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Question 1:

Prove that following by using the principle of mathematical induction for all $n \in N$:

$$1 + 3 + 3^2 + \dots + 3^{n-1} = \frac{(3^n - 1)}{2}$$

Solution 1:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1 + 3 + 3^2 + \dots + 3^{n-1} = \frac{(3^n - 1)}{2}$$

For $n=1$, we have

$$P(1) := \frac{(3^1 - 1)}{2} = \frac{3-1}{2} = \frac{2}{2} = 1, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1 + 3 + 3^2 + \dots + 3^{k-1} = \frac{(3^k - 1)}{2} \quad \dots\dots(i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1 + 3 + 3^2 + \dots + 3^{k-1} + 3^{(k+1)-1} \\ &= (1 + 3 + 3^2 + \dots + 3^{k-1}) + 3^k \\ &= \frac{(3^k - 1)}{2} + 3^k \quad [\text{Using (i)}] \\ &= \frac{(3^k - 1) + 2 \cdot 3^k}{2} \\ &= \frac{(1 + 2)3^k - 1}{2} \\ &= \frac{3 \cdot 3^k - 1}{2} \\ &= \frac{3^{k+1} - 1}{2} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 2:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1^3 + 2^3 + 3^3 + \dots + n^3 = \left(\frac{n(n+1)}{2} \right)^2$$

Solution 2:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1^3 + 2^3 + 3^3 + \dots + n^3 = \left(\frac{n(n+1)}{2} \right)^2$$

For $n=1$, we have

$$P(1): 1^3 = 1 = \left(\frac{1(1+1)}{2} \right)^2 = \left(\frac{1 \cdot 2}{2} \right)^2 = 1^2 = 1, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1^3 + 2^3 + 3^3 + \dots + k^3 = \left(\frac{k(k+1)}{2} \right)^2 \quad \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1^3 + 2^3 + 3^3 + \dots + k^3 + (k+1)^3 \\ &= (1^3 + 2^3 + 3^3 + \dots + k^3) + (k+1)^3 \\ &= \left(\frac{k(k+1)}{2} \right)^2 + (k+1)^3 \quad \quad \quad [\text{Using (i)}] \\ &= \frac{k^2(k+1)^2}{4} + (k+1)^3 \\ &= \frac{k^2(k+1)^2 + 4(k+1)^3}{4} \\ &= \frac{(k+1)^2 \{k^2 + 4(k+1)\}}{4} \\ &= \frac{(k+1)^2 \{k^2 + 4k + 4\}}{4} \\ &= \frac{(k+1)^2 (k+2)^2}{4} \\ &= \frac{(k+1)^2 (k+1+1)^2}{4} \\ &= \left(\frac{(k+1)(k+1+1)}{2} \right)^2 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 3:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1 + \frac{1}{(1+2)} + \frac{1}{(1+2+3)} + \dots + \frac{1}{(1+2+3+\dots+n)} = \frac{2n}{(n+1)}$$

Solution 3:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1 + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+n} = \frac{2n}{n+1}$$

For $n=1$, we have

$$P(1): 1 = \frac{2 \cdot 1}{1+1} = \frac{2}{2} = 1, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1 + \frac{1}{1+2} + \dots + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+k} = \frac{2k}{k+1} \dots\dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1 + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+k} + \frac{1}{1+2+3+\dots+k+(k+1)} \\ &= \left(1 + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+k} \right) + \frac{1}{1+2+3+\dots+k+(k+1)} \\ &= \frac{2k}{k+1} + \frac{1}{1+2+3+\dots+k+(k+1)} \quad \text{[Using (i)]} \\ &= \frac{2k}{k+1} + \frac{1}{\left(\frac{(k+1)(k+1+1)}{2} \right)} \quad \left[1+2+3+\dots+n = \frac{n(n+1)}{2} \right] \\ &= \frac{2k}{(k+1)} + \frac{2}{(k+1)(k+2)} \\ &= \frac{2}{(k+1)} \left(k + \frac{1}{k+2} \right) \\ &= \frac{2}{(k+1)} \left(\frac{k^2 + 2k + 1}{k+2} \right) \\ &= \frac{2}{(k+1)} \left[\frac{(k+1)^2}{k+2} \right] \\ &= \frac{2(k+1)}{(k+2)} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbb{N} .

