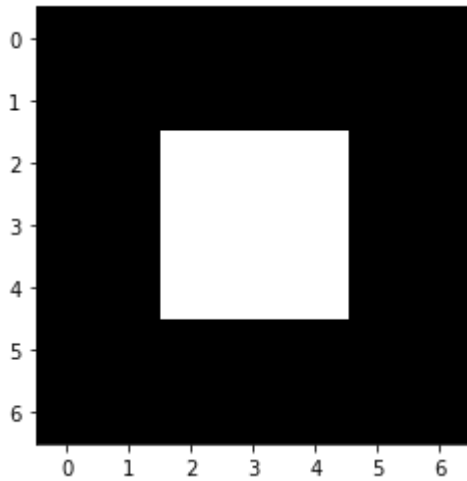


In [29]:

```

1 kernel = 1/9*np.ones((3,3))
2 impulse_conv = conv2(impulse_image, kernel,0)
3 impulse_conv[509:516,509:516]
4 plt.imshow(impulse_conv[509:516,509:516], cmap = 'gray')
5 plt.show()

```



In [30]:

```

1 print(impulse_conv[510:515,510:515])

```

```

[[0.      0.      0.      0.      0.      ]
 [0.      0.11111111 0.11111111 0.11111111 0.      ]
 [0.      0.11111111 0.11111111 0.11111111 0.      ]
 [0.      0.11111111 0.11111111 0.11111111 0.      ]
 [0.      0.      0.      0.      0.      ]]

```

Answer:

The average filter will average out the neighbouring pixel values and the impulse response location and this shows the convolution being performed. Passing the impulse through any function should give the output of the function at the location of that impulse. Eg. The averaging filter in our case $1/9[[1,1,1],[1,1,1],[1,1,1]]$ will give $1/9$ at the location of the impulse.

Q2

Q2 a)

Implementing and testing 2D FFT

In [1]:

```
1 import numpy as np
2 import cv2
3 import matplotlib.pyplot as plt
4
5 %matplotlib inline
```

In [2]:

```
1 image = cv2.imread("lena.png")
2 gray_image = cv2.cvtColor(image, cv2.COLOR_BGR2GRAY)
3 gray_image.shape
```

Out[2]:

(440, 440)

In [3]:

```
1 image = cv2.cvtColor(image, cv2.COLOR_BGR2RGB)
2 plt.imshow(image)
3 plt.axis('off')
4 plt.title('Color Image')
5 plt.show()
```

Color Image



In [4]:

```
1 plt.imshow(gray_image, cmap = "gray")
2 plt.axis('off')
3 plt.title('Gray Image')
4 plt.show()
```

Gray Image



scaling down the pixel values in the lena image to the range - [0,1]

In [5]:

```
1 def scaling_image(input_image):
2
3     scaled_input_image = np.zeros((input_image.shape[0],input_image.shape[1]),dtype = 'float32')
4
5     for row in range(input_image.shape[0]):
6
7         for col in range(input_image.shape[1]):
8
9             scaled_input_image[row,col] = input_image[row,col].astype('float32')/255.
10
11     return scaled_input_image
```

In [6]:

```
1 scaled_image = scaling_image(gray_image)
2 scaled_image
```

Out[6]:

```
array([[0.63529414, 0.63529414, 0.6313726 , ..., 0.6745098 , 0.627451 ,
        0.5137255 ],
       [0.63529414, 0.63529414, 0.6313726 , ..., 0.6745098 , 0.627451 ,
        0.5137255 ],
       [0.63529414, 0.63529414, 0.6313726 , ..., 0.67058825, 0.61960787,
        0.50980395],
       ...,
       [0.16862746, 0.1764706 , 0.19215687, ..., 0.40784314, 0.39607844,
        0.38039216],
       [0.16862746, 0.18431373, 0.20392157, ..., 0.4 , 0.40784314,
        0.4117647 ],
       [0.17254902, 0.18431373, 0.21176471, ..., 0.39607844, 0.4117647 ,
        0.42352942]], dtype=float32)
```

In [7]:

```
1 gray_image
```

Out[7]:

```
array([[162, 162, 161, ..., 172, 160, 131],
       [162, 162, 161, ..., 172, 160, 131],
       [162, 162, 161, ..., 171, 158, 130],
       ...,
       [ 43,  45,  49, ..., 104, 101,  97],
       [ 43,  47,  52, ..., 102, 104, 105],
       [ 44,  47,  54, ..., 101, 105, 108]], dtype=uint8)
```