Question 4:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1.2.3 + 2.3.4 + \dots + n(n+1)(n+2) = \frac{n(n+1)(n+2)(n+3)}{4}$$

Solution 4:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1.2.3 + 2.3.4 + \dots + n(n+1)(n+2) = \frac{n(n+1)(n+2)(n+3)}{4}$$

For $n=1$, we have

$$P(1): 1.2.3 = 6 = \frac{1(1+1)(1+2)(1+3)}{4} = \frac{1.2.3.4}{4} = 6, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1.2.3 + 2.3.4 + \dots + k(k+1)(k+2) = \frac{k(k+1)(k+2)(k+3)}{4} \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1.2.3 + 2.3.4 + \dots + k(k+1)(k+2) + (k+1)(k+2)(k+3) \\ &= \{1.2.3 + 2.3.4 + \dots + k(k+1)(k+2)\} + (k+1)(k+2)(k+3) \\ &= \frac{k(k+1)(k+2)(k+3)}{4} + (k+1)(k+2)(k+3) \quad [\text{Using (i)}] \\ &= (k+1)(k+2)(k+3) \left(\frac{k}{4} + 1 \right) \\ &= \frac{(k+1)(k+2)(k+3)(k+4)}{4} \\ &= \frac{(k+1)(k+1+1)(k+1+2)(k+1+3)}{4} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 5:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1.3 + 2.3^2 + 3.3^3 + \dots + n.3^n = \frac{(2n-1)3^{n+1} + 3}{4}$$

Solution 5:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1.3 + 2.3^2 + 3.3^3 + \dots + n.3^n = \frac{(2n-1)3^{n+1} + 3}{4}$$

For $n=1$, we have

$$P(1): 1.3 = 3 = \frac{(2.1-1)3^{1+1} + 3}{4} = \frac{3^2 + 3}{4} = \frac{12}{4} = 3, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1.3 + 2.3^2 + 3.3^3 + \dots + k.3^k = \frac{(2k-1)3^{k+1} + 3}{4} \dots\dots(i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1.3 + 2.3^2 + 3.3^3 + \dots + k.3^k + (k+1).3^{k+1} \\ &= (1.3 + 2.3^2 + 3.3^3 + \dots + k.3^k) + (k+1).3^{k+1} \\ &= \frac{(2k-1)3^{k+1} + 3}{4} + (k+1).3^{k+1} \quad [\text{Using (i)}] \\ &= \frac{(2k-1)3^{k+1} + 3 + 4(k+1)3^{k+1}}{4} \\ &= \frac{3^{k+1} \{2k-1+4(k+1)\} + 3}{4} \\ &= \frac{3^{k+1} \{6k+3\} + 3}{4} \\ &= \frac{3^{k+1}.3\{2k+1\} + 3}{4} \\ &= \frac{3^{(k+1)+1} \{2k+1\} + 3}{4} \\ &= \frac{\{2(k+1)-1\}3^{(k+1)+1} + 3}{4} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbb{N} .

Question 6:

Prove the following by using the principle of mathematical induction for all $n \in \mathbb{N}$:

$$1.2 + 2.3 + 3.4 + \dots + n.(n+1) = \left[\frac{n(n+1)(n+2)}{3} \right]$$

Solution 6:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1.2 + 2.3 + 3.4 + \dots + n.(n+1) = \left[\frac{n(n+1)(n+2)}{3} \right]$$

For $n = 1$, we have

$$P(1): 1.2 = 2 = \frac{1(1+1)(1+2)}{3} = \frac{1.2.3}{3} = 2, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1.2 + 2.3 + 3.4 + \dots + k.(k+1) = \left[\frac{k(k+1)(k+2)}{3} \right] \dots\dots(i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & 1.2 + 2.3 + 3.4 + \dots + k.(k+1) + (k+1).(k+2) \\ &= [1.2 + 2.3 + 3.4 + \dots + k.(k+1)] + (k+1).(k+2) \\ &= \frac{k(k+1)(k+2)}{3} + (k+1)(k+2) \quad \quad \quad [\text{Using (i)}] \\ &= (k+1)(k+2) \left(\frac{k}{3} + 1 \right) \\ &= \frac{(k+1)(k+2)(k+3)}{3} \\ &= \frac{(k+1)(k+1+1)(k+1+2)}{3} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 7:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1.3 + 3.5 + 5.7 + \dots + (2n-1)(2n+1) = \frac{n(4n^2 + 6n - 1)}{3}$$

Solution 7:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1.3 + 3.5 + 5.7 + \dots + (2n-1)(2n+1) = \frac{n(4n^2 + 6n - 1)}{3}$$