DFT2 function

In [8]:

```
1 def DFT2(input_image):
2     fft1_image = np.zeros((input_image.shape[0], input_image.shape[1]), dtype = 'complex')
3     fft2_image = np.zeros((input_image.shape[0], input_image.shape[1]), dtype = 'complex')
4     for row in range(input_image.shape[0]):
5
6         fft1_image[row, :] = np.fft.fft(input_image[row, :])
7
8     for col in range(fft1_image.shape[1]):
9
10        fft2_image[:, col] = np.fft.fft(fft1_image[:, col])
11
12    return fft2_image
```

In [9]:

```

1 # scaled_image(passed in the dft2 function below) is the scaled down image of the gray
2 f = DFT2(scaled_image)
3 f

```

Out[9]:

```

array([[ 9.41791595e+04   +0.j           , -1.32605217e+03+6928.26008459j,
        4.45443677e+03-3279.87446605j, ...,
        -6.91412729e+02-1838.48699722j,  4.45443677e+03+3279.87446605j,
        -1.32605217e+03-6928.26008459j],
       [-8.37846430e+01-3545.76435384j, -4.60583848e+03+4606.16030199j,
        -3.20398722e+03 +217.75357611j, ...,
        1.89208271e+03+2351.68299707j, -1.02786249e+03+1296.80102976j,
        1.02025131e+02+2741.4323825j ],
       [-1.30229192e+03 -475.37879051j, -7.95709409e+02 -387.10940328j,
        1.93767512e+03-1311.96666989j, ...,
        1.02391899e+03+2684.36743376j, -2.09555156e+03 -509.04877382j,
        2.37833145e+03 -182.71618199j],
       ...,
       [ 1.49437918e+03 -627.39367783j,  2.13376237e+03+2046.8179341j ,
        -1.52536299e+03 -580.14642037j, ...,
        2.87895939e+03 +316.70306245j,  3.76828573e+02-1965.96863635j,
        -1.56015196e+02+1749.10240541j],
       [-1.30229192e+03 +475.37879051j,  2.37833145e+03 +182.71618199j,
        -2.09555156e+03 +509.04877382j, ...,
        -1.50090182e+03-2181.31083998j,  1.93767512e+03+1311.96666989j,
        -7.95709409e+02 +387.10940328j],
       [-8.37846430e+01+3545.76435384j,  1.02025131e+02-2741.4323825j ,
        -1.02786249e+03-1296.80102976j, ...,
        -1.48190256e+03+5509.44338343j, -3.20398722e+03 -217.75357611j,
        -4.60583848e+03-4606.16030199j]])

```

Spectrum of the image

In [10]:

```

1 def spectrum(input_image):
2     result = np.sqrt(np.real(input_image)**2+np.imag(input_image)**2)
3     return result

```

In [11]:

```
1 spectrum_lena = spectrum(f)
2 spectrum_lena
```

Out[11]:

```
array([[94179.15949942, 7054.02028248, 5531.68902172, ...,
        1964.20111018, 5531.68902172, 7054.02028248],
       [ 3546.75411036, 6513.86681256, 3211.37832252, ...,
        3018.34224132, 1654.74898476, 2743.33020891],
       [ 1386.34384168, 884.87691467, 2340.05157947, ...,
        2873.01907695, 2156.4941446 , 2385.33974633],
       ...,
       [ 1620.73809423, 2956.75590758, 1631.96266168, ...,
        2896.32663543, 2001.75734113, 1756.04668675],
       [ 1386.34384168, 2385.33974633, 2156.4941446 , ...,
        2647.7959258 , 2340.05157947, 884.87691467],
       [ 3546.75411036, 2743.33020891, 1654.74898476, ...,
        5705.2608703 , 3211.37832252, 6513.86681256]])
```