For $n = 1$, we have

$$P(1): 1.3 = 3 = \frac{1(4.1^2 + 6.1 - 1)}{3} = \frac{4 + 6 - 1}{3} = \frac{9}{3} = 3, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1.3 + 3.5 + 5.7 + \dots + (2k-1)(2k+1) = \frac{k(4k^2 + 6k - 1)}{3} \dots\dots(i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & (1.3 + 3.5 + 5.7 + \dots + (2k-1)(2k+1)) + \{(k+1)-1\}\{2(k+1)+1\} \\ &= \frac{k(4k^2 + 6k - 1)}{3} + (2k+2-1)(2k+2+1) \quad [\text{Using (i)}] \\ &= \frac{k(4k^2 + 6k - 1)}{3} + (2k+1)(2k+3) \\ &= \frac{k(4k^2 + 6k - 1)}{3} + (4k^2 + 8k + 3) \\ &= \frac{k(4k^2 + 6k - 1) + 3(4k^2 + 8k + 3)}{3} \\ &= \frac{4k^3 + 6k^2 - k + 12k^2 + 24k + 9}{3} \\ &= \frac{4k^3 + 18k^2 + 23k + 9}{3} \\ &= \frac{4k^3 + 14k^2 + 9k + 4k^2 + 14k + 9}{3} \\ &= \frac{k(4k^2 + 14k + 9) + 1(4k^2 + 14k + 9)}{3} \\ &= \frac{(k+1)(4k^2 + 14k + 9)}{3} \\ &= \frac{(k+1)\{4k^2 + 8k + 4 + 6k + 6 - 1\}}{3} \\ &= \frac{(k+1)\{4(k^2 + 2k + 1) + 6(k+1) - 1\}}{3} \\ &= \frac{(k+1)\{4(k+1)^2 + 6(k+1) - 1\}}{3} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 8:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1.2 + 2.2^2 + 3.2^2 + \dots + n.2^n = (n-1)2^{n+1} + 2$$

Solution 8:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1.2 + 2.2^2 + 3.2^2 + \dots + n.2^n = (n-1)2^{n+1} + 2$$

For $n = 1$, we have

$$P(1): 1.2 = 2 = (1-1)2^{1+1} + 2 = 0 + 2 = 2, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1.2 + 2.2^2 + 3.2^2 + \dots + k.2^k = (k-1)2^{k+1} + 2 \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & \{1.2 + 2.2^2 + 3.2^2 + \dots + k.2^k\} + (k+1).2^{k+1} \\ &= (k-1)2^{k+1} + 2 + (k+1)2^{k+1} \\ &= 2^{k+1} \{(k-1) + (k+1)\} + 2 \\ &= 2^{k+1}.2k + 2 \\ &= k.2^{(k+1)+1} + 2 \\ &= \{(k+1)-1\}2^{(k+1)+1} + 2 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 9:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^n} = 1 - \frac{1}{2^n}$$

Solution 9:

Let the given statement be $P(n)$, i.e.,

$$P(n): \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^n} = 1 - \frac{1}{2^n}$$

For $n = 1$, we have

$$P(1): \frac{1}{2} = 1 - \frac{1}{2^1} = \frac{1}{2}, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^k} = 1 - \frac{1}{2^k} \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & \left(\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^k} \right) + \frac{1}{2^{k+1}} \\ &= \left(1 - \frac{1}{2^k} \right) + \frac{1}{2^{k+1}} \quad [\text{Using (i)}] \end{aligned}$$

$$\begin{aligned}
 & 1 - \frac{1}{2^k} \left(1 - \frac{1}{2} \right) \\
 &= 1 - \frac{1}{2^k} \left(\frac{1}{2} \right) \\
 &= 1 - \frac{1}{2^{k+1}}
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 10:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\frac{1}{2.5} + \frac{1}{5.8} + \frac{1}{8.11} + \dots + \frac{1}{(3n-1)(3n+2)} = \frac{n}{(6n+4)}$$

Solution 10:

Let the given statement be $P(n)$, i.e.,

$$P(n): \frac{1}{2.5} + \frac{1}{5.8} + \frac{1}{8.11} + \dots + \frac{1}{(3n-1)(3n+2)} = \frac{n}{(6n+4)}$$

For $n=1$, we have

$$P(1) = \frac{1}{2.5} = \frac{1}{10} = \frac{1}{6.1+4} = \frac{1}{10}, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$\frac{1}{2.5} + \frac{1}{5.8} + \frac{1}{8.11} + \dots + \frac{1}{(3k+1)(3k+2)} = \frac{k}{6k+4} \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned}
 & \frac{1}{2.5} + \frac{1}{5.8} + \frac{1}{8.11} + \dots + \frac{1}{(3k+1)(3k+2)} + \frac{1}{\{3(k+1)-1\}\{3(k+1)+2\}} \\
 &= \frac{k}{6k+4} + \frac{1}{(3k+3-1)(3k+3+2)} \quad \quad \quad [\text{Using (i)}] \\
 &= \frac{k}{6k+4} + \frac{1}{(3k+2)(3k+5)} \\
 &= \frac{k}{2(3k+2)} + \frac{1}{(3k+2)(3k+5)} \\
 &= \frac{1}{(3k+2)} \left(\frac{k}{2} + \frac{1}{3k+5} \right) \\
 &= \frac{1}{(3k+2)} \left(\frac{k(3k+5)+2}{2(3k+5)} \right)
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{1}{(3k+2)} \left(\frac{3k^2+5k+2}{2(3k+5)} \right) \\
 &= \frac{1}{(3k+2)} \left(\frac{(3k+2)(k+1)}{2(3k+5)} \right) \\
 &= \frac{(k+1)}{6k+10} \\
 &= \frac{(k+1)}{6(k+1)+4}
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 11:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\frac{1}{1.2.3} + \frac{1}{2.3.4} + \frac{1}{3.4.5} + \dots + \frac{1}{n(n+1)(n+2)} = \frac{n(n+3)}{4(n+1)(n+2)}$$