In [12]:

```
1 s = np.log(1+abs(f))
2 s
```

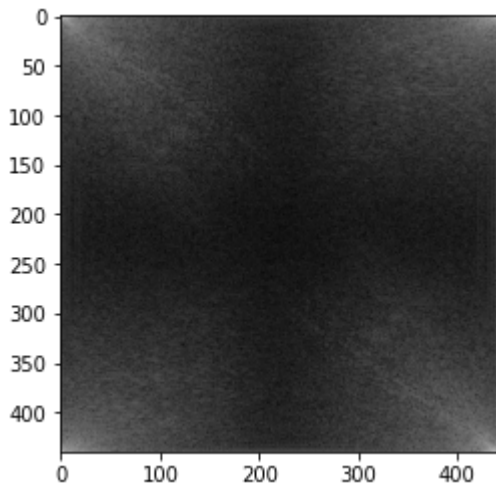
Out[12]:

```
array([[11.45296482, 8.86149474, 8.61842924, ..., 7.58334987,
        8.61842924, 8.86149474],
       [ 8.17407004, 8.78184205, 8.07476685, ..., 8.01279429,
        7.41200874, 7.91729232],
       [ 7.23514629, 6.78657802, 7.7583555 , ..., 7.9634667 ,
        7.67670271, 7.77751598],
       ...,
       [ 7.39125375, 7.99218612, 7.39815123, ..., 7.97154374,
        7.60228018, 7.47138966],
       [ 7.23514629, 7.77751598, 7.67670271, ..., 7.88186045,
        7.7583555 , 6.78657802],
       [ 8.17407004, 7.91729232, 7.41200874, ..., 8.64931925,
        8.07476685, 8.78184205]])
```

Plotting the spectrum

In [13]:

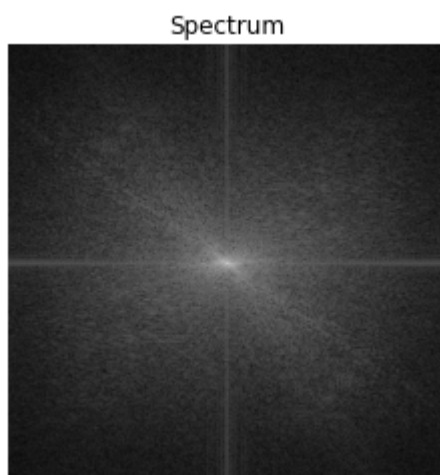
```
1 plt.imshow(s, cmap = 'gray')
2 plt.show()
```



Visualizing the shifted spectrum

In [14]:

```
1 s_shifted = np.fft.fftshift(f)
2 s_shifted = np.log(1+abs(s_shifted))
3
4 plt.imshow(s_shifted, cmap = 'gray')
5 plt.title('Spectrum')
6 plt.axis('off')
7 plt.show()
```



Calculating the phase angle

In [15]:

```
1 angle = np.arctan2(np.imag(f),np.real(f))
2 angle
```

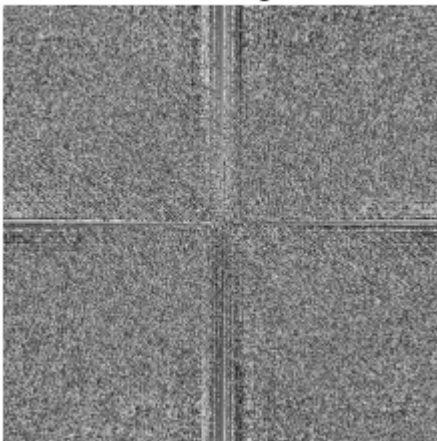
Out[15]:

```
array([[ 0.          ,  1.75990681, -0.63468588, ..., -1.93051091,
        0.63468588, -1.75990681],
       [-1.59442143,  2.35615956,  3.0737337 , ...,  0.89327781,
        2.24101728,  1.5335975  ],
       [-2.79158918, -2.68880653, -0.59517921, ...,  1.20639361,
        -2.90328972, -0.07667475],
       ...,
       [-0.39748829,  0.76460394, -2.77815439, ...,  0.10956554,
        -1.38141749,  1.65975818],
       [ 2.79158918,  0.07667475,  2.90328972, ..., -2.17347289,
        0.59517921,  2.68880653],
       [ 1.59442143, -1.5335975 , -2.24101728, ...,  1.83355257,
        -3.0737337 , -2.35615956]])
```

In [16]:

```
1 angle = np.fft.fftshift(angle)
2 plt.imshow(angle, cmap = 'gray')
3 plt.axis('off')
4 plt.title('Phase angle')
5 plt.show()
```

Phase angle



Q2 b)

IDFT2 function

In [17]:

```

1 def IDFT2(dft2_image):
2     swapped = np.imag(dft2_image) + complex('j') * np.real(dft2_image)
3     swapped_dft2_image = DFT2(swapped)
4     idft2_image = np.imag(swapped_dft2_image) + complex('j') * np.real(swapped_dft2_image)
5
6     return idft2_image/(idft2_image.shape[0]*idft2_image.shape[1])

```

In [18]:

```

1 g = IDFT2(f)
2 g
3 g_real = np.real(g)

```

In [19]:

```
1 np.imag(g)
```

Out[19]:

```

array([[ -1.40468696e-17,  1.82816020e-17,  3.26409906e-17, ...,
        -1.96882383e-17, -1.66316024e-17, -6.37847972e-18],
       [ -5.31418559e-18,  3.86877384e-18, -6.78568986e-18, ...,
        -3.37361671e-17, -4.02593538e-17, -3.19379713e-17],
       [ -3.23976634e-17,  1.13817035e-17, -1.49609685e-17, ...,
        -8.48702578e-17, -2.75686755e-17,  2.25423713e-17],
       ...,
       [ -3.00014228e-17, -1.65967360e-17, -4.16570256e-17, ...,
        -5.75406449e-17, -3.94259719e-17, -1.29446169e-17],
       [ -7.50018658e-17, -3.13495481e-17, -4.42679008e-18, ...,
         1.14749351e-17, -3.14773350e-17, -1.75458419e-17],
       [ -5.34013569e-17, -4.81203418e-17, -9.69945350e-18, ...,
         3.76586897e-17, -8.79412950e-18, -9.47196273e-18]])

```

In [20]:

```

1 d = scaled_image - g_real
2 d

```

Out[20]:

```

array([[ 0.00000000e+00, -1.11022302e-16, -1.11022302e-16, ...,
        -1.11022302e-16, -2.22044605e-16, -2.22044605e-16],
       [ 2.22044605e-16,  0.00000000e+00,  0.00000000e+00, ...,
         1.11022302e-16,  0.00000000e+00,  0.00000000e+00],
       [ -1.11022302e-16,  0.00000000e+00,  0.00000000e+00, ...,
         0.00000000e+00,  0.00000000e+00,  0.00000000e+00],
       ...,
       [ -5.55111512e-17, -1.66533454e-16, -2.77555756e-17, ...,
        -1.66533454e-16, -5.55111512e-17, -1.11022302e-16],
       [ -5.55111512e-17, -5.55111512e-17, -2.77555756e-17, ...,
        -1.66533454e-16, -1.66533454e-16, -2.77555756e-16],
       [ 0.00000000e+00, -8.32667268e-17, -2.77555756e-17, ...,
        -1.66533454e-16, -5.55111512e-17, -5.55111512e-17]])

```


In [21]:

1 g_real

Out[21]:

```
array([[0.63529414, 0.63529414, 0.63137257, ..., 0.67450982, 0.627451 ,
        0.51372552],
       [0.63529414, 0.63529414, 0.63137257, ..., 0.67450982, 0.627451 ,
        0.51372552],
       [0.63529414, 0.63529414, 0.63137257, ..., 0.67058825, 0.61960787,
        0.50980395],
       ...,
       [0.16862746, 0.17647059, 0.19215687, ..., 0.40784314, 0.39607844,
        0.38039216],
       [0.16862746, 0.18431373, 0.20392157, ..., 0.40000001, 0.40784314,
        0.41176471],
       [0.17254902, 0.18431373, 0.21176471, ..., 0.39607844, 0.41176471,
        0.42352942]])
```

In [22]:

1 d2 = gray_image - (g_real * 255).astype(np.uint8)

In [23]:

1 d2

Out[23]:

```
array([[0, 0, 0, ..., 0, 0, 0],
       [0, 0, 0, ..., 0, 0, 0],
       [0, 0, 0, ..., 0, 0, 0],
       ...,
       [0, 0, 0, ..., 0, 0, 0],
       [0, 0, 0, ..., 0, 0, 0],
       [0, 0, 0, ..., 0, 0, 0]], dtype=uint8)
```

Plot of the difference between the original image and the inverse fourier transformed image

In [24]:

```
1 plt.imshow(d2, cmap = "gray")  
2 plt.axis('off')  
3 plt.show()
```



In [25]:

```
1 # got a black image which means there is no difference
```