Solution 11:

Let the given statement be $P(n)$, i.e.,

$$P(n): \frac{1}{1.2.3} + \frac{1}{2.3.4} + \frac{1}{3.4.5} + \dots + \frac{1}{n(n+1)(n+2)} = \frac{n(n+3)}{4(n+1)(n+2)}$$

For $n = 1$, we have

$$P(1): \frac{1}{1 \cdot 2 \cdot 3} = \frac{1 \cdot (1+3)}{4(1+1)(1+2)} = \frac{1 \cdot 4}{4 \cdot 2 \cdot 3} = \frac{1}{1 \cdot 2 \cdot 3}, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$\frac{1}{1.2.3} + \frac{1}{2.3.4} + \frac{1}{3.4.5} + \dots + \frac{1}{k(k+1)(k+2)} = \frac{k(k+3)}{4(k+1)(k+2)} \quad \dots (i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned}
 &\left[\frac{1}{1 \cdot 2 \cdot 3} + \frac{1}{2 \cdot 3 \cdot 4} + \frac{1}{3 \cdot 4 \cdot 5} + \dots + \frac{1}{k(k+1)(k+2)} \right] + \frac{1}{(k+1)(k+2)(k+3)} \\
 &= \frac{k(k+3)}{4(k+1)(k+2)} + \frac{1}{(k+1)(k+2)(k+3)} \quad \text{[Using (i)]} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k(k+3)}{4} + \frac{1}{k+3} \right\}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k(k+3)^2 + 4}{4(k+3)} \right\} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k(k^2 + 6k + 9) + 4}{4(k+3)} \right\} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k^3 + 6k^2 + 9k + 4}{4(k+3)} \right\} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k^3 + 2k^2 + k + 4k^2 + 8k + 4}{4(k+3)} \right\} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k(k^2 + 2k + 1) + 4(k^2 + 2k + 1)}{4(k+3)} \right\} \\
 &= \frac{1}{(k+1)(k+2)} \left\{ \frac{k(k+1)^2 + 4(k+1)^2}{4(k+3)} \right\} \\
 &= \frac{(k+1)^2(k+4)}{4(k+1)(k+2)(k+3)} \\
 &= \frac{(k+1)\{(k+1)+3\}}{4\{(k+1)+1\}\{(k+1)+2\}}
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 12:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$a + ar + ar^2 + \dots + ar^{n-1} = \frac{a(r^n - 1)}{r - 1}$$

Solution 12:

Let the given statement be $P(n)$, i.e.,

$$P(n): a + ar + ar^2 + \dots + ar^{n-1} = \frac{a(r^n - 1)}{r - 1}$$

For $n = 1$, we have

$$P(1): a = \frac{a(r^1 - 1)}{(r - 1)} = a, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$a + ar + ar^2 + \dots + ar^{k-1} = \frac{a(r^k - 1)}{r - 1} \dots\dots(i)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned}
 & \{a + ar + ar^2 + \dots + ar^{k-1}\} + ar^{(k+1)-1} \\
 &= \frac{a(r^k - 1)}{r - 1} + ar^k \quad [\text{Using (i)}] \\
 &= \frac{a(r^k - 1) + ar^k(r - 1)}{r - 1} \\
 &= \frac{a(r^k - 1) + ar^{k+1} - ar^k}{r - 1} \\
 &= \frac{ar^{k+1} - a}{r - 1} \\
 &= \frac{a(r^{k+1} - 1)}{r - 1}
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 13:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\left(1 + \frac{3}{1}\right)\left(1 + \frac{5}{4}\right)\left(1 + \frac{7}{9}\right) \dots \left(1 + \frac{(2n+1)}{n^2}\right) = (n+1)^2$$

Solution 13:

Let the given statement be $P(n)$, i.e.,

$$P(n): \left(1 + \frac{3}{1}\right)\left(1 + \frac{5}{4}\right)\left(1 + \frac{7}{9}\right) \dots \left(1 + \frac{(2n+1)}{n^2}\right) = (n+1)^2$$

For $n = 1$, we have

$$P(1): \left(1 + \frac{3}{1}\right) = 4 = (1+1)^2 = 2^2 = 4, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$\left(1 + \frac{3}{1}\right)\left(1 + \frac{5}{4}\right)\left(1 + \frac{7}{9}\right) \dots \left(1 + \frac{(2k+1)}{k^2}\right) = (k+1)^2 \dots (1)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned}
 & \left[\left(1 + \frac{3}{1}\right)\left(1 + \frac{5}{4}\right)\left(1 + \frac{7}{9}\right) \dots \left(1 + \frac{(2k+1)}{k^2}\right) \right] \left[1 + \frac{2(k+1)+1}{(k+1)^2} \right] \\
 &= (k+1)^2 \left[1 + \frac{2(k+1)+1}{(k+1)^2} \right] \quad [\text{Using (1)}]
 \end{aligned}$$

$$\begin{aligned}
 &= (k+1)^2 \left[\frac{(k+1)^2 + 2(k+1) + 1}{(k+1)^2} \right] \\
 &= (k+1)^2 + 2(k+1) + 1 \\
 &= \{(k+1) + 1\}^2
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 14:

Prove the following by using principle of mathematical induction for all $n \in N$:

$$\left(1 + \frac{1}{1}\right) \left(1 + \frac{1}{2}\right) \left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{n}\right) = (n+1)$$

Solution 14:

Let the given statement be $P(n)$, i.e.,

$$P(n): \left(1 + \frac{1}{1}\right) \left(1 + \frac{1}{2}\right) \left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{n}\right) = (n+1)$$

For $n = 1$, we have

$$P(1): \left(1 + \frac{1}{1}\right) = 2 = (1+1), \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$P(k): \left(1 + \frac{1}{1}\right) \left(1 + \frac{1}{2}\right) \left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{k}\right) = (k+1) \dots \dots (1)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned}
 &\left[\left(1 + \frac{1}{1}\right) \left(1 + \frac{1}{2}\right) \left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{k}\right) \right] \left(1 + \frac{1}{k+1}\right) \\
 &= (k+1) \left(1 + \frac{1}{k+1}\right) \quad \quad \quad [\text{Using (1)}] \\
 &= (k+1) \left[\frac{(k+1)+1}{(k+1)} \right] \\
 &= (k+1) + 1
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 15:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1^2 + 3^2 + 5^2 + \dots + (2n-1)^2 = \frac{n(2n-1)(2n+1)}{3}$$

Solution 15:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1^2 + 3^2 + 5^2 + \dots + (2n-1)^2 = \frac{n(2n-1)(2n+1)}{3}$$

For $n=1$, we have

$$P(1) = 1^2 = 1 = \frac{1(2 \cdot 1 - 1)(2 \cdot 1 + 1)}{3} = \frac{1 \cdot 1 \cdot 3}{3} = 1, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$P(k) = 1^2 + 3^2 + 5^2 + \dots + (2k-1)^2 = \frac{k(2k-1)(2k+1)}{3} \dots (1)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & \{1^2 + 3^2 + 5^2 + \dots + (2k-1)^2\} + \{2(k+1)-1\}^2 \\ &= \frac{k(2k-1)(2k+1)}{3} + (2k+2-1)^2 \quad \quad \quad [\text{Using (1)}] \\ &= \frac{k(2k-1)(2k+1)}{3} + (2k+1)^2 \\ &= \frac{2(2k-1)(2k+1) + 3(2k+1)^2}{3} \\ &= \frac{(2k+1)\{k(2k-1) + 3(2k+1)\}}{3} \\ &= \frac{(2k+1)\{2k^2 - k + 6k + 3\}}{3} \\ &= \frac{(2k+1)\{2k^2 + 5k + 3\}}{3} \\ &= \frac{(2k+1)\{2k^2 + 2k + 3k + 3\}}{3} \\ &= \frac{(2k+1)\{2k(k+1) + 3(k+1)\}}{3} \\ &= \frac{(2k+1)(k+1)(2k+3)}{3} \\ &= \frac{(k+1)\{2(k+1)-1\}\{2(k+1)+1\}}{3} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 16:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\frac{1}{1.4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \frac{1}{(3n-2)(3n+1)} = \frac{n}{(3n+1)}$$

Solution 16:

Let the given statement be $P(n)$, i.e.,

$$P(n): \frac{1}{1.4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \frac{1}{(3n-2)(3n+1)} = \frac{n}{(3n+1)}$$

For $n = 1$, we have

$$P(1) = \frac{1}{1.4} = \frac{1}{3.1+1} = \frac{1}{4} + \frac{1}{1.4}, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$P(k) = \frac{1}{1.4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \frac{1}{(3k-2)(3k+1)} = \frac{k}{3k+1} \dots\dots(1)$$

We shall now prove that $P(k+1)$ is true.

Consider

$$\begin{aligned} & \left\{ \frac{1}{1.4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \frac{1}{(3k-2)(3k+1)} \right\} + \frac{1}{\{3(k+1)-2\}\{3(k+1)+1\}} \\ &= \frac{k}{3k+1} + \frac{1}{(3k+1)(3k+4)} \quad \text{[Using (1)]} \\ &= \frac{1}{(3k+1)} \left\{ k + \frac{1}{(3k+4)} \right\} \\ &= \frac{1}{(3k+1)} \left\{ \frac{k(3k+4)+1}{(3k+4)} \right\} \\ &= \frac{1}{(3k+1)} \left\{ \frac{3k^2+4k+1}{(3k+4)} \right\} \\ &= \frac{1}{(3k+1)} \left\{ \frac{3k^2+3k+k+1}{(3k+4)} \right\} \\ &= \frac{(3k+1)(k+1)}{(3k+1)(3k+4)} \\ &= \frac{(k+1)}{3(k+1)+1} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 17:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$\frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \dots + \frac{1}{(2n+1)(2n+3)} = \frac{n}{3(2n+3)}$$

Solution 17:

Let the given statement be $P(n)$, i.e.,

$$P(n): \frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \dots + \frac{1}{(2n+1)(2n+3)} = \frac{n}{3(2n+3)}$$

For $n = 1$, we have

$$P(1): \frac{1}{3.5} = \frac{1}{3(2.1+3)} = \frac{1}{3.5}, \text{ which is true.}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$P(k): \frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \dots + \frac{1}{(2k+1)(2k+3)} = \frac{k}{3(2k+3)} \dots (1)$$

We shall now prove that $P(k+1)$ is true. Consider

$$\begin{aligned} & \left[\frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \dots + \frac{1}{(2k+1)(2k+3)} \right] + \frac{1}{\{2(k+1)+1\}\{2(k+1)+3\}} \\ &= \frac{k}{3(2k+3)} + \frac{1}{(2k+3)(2k+5)} \quad \text{[Using (1)]} \\ &= \frac{1}{(2k+3)} \left[\frac{k}{3} + \frac{1}{(2k+5)} \right] \\ &= \frac{1}{(2k+3)} \left[\frac{k(2k+5)+3}{3(2k+5)} \right] \\ &= \frac{1}{(2k+3)} \left[\frac{2k^2+5k+3}{3(2k+5)} \right] \\ &= \frac{1}{(2k+3)} \left[\frac{2k^2+2k+3k+3}{3(2k+5)} \right] \\ &= \frac{1}{(2k+3)} \left[\frac{2k(k+1)+3(k+1)}{3(2k+5)} \right] \\ &= \frac{(k+1)(2k+3)}{3(2k+3)(2k+5)} \\ &= \frac{(k+1)}{3\{2(k+1)+3\}} \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 18:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$1 + 2 + 3 + \dots + n < \frac{1}{8}(2n+1)^2$$

Solution 18:

Let the given statement be $P(n)$, i.e.,

$$P(n): 1 + 2 + 3 + \dots + n < \frac{1}{8}(2n+1)^2$$

It can be noted that $P(n)$ is true for $n = 1$ since

$$1 < \frac{1}{8}(2 \cdot 1 + 1)^2 = \frac{9}{8}$$

Let $P(k)$ be true for some positive integer k , i.e.,

$$1 + 2 + \dots + k < \frac{1}{8}(2k+1)^2 \dots (1)$$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$(1 + 2 + \dots + k) + (k+1) < \frac{1}{8}(2k+1)^2 + (k+1) \quad [\text{Using (1)}]$$

$$< \frac{1}{8}\{(2k+1)^2 + 8(k+1)\}$$

$$< \frac{1}{8}\{4k^2 + 4k + 1 + 8k + 8\}$$

$$< \frac{1}{8}\{4k^2 + 12k + 9\}$$

$$< \frac{1}{8}(2k+3)^2$$

$$< \frac{1}{8}\{2(k+1)+1\}^2$$

$$\text{Hence, } (1 + 2 + 3 + \dots + k) + (k+1) < \frac{1}{8}(2k+1)^2 + (k+1)$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 19:

Prove the following by using the principle of mathematical induction for all $n \in N$:

$$n(n+1)(n+5) \text{ is a multiple of 3.}$$

Solution 19:

Let the given statement be $P(n)$, i.e.,

$$P(n): n(n+1)(n+5), \text{ which is a multiple of 3.}$$

It can be noted that $P(n)$ is true for $n = 1$ since $1(1+1)(1+5) = 12$, which is a multiple of 3.

Let $P(k)$ be true for some positive integer k , i.e.,

$k(k+1)(k+5)$ is a multiple of 3.

$$\therefore k(k+1)(k+5) = 3m, \text{ where } m \in \mathbf{N} \dots (1)$$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$\begin{aligned} & (k+1)\{(k+1)+1\}\{(k+1)+5\} \\ &= (k+1)(k+2)\{(k+5)+1\} \\ &= (k+1)(k+2)(k+5) + (k+1)(k+2) \\ &= \{k(k+1)(k+5) + 2(k+1)(k+5)\} + (k+1)(k+2) \\ &= 3m + (k+1)\{2(k+5) + (k+2)\} \\ &= 3m + (k+1)\{2k+10+k+2\} \\ &= 3m + (k+1)\{3k+12\} \\ &= 3m + 3(k+1)\{k+4\} \\ &= 3\{m + (k+1)(k+4)\} = 3 \times q, \text{ where } q = \{m + (k+1)(k+4)\} \text{ is some natural number.} \end{aligned}$$

Therefore, $(k+1)\{(k+1)+1\}\{(k+1)+5\}$ is a multiple of 3.

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbf{N} .

Question 20:

Prove the following by using the principle of mathematical induction for all $n \in \mathbf{N}$:

$$10^{2n-1} + 1 \text{ is divisible by 11.}$$

Solution 20:

Let the given statement be $P(n)$, i.e.,

$$P(n): 10^{2n-1} + 1 \text{ is divisible by 11.}$$

It can be observed that $P(n)$ is true for $n = 1$

Since $P(1) = 10^{2 \cdot 1 - 1} + 1 = 11$, which is divisible by 11.

Let $P(k)$ be true for some positive integer k ,

i.e., $10^{2k-1} + 1$ is divisible by 11.

$$\therefore 10^{2k-1} + 1 = 11m, \text{ where}$$

$$m \in \mathbf{N} \dots (1)$$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$\begin{aligned} & 10^{2(k+1)-1} + 1 \\ &= 10^{2k+2-1} + 1 \end{aligned}$$

$$\begin{aligned}
 &= 10^{2k+1} + 1 \\
 &= 10^2 (10^{2k-1} + 1 - 1) + 1 \\
 &= 10^2 (10^{2k-1} + 1) - 10^2 + 1 \\
 &= 10^2 \cdot 11m - 100 + 1 && \text{[Using (1)]} \\
 &= 100 \times 11m - 99 \\
 &= 11(100m - 9) \\
 &= 11r, \text{ where } r = (100m - 9) \text{ is some natural number}
 \end{aligned}$$

Therefore, $10^{2(k+1)-1} + 1$ is divisible by 11.

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbb{N} .

Question 21:

Prove the following by using the principle of mathematical induction for all $n \in \mathbb{N}$:

$x^{2n} - y^{2n}$ is divisible by $x + y$.

Solution 21:

Let the given statement be $P(n)$, i.e.,

$P(n): x^{2n} - y^{2n}$ is divisible by $x + y$.

It can be observed that $P(n)$ is true for $n = 1$.

This is so because $x^{2 \times 1} - y^{2 \times 1} = x^2 - y^2 = (x + y)(x - y)$ is divisible by $(x + y)$.

Let $P(k)$ be true for some positive integer k , i.e.,

$x^{2k} - y^{2k}$ is divisible by $x + y$.

\therefore Let $x^{2k} - y^{2k} = m(x + y)$, where $m \in \mathbb{N} \dots (1)$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$\begin{aligned}
 &x^{2(k+1)} - y^{2(k+1)} \\
 &= x^{2k} \cdot x^2 - y^{2k} \cdot y^2 \\
 &= x^2 (x^{2k} - y^{2k} + y^{2k}) - y^{2k} \cdot y^2 \\
 &= x^2 \{m(x + y) + y^{2k}\} - y^{2k} \cdot y^2 && \text{[Using (1)]} \\
 &= m(x + y)x^2 + y^{2k} \cdot x^2 - y^{2k} \cdot y^2 \\
 &= m(x + y)x^2 + y^{2k}(x^2 - y^2) \\
 &= m(x + y)x^2 + y^{2k}(x + y)(x - y) \\
 &= (x + y)\{mx^2 + y^{2k}(x - y)\}, \text{ which is a factor of } (x + y).
 \end{aligned}$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., N .

Question 22:

Prove the following by using the principle of mathematical induction for all $n \in N : 3^{2n+2} - 8n - 9$ is divisible by 8.

Solution 22:

Let the given statement be $P(n)$, i.e.,

$P(n) : 3^{2n+2} - 8n - 9$ is divisible by 8.

It can be observed that $P(n)$ is true for $n = 1$

Since $3^{2 \times 1 + 2} - 8 \times 1 - 9 = 64$, which is divisible by 8.

Let $P(k)$ be true for some positive integer

k , i.e., $3^{2k+2} - 8k - 9$ is divisible by 8.

$\therefore 3^{2k+2} - 8k - 9 = 8m$; where $m \in N \dots \dots (1)$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$3^{2(k+1)+2} - 8(k+1) - 9$$

$$3^{2k+2} \cdot 3^2 - 8k - 8 - 9$$

$$= 3^2 (3^{2k+2} - 8k - 9 + 8k + 9) - 8k - 17$$

$$= 3^2 (3^{2k+2} - 8k - 9) + 3^2 (8k + 9) - 8k - 17$$

$$= 9.8m + 9(8k + 9) - 8k - 17$$

$$= 9.8m + 72k + 81 - 8k - 17$$

$$= 9.8m + 64k + 64$$

$$= 8(9m + 8k + 8)$$

$$= 8r, \text{ where } r = (9m + 8k + 8) \text{ is a natural number}$$

Therefore, $3^{2(k+1)+2} - 8(k+1) - 9$ is divisible by 8.

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all numbers i.e., N .

Question 23:

Prove the following by using the principle of mathematical induction for all $n \in N$: $41^n - 14^n$ is a multiple of 27.

Solution 23:

Let the given statement be $P(n)$, i.e.,

$P(n) : 41^n - 14^n$ is a multiple of 27.

It can be observed that $P(n)$ is true for $n = 1$

Since $41^1 - 14^1 = 27$, which is a multiple of 27.

Let $P(k)$ be true for some positive integer k , i.e.,

$41^k - 14^k$ is a multiple of 27

$$\therefore 41^k - 14^k = 27m, \quad m \in \mathbb{N} \dots (1)$$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$\begin{aligned} &41^{k+1} - 14^{k+1} \\ &= 41^k \cdot 41 - 14^k \cdot 14 \\ &= 41(41^k - 14^k + 14^k) - 14^k \cdot 14 \\ &= 41 \cdot 27m + 14^k(41 - 14) \\ &= 41 \cdot 27m + 27 \cdot 14^k \\ &= 27(41m + 14^k) \\ &= 27 \times r, \text{ where } r = (41m + 14^k) \text{ is a natural number.} \end{aligned}$$

Therefore, $41^{k+1} - 14^{k+1}$ is a multiple of 27.

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbb{N} .

Question 24:

Prove the following by using the principle of mathematical induction for all $n \in \mathbb{N}$:

$$(2n+7) < (n+3)^2$$

Solution 24:

Let the given statement be $P(n)$, i.e.,

$$P(n): (2n+7) < (n+3)^2$$

It can be observed that $P(n)$ is true for $n = 1$

Since $2 \cdot 1 + 7 = 9 < (1+3)^2 = 16$, which is true.

Let $P(k)$ be true for some positive integer k , i.e.,

$$(2k+7) < (k+3)^2 \dots (1)$$

We shall now prove that $P(k+1)$ is true whenever $P(k)$ is true.

Consider

$$\{2(k+1)+7\} = (2k+7)+2$$

$$\therefore \{2(k+1)+7\} = (2k+7)+2 < (k+3)^2 + 2 \quad [\text{Using (1)}]$$

$$2(k+1)+7 < k^2 + 6k + 9 + 2$$

$$2(k+1)+7 < k^2 + 6k + 11$$

Now, $k^2 + 6k + 11 < k^2 + 8k + 16$

$$\therefore 2(k+1) + 7 < (k+4)^2$$

$$2(k+1) + 7 < \{(k+1) + 3\}^2$$

Thus, $P(k+1)$ is true whenever $P(k)$ is true.

Hence, by the principle of mathematical induction, statement $P(n)$ is true for all natural numbers i.e., \mathbb{N} .

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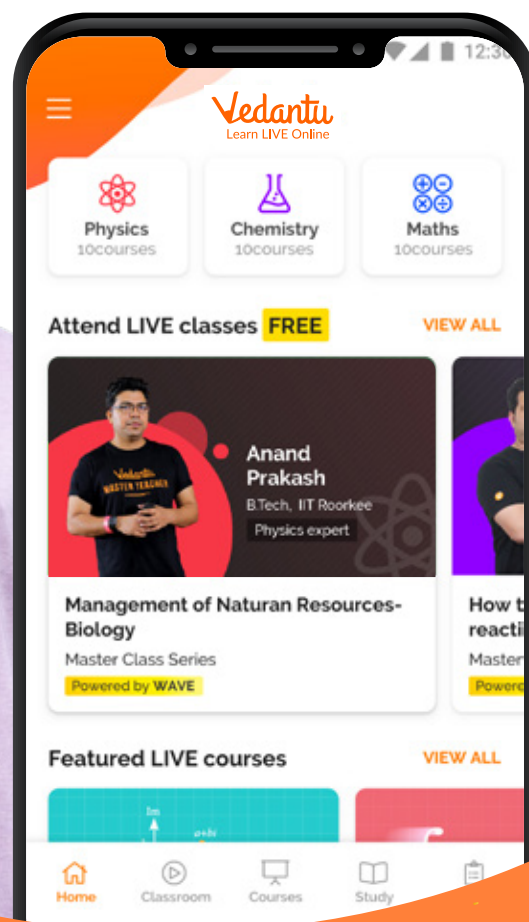
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